

Bridging Ostrom's governance theory to dynamic adaptive policy pathway (DAPP) maps: theory and application example

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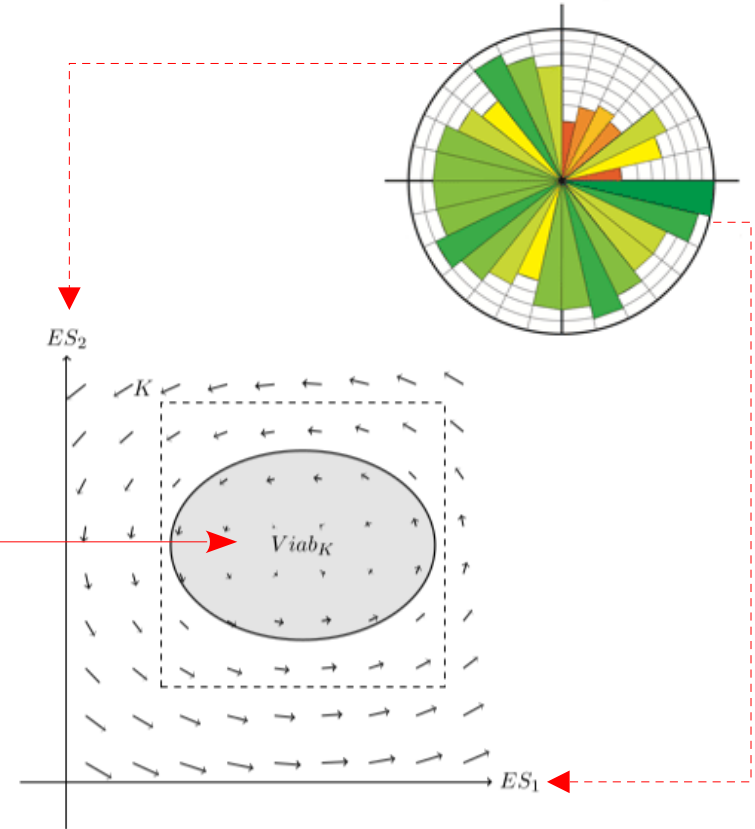
Viability of a dynamical system in SES

Axiological definition (value theory)

System's value, its robustness, durability, resilience, f(utilitarian, ethic, aesthetic values)

Viability (robustness):

$$\text{Viab}_f(K) = \{ \mathbf{x}(0) \in K \mid \exists u(\cdot) \in U \text{ such that } \forall t \geq 0, \mathbf{x}(u(\cdot)) \in K \}$$



Difference between

viability or adaptation

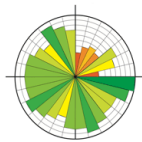
Adaptation of a dynamical system in SES

Praxeological definition (theory of action)

Planning actions & decisions, nodes, transitions, collective vs indiv., effectiveness, etc ...

Set of actions:

$$U = \{u_1, u_2, u_3, u_4, u_5\}$$



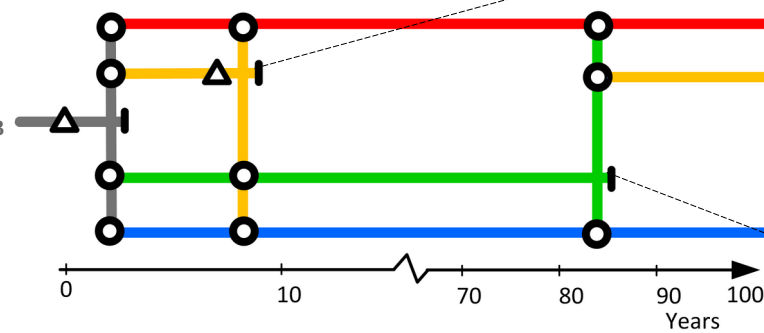
Action u_1

Action u_2

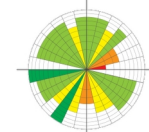
Action u_3

Action u_4

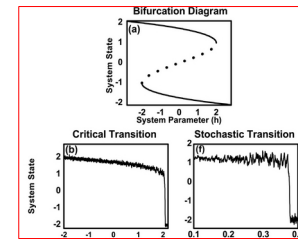
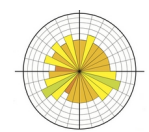
Action u_5



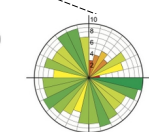
$x(u_2(t_7)) \in K$



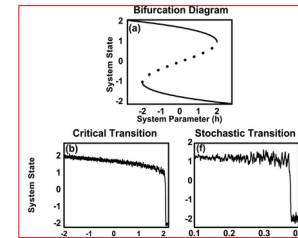
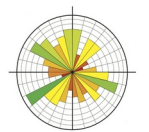
$x(u_2(t_8)) \notin K$



$x(u_4(t_{84})) \in K$



$x(u_4(t_{85})) \notin K$



What is a DAPP map?

Definition independent from viability

Conditions (actions, time):

- Set of actions: $\mathbf{U} = \{u_1, u_2, \dots, u_i, \dots, u_m\}$,
- Time sequence: $T = \{t_0, t_1, \dots, t_j, \dots, t_n\}$,

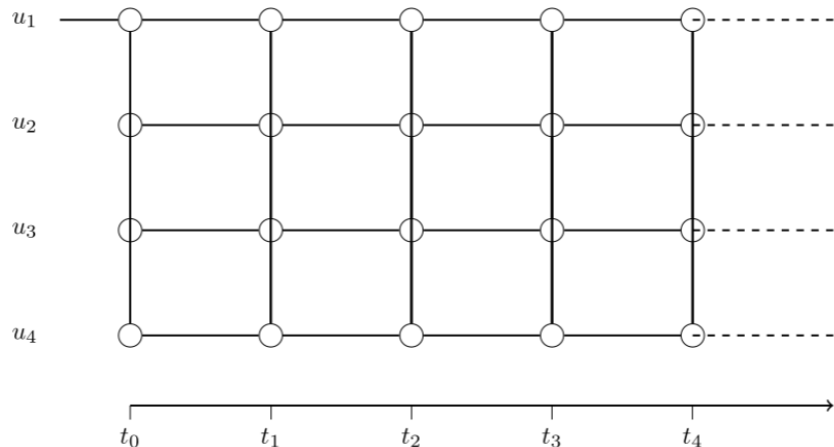
A policy pathway (i.e. DAPP) $u(\cdot)$:

$$u(\cdot) = u(t_0), u(t_1), \dots, u(t_j), \dots, u(t_n) \quad \text{such that} \quad u(t_j) \in \mathbf{U} \quad (32)$$

DAPP map (graph)

DAPP Graph: $\mathcal{G} = V \times E$ with $\dim(\mathcal{G}) = U^T$

- Vertex $V \rightarrow U \times T$ representing decision nodes at time t_0, t_1, \dots, t_n for every possible action u , such that $V = \bigcup_{t=0}^T U(x(t))$
- Edges $E \rightarrow U^T$ possible transition pathways under control $u(t)$ between decision nodes V .



$$\mathcal{G} : V(u_1, t_0) = \{u_1, u_2, u_3, u_4\} \quad \mathcal{G} : V(u_1, t_1) = \{u_1, u_2, u_3, u_4\} \quad \mathcal{G} : V(u_1, t_2) = \{u_1, u_2, u_3, u_4\}$$

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Formal definition of a DAPP map

Definition that integrates viability

Conditions (actions, time, states):

- Set of actions: $\mathbf{U} = \{u_1, u_2, \dots, u_i, \dots, u_m\}$,
- Time sequence: $T = \{t_0, t_1, \dots, t_j, \dots, t_n\}$,
- Set of states: $X = \{x_1, x_2, \dots, x_l\}$

A viable policy pathway (i.e. viable DAPP):

$$u_K(\cdot) = u(t_0), u(t_1), \dots, u(t_j), \dots, u(t_n) \quad \text{such that} \quad u(t_j) \in (\mathbf{U}_K(t_j) \forall j) \in \mathbf{U} \quad (33)$$

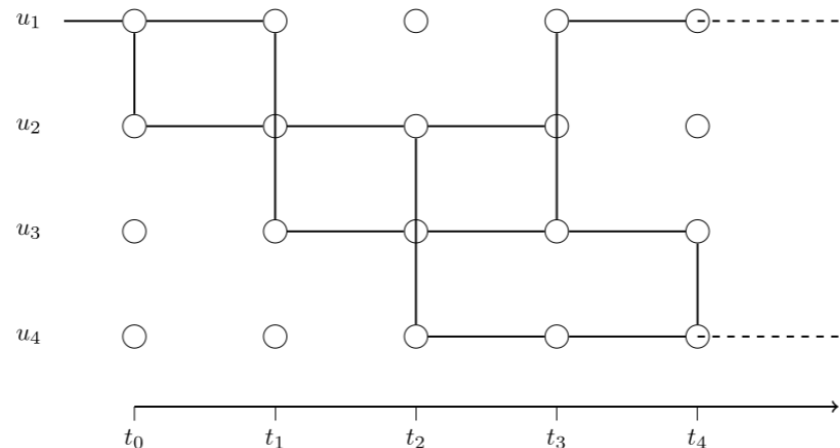
Regulatory Map (Aubin et al., 2011) [Definition 2.9.4 p.73]:

$$\mathcal{R}(x) = \{u \in U(x) \mid x \in K, f(x, u(x)) \in Viab_K\} \quad (34)$$

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 $E = \{u(t), u(t+1) \mid u(t) \in \mathcal{R}(x(t), u(t)), u(t+1) \in \mathcal{R}(x(t+1), u(t+1))\}$



$$\Gamma(u_1, t_0) = \{u_1, u_2\}$$

$$\Gamma(u_2, t_0) = \{u_1\}$$

$$\Gamma(u_3, t_0) = \emptyset$$

$$\Gamma(u_4, t_0) = \emptyset$$

$$\Gamma(u_1, t_1) = \emptyset$$

$$\Gamma(u_2, t_1) = \{u_1, u_2, u_3\}$$

$$\Gamma(u_3, t_1) = \{u_1, u_2, u_3\}$$

$$\Gamma(u_4, t_1) = \emptyset$$

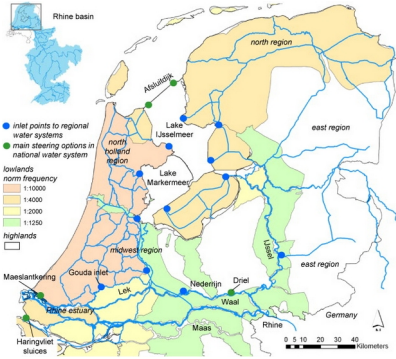
$$\Gamma(u_1, t_2) = \emptyset$$

$$\Gamma(u_2, t_2) = \{u_2, u_3, u_4\}$$

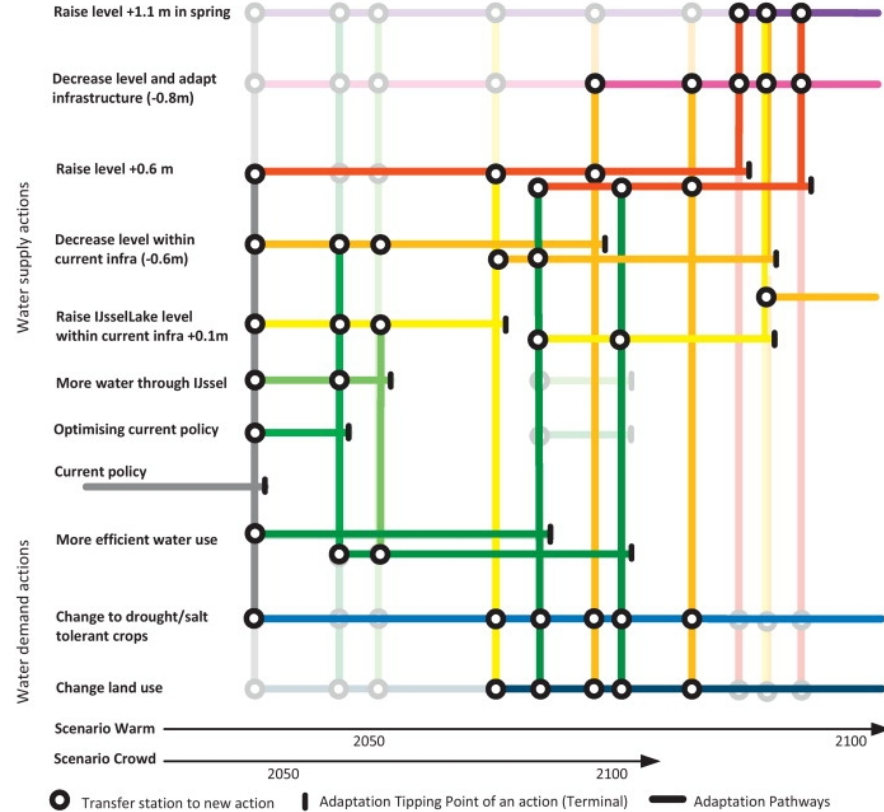
$$\Gamma(u_3, t_2) = \{u_2, u_3, u_4\}$$

$$\Gamma(u_4, t_2) = \{u_2, u_3, u_4\}$$

Adaptive policy of few infrastructures for fresh water supply vs safety



$$\dim(U) = 10$$



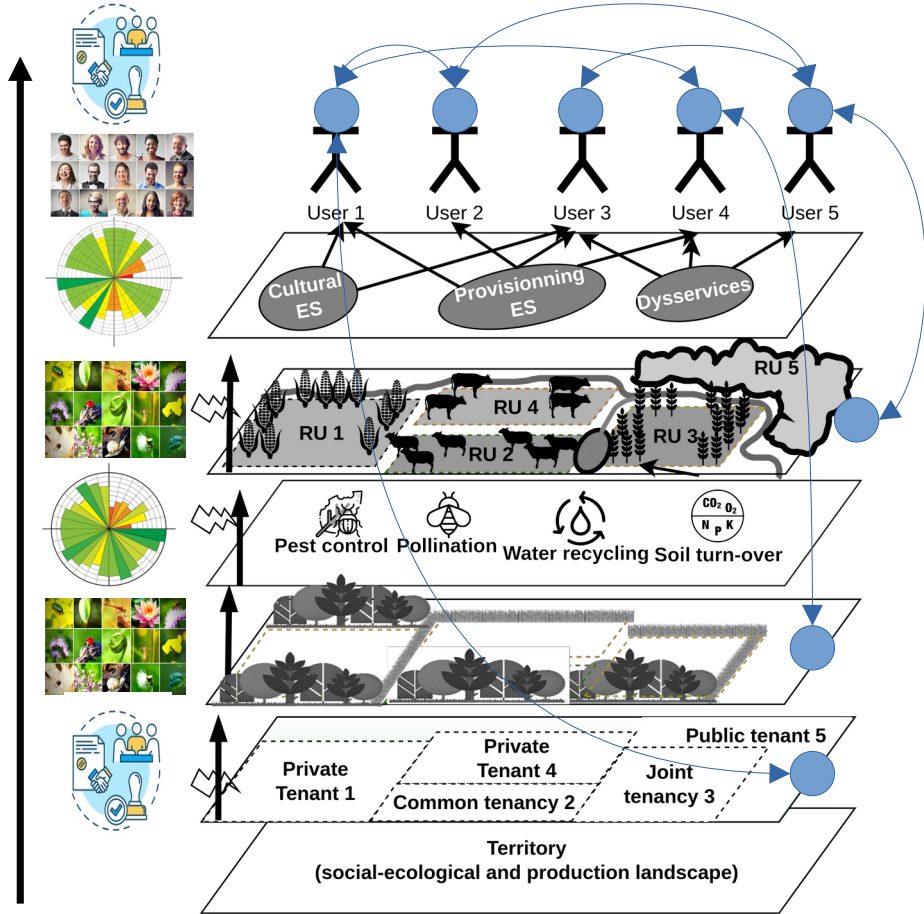
$$\dim(\mathcal{G}_K) \leq 10^{11} \text{ viable policy pathways}$$

$$\dim(T) = 11$$

Problem

How to operationalize this method for hyper diverse social-ecological systems?





Social rules (operational, collective, constitutional)?

Resource actors (exploite, use, conserve, govern)?

Final ecosystem services (Private, common, Public, Club)?

Infrastructures, e.g. field, forest, river (private, communal, public, club)?

Supporting & regulating ecosystem services (common, private, public, club)?

Hedgerow network (~private)?

Cadastral rules (private, public, common, club) ?

Territorial geography

Challenge!

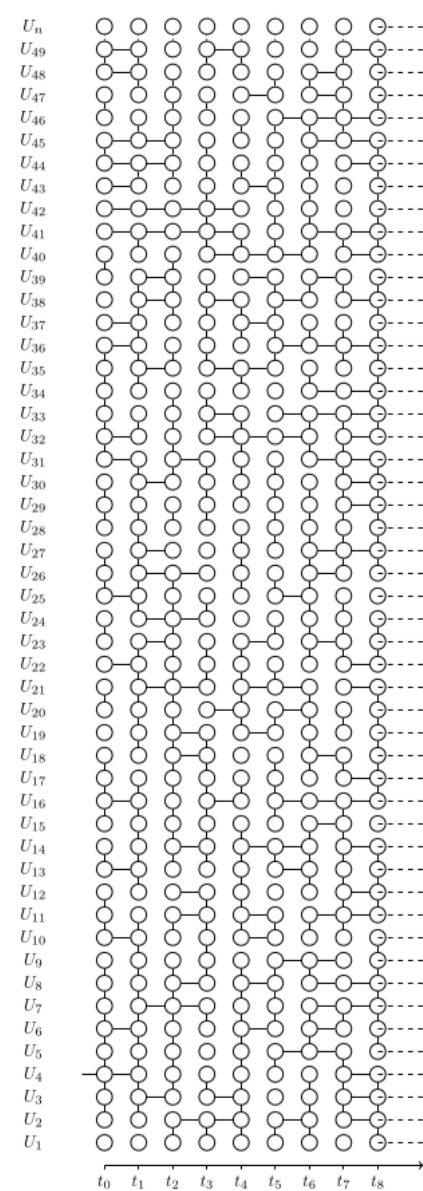
Define U , Viab_K and $\mathcal{G}(u(x), x(t))$ for these hyper-diverse SES

Modelling, structural & visual explosion

$$\dim(U) = n$$

$$\dim(\mathcal{G}_K) \leq n^m \text{ viable policy pathways}$$

Hypothetical DAPP map with n actions



Challenge!

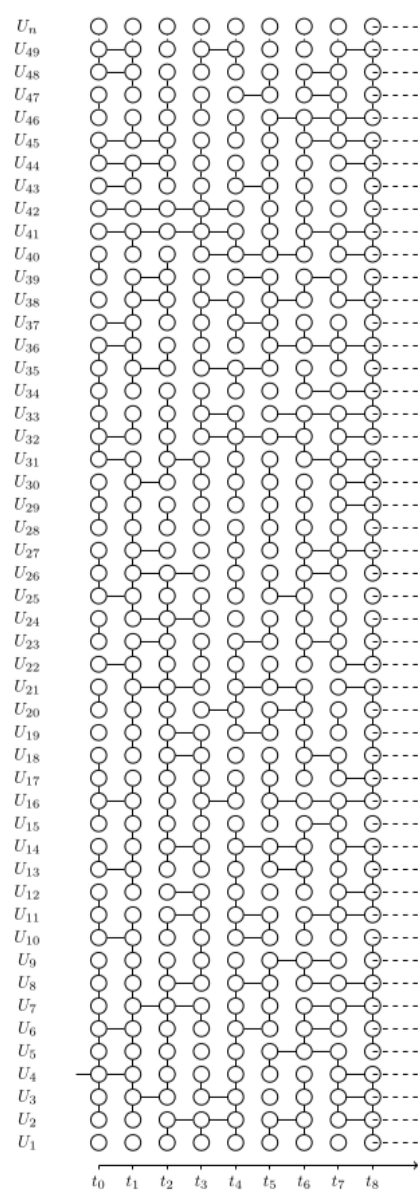
Define U , Viab_K , $\mathcal{G}(u(x), x(t))$

Modelling, structural & visual explosion

$$\dim(U) = n$$

$$\dim(\mathcal{G}_K) \leq n^m \text{ viable policy pathways}$$

Hypothetical DAPP map with n actions



We need guidelines for their design

Focus

Organizing principles

~~Algorithm to match dimensional problem
(combinatorial problem)~~

Possible guidelines

Ostrom's theory on the governance of common pool resources



Conditions (actions, time, states):

- Set of actions: $U = \{u_1, u_2, \dots, u_i, \dots, u_m\}$,
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$$u_K(\cdot) = u(t_0), u(t_1), \dots, u(t_j), \dots, u(t_n) \text{ such that } u(t_j) \in (U_K(t_j) \forall j) \in U \quad (33)$$

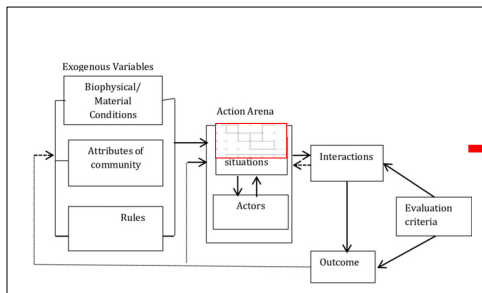
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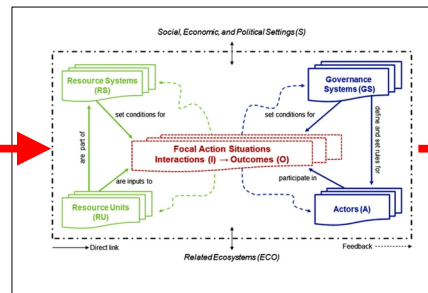
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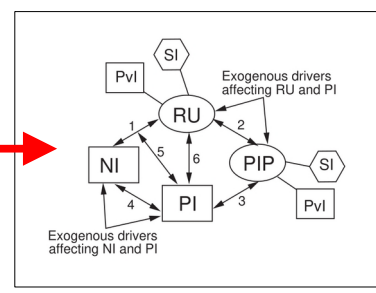
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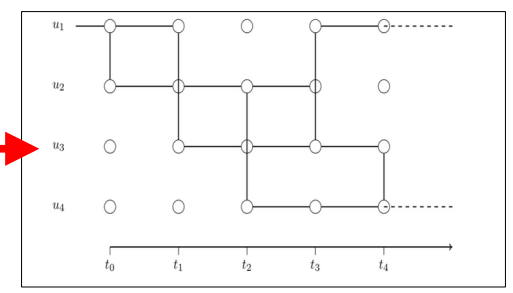
IAD framework



SES framework

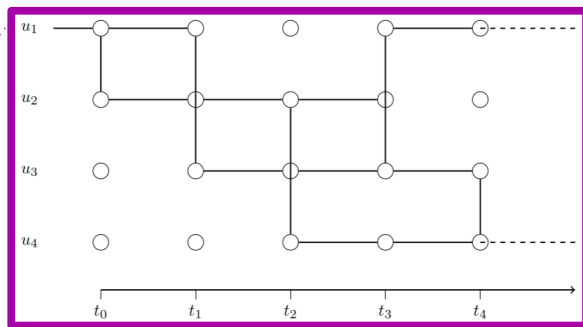


CIS framework

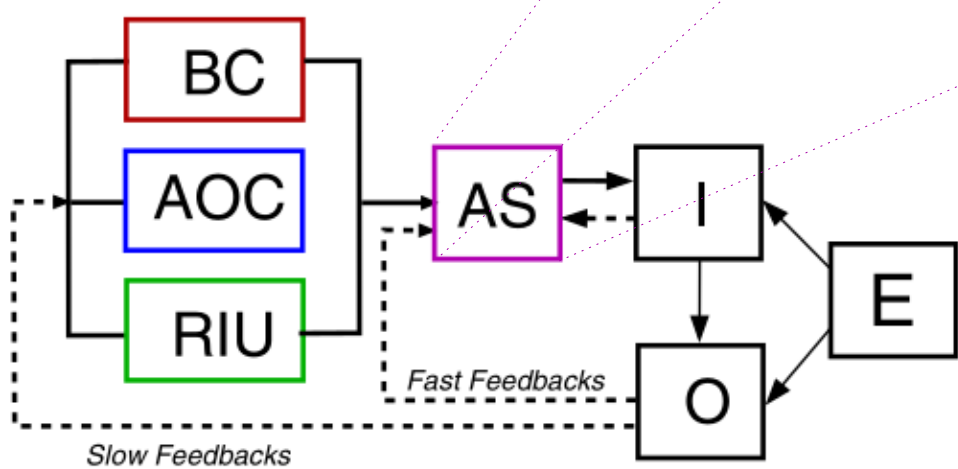


DAPP framework

IAD framework

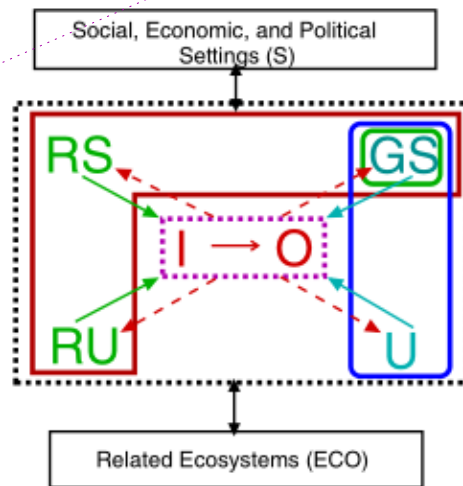


DAPP = "action situation"



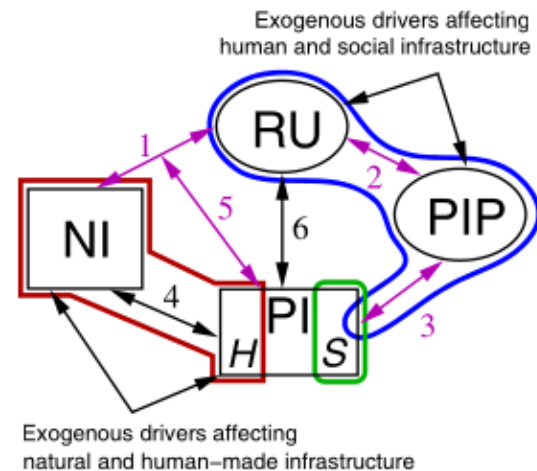
IAD Framework

a



Diagnostic/SES Framework

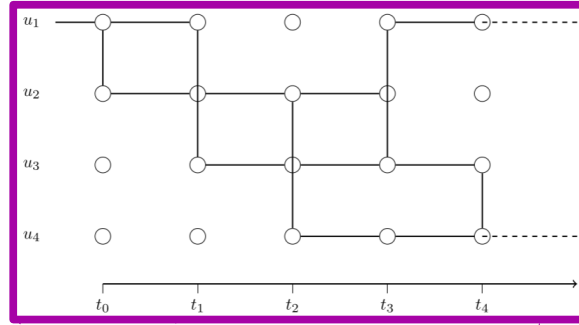
b



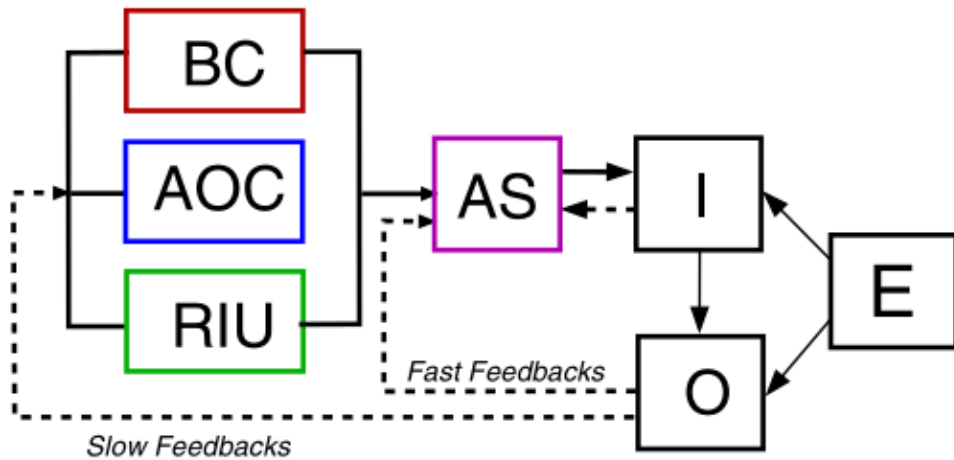
Robustness Framework

c

SES framework

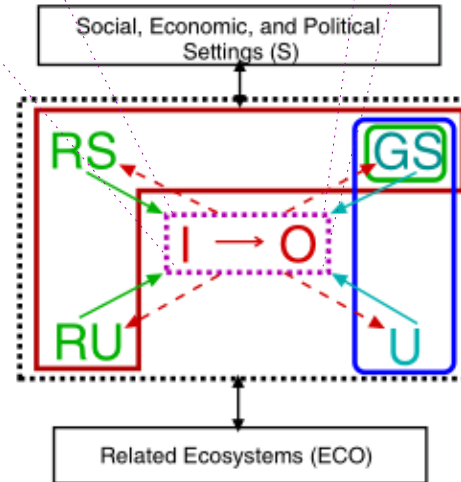


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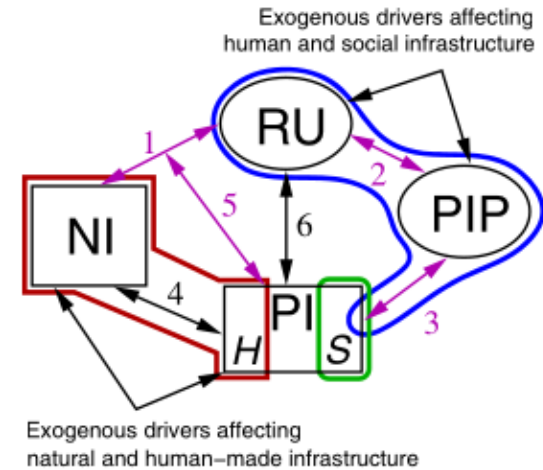
IAD Framework

a



Diagnostic/SES Framework

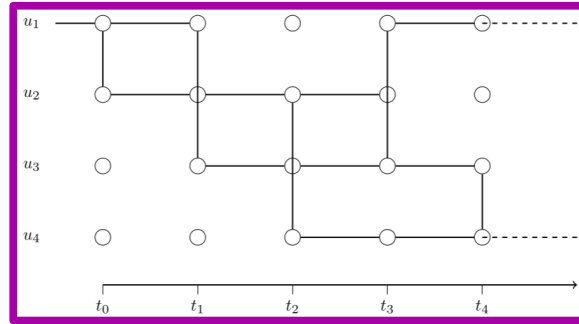
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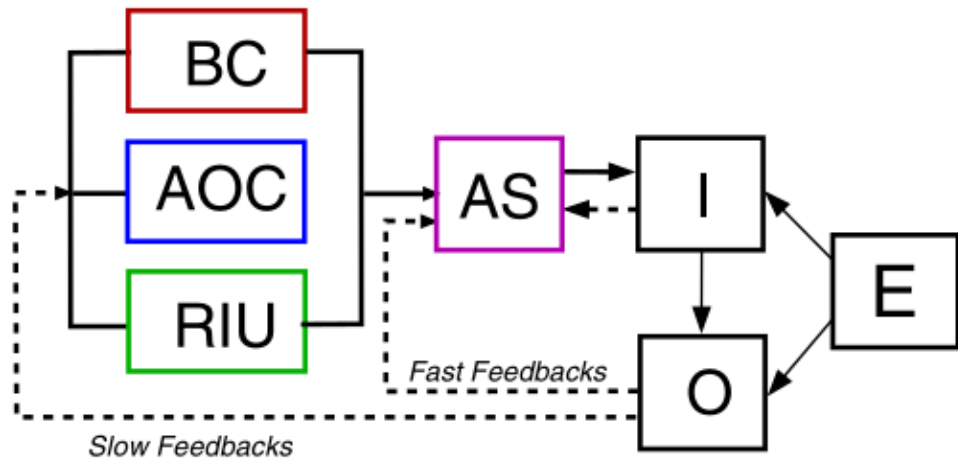
Robustness Framework

c

CIS & Robustness framework

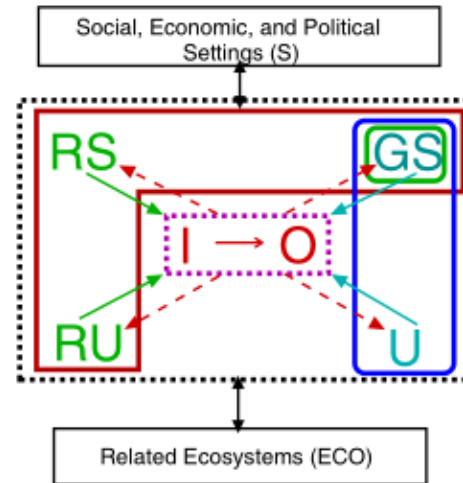


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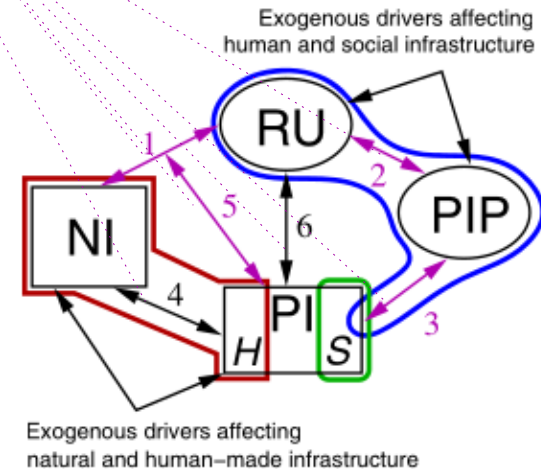
IAD Framework

a



Diagnostic/SES Framework

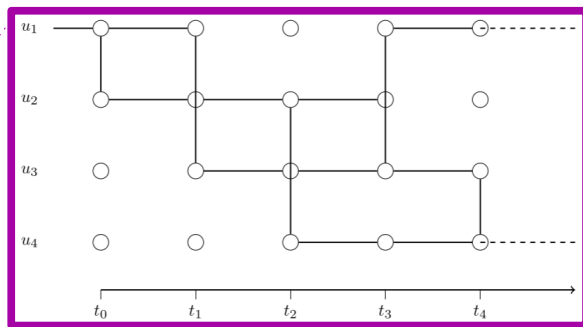
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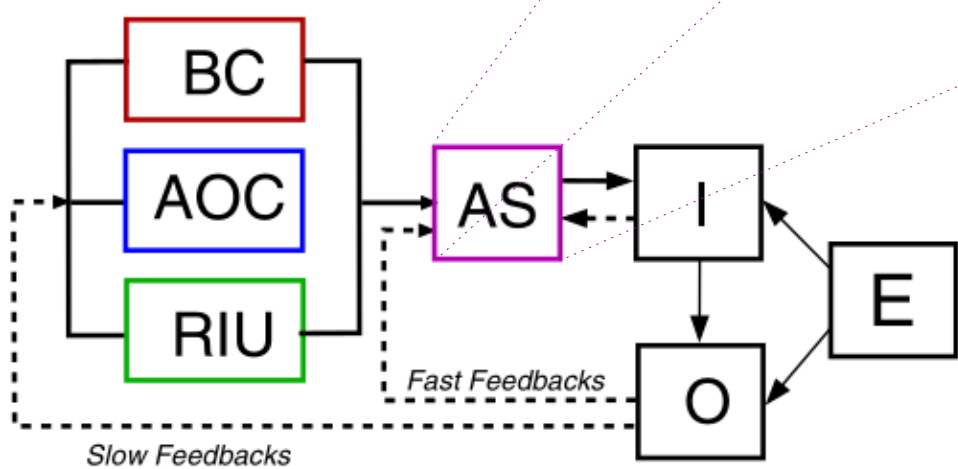
Robustness Framework

c

IAD framework

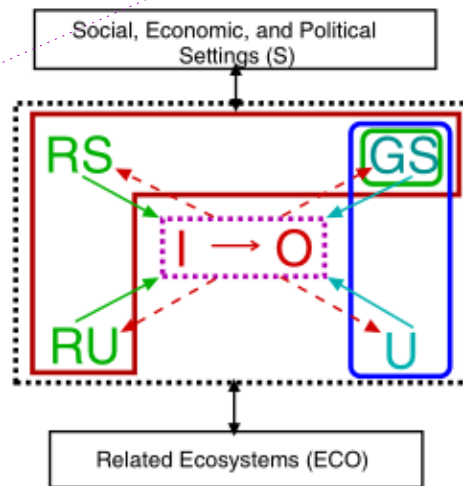


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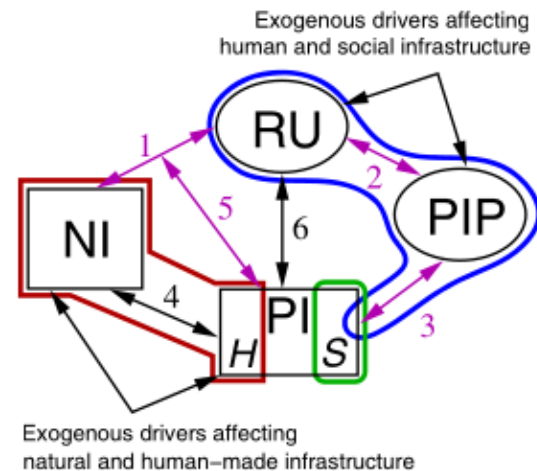
IAD Framework

a



Diagnostic/SES Framework

b

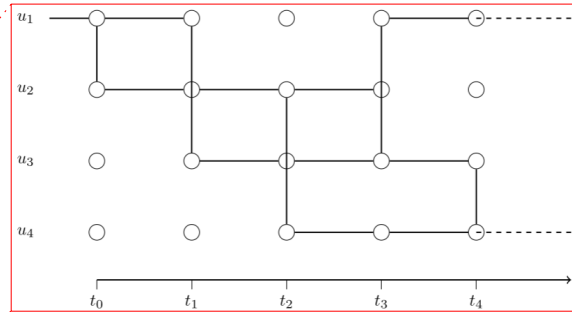
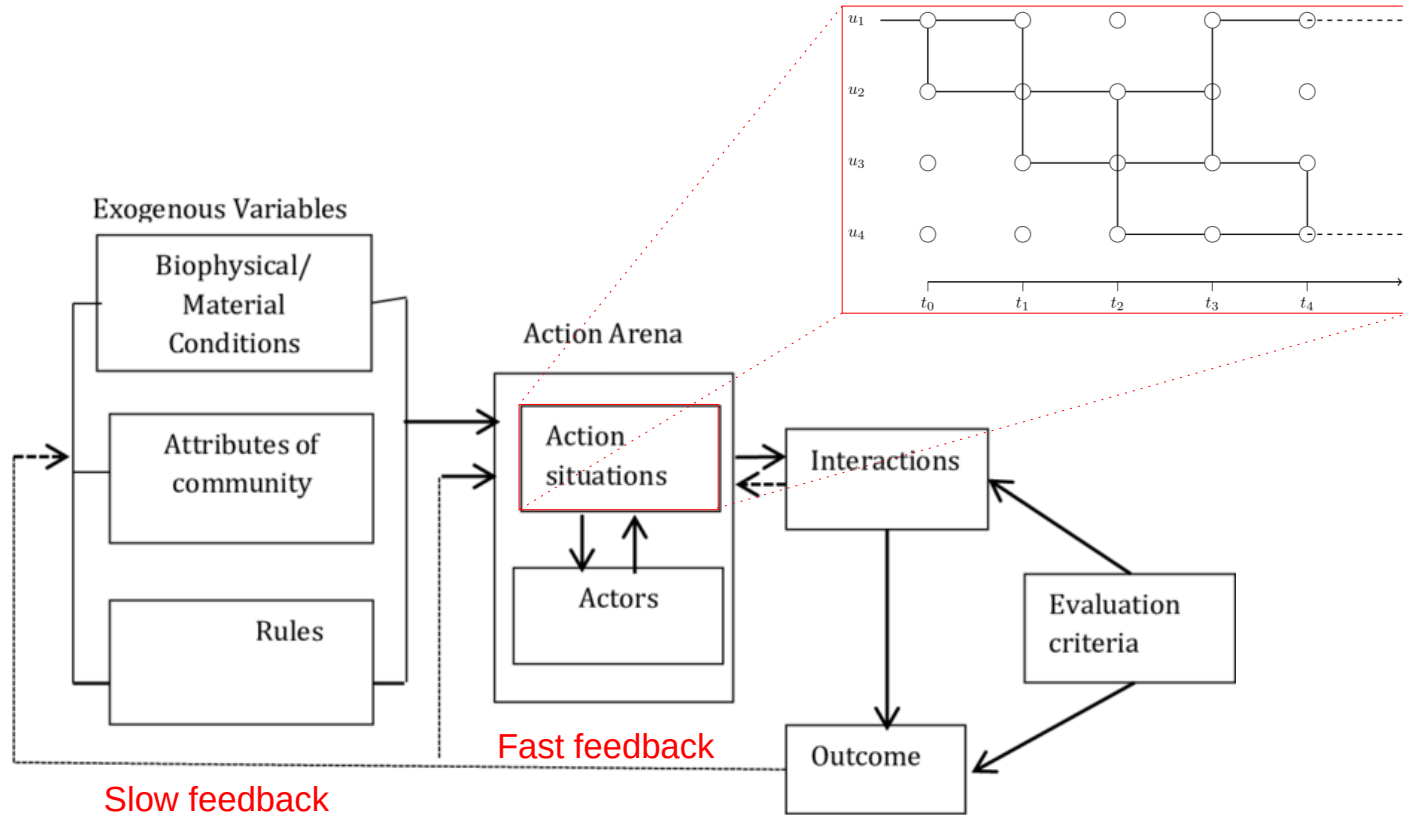


Robustness Framework

c

What are DAPP maps inside IAD framework?

DAPP = “action situation”



Conditions (actions, time, states):

- Set of actions: $U = \{u_1, u_2, \dots, u_i, \dots, u_m\}$,
- Time sequence: $T = \{t_0, t_1, \dots, t_j, \dots, t_n\}$,
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A viable policy pathway (i.e. viable DAPP):

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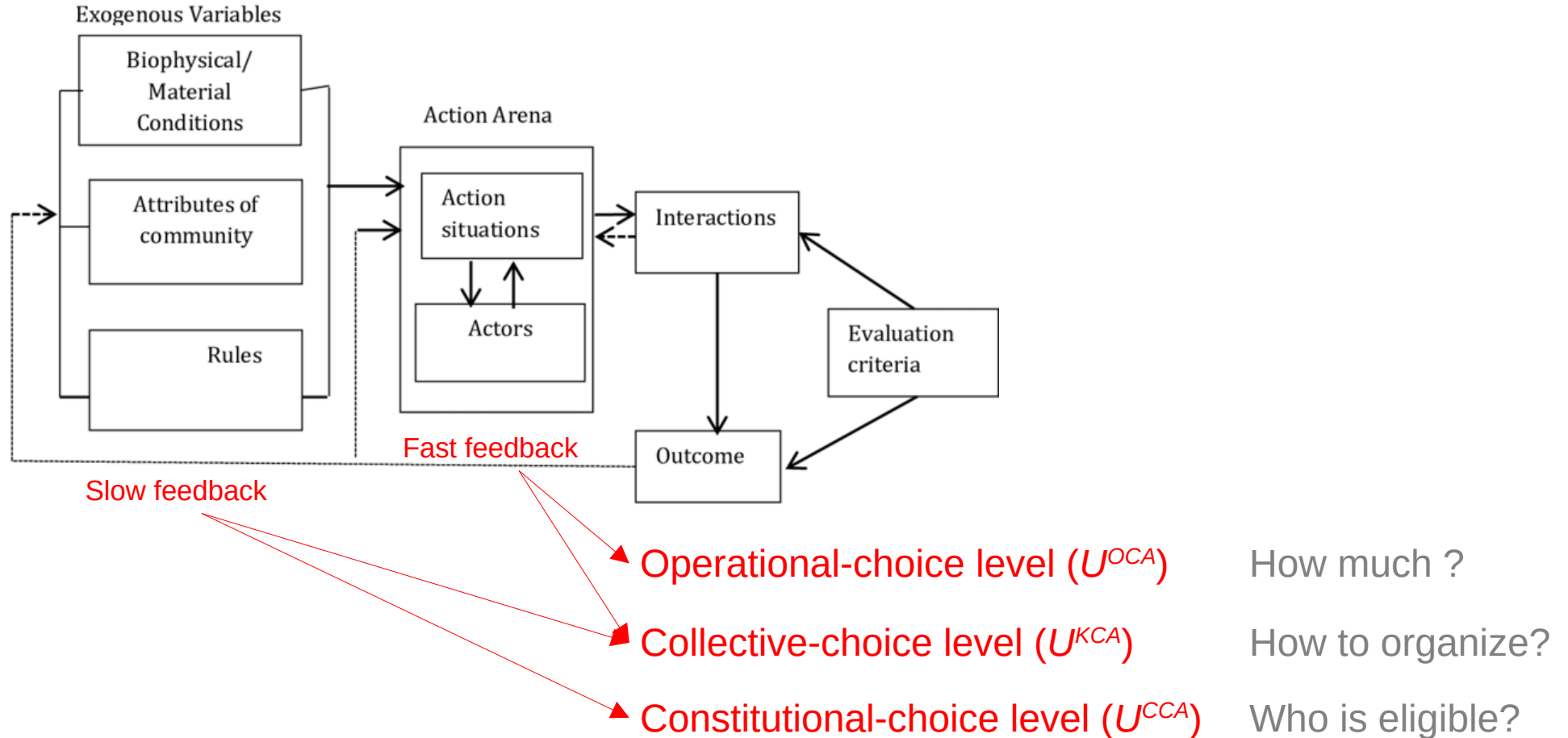
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Viable DAPP map (graph):

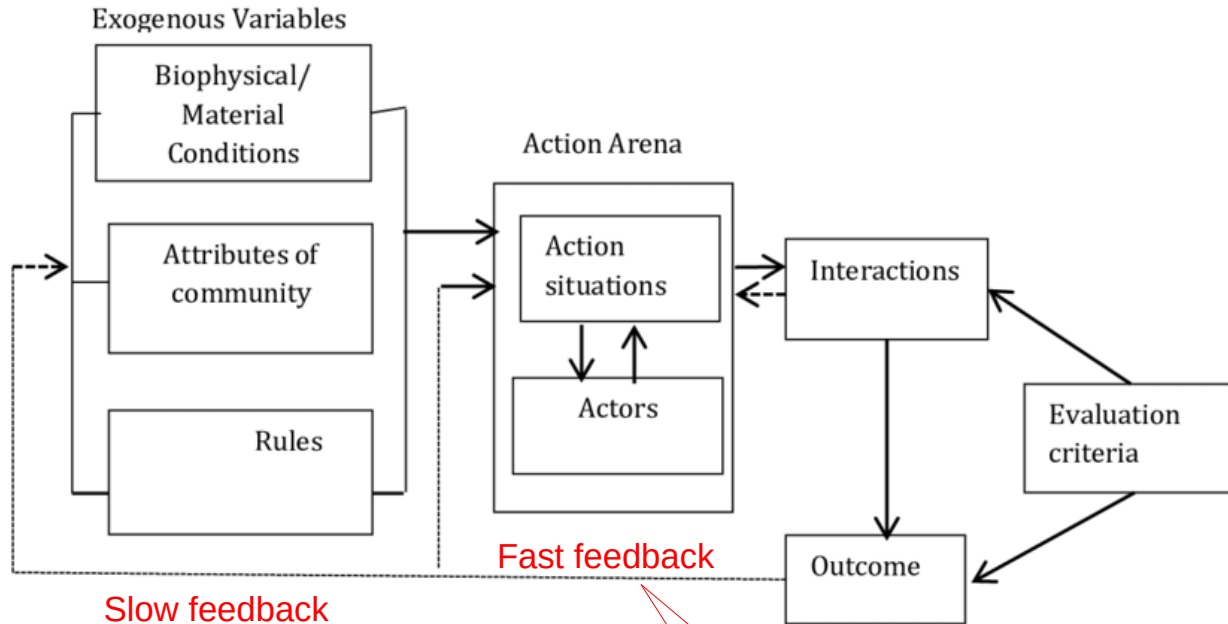
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Feedback (slow / fast) = adaptation at different levels



Nested (slow / fast) DAPP maps



Slow feedback

Fast feedback

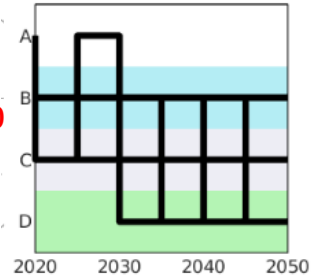
Operational (U^{OCA})

Collective (U^{KCA})

Constitutional (U^{CCA})

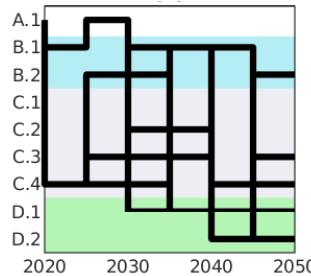
Constitutional DAPP map

Who ? What ? Eligible



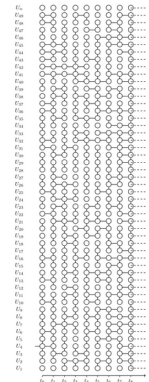
Collective DAPP map

How to organize?

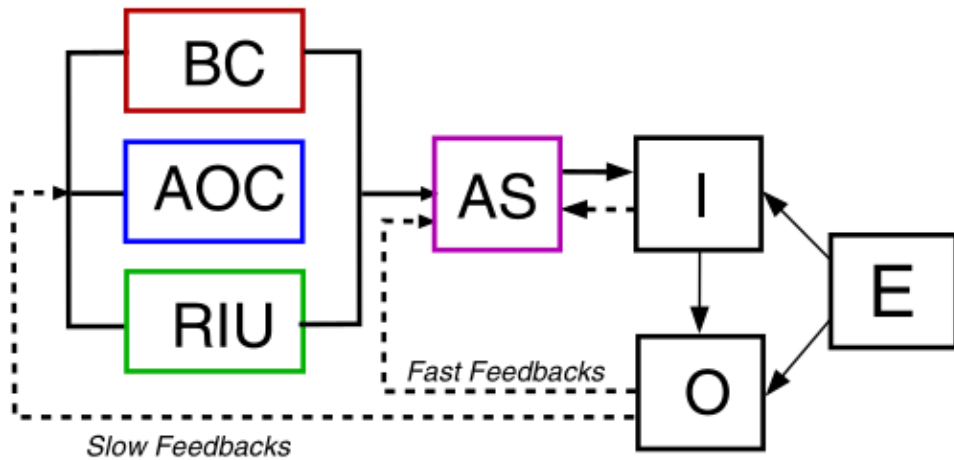
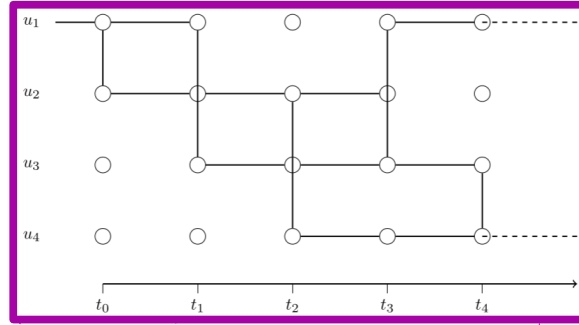


Operational DAPP map

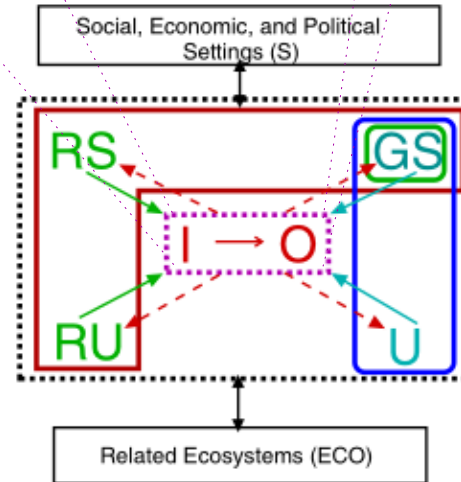
How much ?



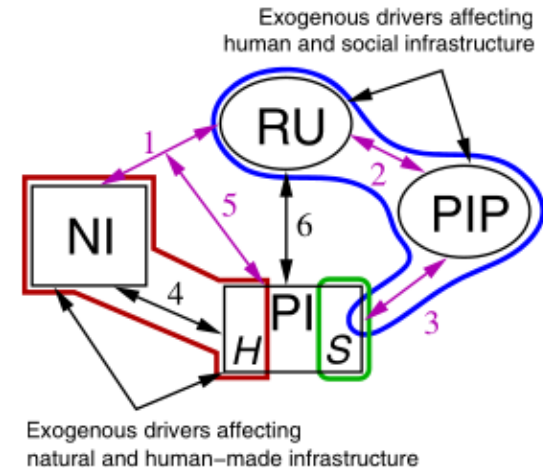
SES framework (targets of adaptation)



a



b



c

SES framework

Goal: describe SES attributes using a multi-tier framework

Version of the SES Framework used to predict the possible targets of adaptation	
Social, Economic and Political settings (S)	
S1 Economic development * †	S4 Other governance systems †
S2 Demographic trends * †	S5 Markets †
S3 Political stability (rate of political change) * †	S6 Media organizations †
	S7 Technology †
Resource Systems (RS)	Resource units (RU)
RS1 Sector	RU1 Resource unit mobility ** †
RS2 Clarity of system boundaries	RU2 Growth or replacement rate of resource units
RS3 Size of resource system	RU3 Interactions among resource units * †
RS4 Human constructed facilities *	RU4 Economic value
RS5 Productivity of the system	RU5 Number of units
RS6 Equilibrium properties	RU6 Distinctive characteristics
RS7 Predictability of system dynamics	RU7 Spatial & temporal distribution
RS8 Storage characteristics	
RS9 Location	
RS10 Ecosystem history	
Governance Systems (GS)	Actors (A)
GS1 Policy area	A1 Number of relevant actors *
GS2 Geographic scale of governance system *	A2 Socio-economic attributes *
GS3 Proportion of participating population **	A3 History of past experience **
GS4 Regime type (demo/auto-cratic, mono/poly-centric) *	A4 Location *
GS5 Rule-making organizations *	A5 Leadership / entrepreneurship *
GS6 Rules-in-Use *	A6 Norms (trust-reciprocity) / social capital *
GS7 Property rights systems (relations among people in relation to resource units and infrastructures) *	A7 Knowledge of SES / mental models / beliefs *
GS8 Repertoire of cultural knowledge, beliefs, norms, practices (strategies) with no rules and sanctions *	A8 Proportion of resource dependent actors *
GS9 Network structure (connections among the rule-making organizations and the population subject to these rules) **	A9 Technologies available *
GS10 Historical continuity of the governance system (recent vs long-lasting, open vs close to internal adaptation) *	
Interactions (I)	Outcomes (O)
I1 Harvesting / using resource units by divers users	O1 Social performance measures (e.g. efficiency, equity, accountability, sustainability) **
I2 Information sharing among actors **	O2 Ecological performance measures (e.g. overharvested, resilience, robustness, biodiversity) **
I3 Deliberation process **, **	O3 Externalities to other SES †
I4 Conflicts among actors *, **	
I5 Investment activities *, **	
I6 Lobbying activities **, ** †	
I7 Self-organizing activities *, **	
I8 Networking activities *, **	
I9 Monitoring activities *, **	
I10 Evaluative activities **, **	

SES framework

Constant improvement of the framework,
match different ways of describing SES

Version of the SES Framework used to predict the possible targets of adaptation			
Social, Economic and Political settings (S)			
S1	Economic development * †	S4	Other governance systems †
S2	Demographic trends * †	S5	Markets †
S3	Political stability (rate of political change) * †	S6	Media organizations †
		S7	Technology †
Resource Systems (RS)		Resource units (RU)	
RS1	Sector	RU1	Resource unit mobility ** †
RS2	Clarity of system boundaries	RU2	Growth or replacement rate of resource units
RS3	Size of resource system	RU3	Interactions among resource units * †
RS4	Human constructed facilities *	RU4	Economic value
RS5	Productivity of the system	RU5	Number of units
RS6	Equilibrium properties	RU6	Distinctive characteristics
RS7	Predictability of system dynamics	RU7	Spatial & temporal distribution
RS8	Storage characteristics		
RS9	Location		
RS10	Ecosystem history		
Governance Systems (GS)		Actors (A)	
GS1	Policy area	A1	Number of relevant actors *
GS2	Geographic scale of governance system *	A2	Socio-economic attributes *
GS3	Proportion of participating population **	A3	History of past experience ***
GS4	Regime type (demo/auto-cratic, mono/poly-centric) *	A4	Location *
GS5	Rule-making organizations *	A5	Leadership / entrepreneurship *
GS6	Rules-in-Use *	A6	Norms (trust-reciprocity) / social capital *
GS7	Property rights systems (relations among people in relation to resource units and infrastructures) *	A7	Knowledge of SES / mental models / beliefs *
GS8	Repertoire of cultural knowledge, beliefs, norms, practices (strategies) with no rules and sanctions *	A8	Proportion of resource dependent actors *
GS9	Network structure (connections among the rule-making organizations and the population subject to these rules) ***	A9	Technologies available *
GS10	Historical continuity of the governance system (recent vs long-lasting, open vs close to internal adaptation) *		
Interactions (I)		Outcomes (O)	
I1	Harvesting / using resource units by divers users	O1	Social performance measures (e.g. efficiency, equity, accountability, sustainability) **
I2	Information sharing among actors **, **	O2	Ecological performance measures (e.g. overharvested, resilience, robustness, biodiversity) **
I3	Deliberation process **, **	O3	Externalities to other SES †
I4	Conflicts among actors **, **		
I5	Investment activities **, **		
I6	Lobbying activities **, ** †		
I7	Self-organizing activities **, **		
I8	Networking activities **, **		
I9	Monitoring activities **, **		
I10	Evaluative activities **, **		

Ostrom, E. (2007). A diagnostic approach for going beyond panaceas. Proceedings of the National Academy of Sciences of the United States of America, 104(39), 15181-15187.

Iteration 1

Ostrom, E. (2009). A general framework for analyzing sustainability of social-ecological systems. Science, 325, 419-422

Iteration 2

McGinnis, M. D., and **Ostrom, E. (2014).** Social-ecological system framework: initial changes and continuing challenges. Ecology and Society, 19

Iteration 3

Vogt, J., Epstein, G., Mincey, S.K., Fischer, B.C., and McCord, P.F. (2015). Putting the "E" in SES: unpacking the ecology in the Ostrom social-ecological system framework. Ecology and Society, 20.

Iteration 4

Filtre 1 : SES framework

Define adaptation actions according to targeted SES attributes

SES framework

Version of the SES Framework used to predict the possible targets of adaptation	
Social, Economic and Political settings (S)	
S1 Economic development ** †	S4 Other governance systems †
S2 Demographic trends * †	S5 Markets †
S3 Political stability (rate of political change) * †	S6 Media organizations †
	S7 Technology †
Resource Systems (RS)	
RS1 Sector	Resource units (RU)
RS2 Clarity of system boundaries	RU1 Resource unit mobility ** †
RS3 Size of resource system	RU2 Growth or replacement rate of resource units
RS4 Human constructed facilities *	RU3 Interactions among resource units * †
RS5 Productivity of the system	RU4 Economic value
RS6 Equilibrium properties	RU5 Number of units
RS7 Predictability of system dynamics	RU6 Distinctive characteristics
RS8 Storage characteristics	RU7 Spatial & temporal distribution
RS9 Location	
RS10 Ecosystem history	
Governance Systems (GS)	
GS1 Policy area	Actors (A)
GS2 Geographic scale of governance system *	A1 Number of relevant actors *
GS3 Proportion of participating population **	A2 Socio-economic attributes *
GS4 Regime type (demo/auto-crat, mono/poly-centric) *	A3 History of past experience **
GS5 Rule-making organizations *	A4 Location *
GS6 Rules-in-Use *	A5 Leadership / entrepreneurship *
GS7 Property rights systems (relations among people in relation to resource units and infrastructures) *	A6 Norms (trust-reciprocity) / social capital *
GS8 Repertoire of cultural knowledge, beliefs, norms, practices (strategies) with no rules and sanctions *	A7 Knowledge of SES / mental models / beliefs *
GS9 Network structure (connections among the rule-making organizations and the population subject to these rules) **	A8 Proportion of resource dependent actors *
GS10 Historical continuity of the governance system (recent vs long-lasting, open vs close to internal adaptation) *	A9 Technologies available *
Interactions (I)	
I1 Harvesting / using resource units by divers users	Outcomes (O)
I2 Information sharing among actors * **	O1 Social performance measures (e.g. efficiency, equity, accountability, sustainability) **
I3 Deliberation process * **	O2 Ecological performance measures (e.g. overharvested, resilience, robustness, biodiversity) **
I4 Conflicts among actors * **	O3 Externalities to other SES †
I5 Investment activities * **	
I6 Lobbying activities * ** †	
I7 Self-organizing activities * **	
I8 Networking activities * **	
I9 Monitoring activities * **	
I10 Evaluative activities * **	

$$U = \{u_1, u_2, u_3, \dots, u_n\}$$

Attributs : Tier 1

$$U = \{U_S, U_{RS}, U_{RU}, U_{GS}, U_A, U_I, U_O\}$$

Tier 2

$$U_S = \{u_{S1}, u_{S2}, \dots, u_{S7}\}$$

$$U_{RS} = \{u_{RS1}, u_{RS2}, \dots, u_{RS10}\}$$

$$U_{RU} = \{u_{RU1}, u_{RU2}, \dots, u_{RS7}\}$$

$$U_{GS} = \{u_{GS1}, u_{GS2}, \dots, u_{GS10}\}$$

$$U_A = \{u_{A1}, u_{A2}, \dots, u_{A9}\}$$

$$U_I = \{u_{I1}, u_{I2}, \dots, u_{I10}\}$$

$$U_O = \{u_{O1}, u_{O2}, u_{O3}\}$$

Tier 3

...

Construction the set U of 2nd tier actions based on a version of Ostrom's social-ecological system framework (SESF)

Set of actions related to the social, economic & political Settings (U_s)

- U_{S1} Economic development * †
- U_{S2} Demographic trends * †
- U_{S3} Political stability (rate of political change) * †

- U_{S4} Other governance systems †
- U_{S5} Markets †
- U_{S6} Media organizations †
- U_{S7} Technology †

Set of actions related to the Resource Systems (U_{RS})

- U_{RS1} Sector
- U_{RS2} Clarity of system boundaries
- U_{RS3} Size of resource system
- U_{RS4} Human constructed facilities *
- U_{RS5} Productivity of the system
- U_{RS6} Equilibrium properties
- U_{RS7} Predictability of system dynamics
- U_{RS8} Storage characteristics
- U_{RS9} Location
- U_{RS10} Ecosystem history

Set of actions related to the Resource Units (U_{RU})

- U_{RU1} Resource unit mobility ** †
- U_{RU2} Growth or replacement rate of resource units
- U_{RU3} Interactions among resource units * †
- U_{RU4} Economic value
- U_{RU5} Number of units
- U_{RU6} Distinctive characteristics
- U_{RU7} Spatial & temporal distribution

Set of actions related to the Governance Systems (U_{GS})

- U_{GS1} Policy area
- U_{GS2} Geographic scale of governance system *
- U_{GS3} Proportion of participating population **
- U_{GS4} Regime type (demo/auto-cratic, mono/poly-centric) *
- U_{GS5} Rule-making organizations *
- U_{GS6} Rules-in-Use *
- U_{GS7} Property rights systems (relations among people in relation to resource units and infrastructures) *
- U_{GS8} Repertoire of cultural knowledge, beliefs, norms, practices (strategies) with no rules and sanctions *
- U_{GS9} Network structure (connections among the rule-making organizations and the population subject to these rules) * **
- U_{GS10} Historical continuity of the governance system (recent vs long-lasting, open vs close to internal adaptation) *

Set of actions related to the Actors (U_A)

- U_{A1} Number of relevant actors *
- U_{A2} Socio-economic attributes *
- U_{A3} History of past experience **
- U_{A4} Location *
- U_{A5} Leadership / entrepreneurship *
- U_{A6} Norms /(trust-reciprocity) / social capital *
- U_{A7} Knowledge of SES / mental models / beliefs *
- U_{A8} Proportion of resource dependent actors *
- U_{A9} Technologies available *

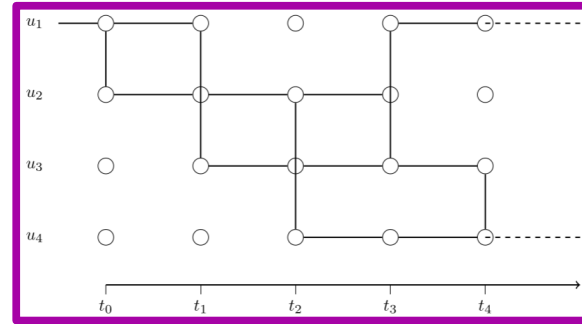
Set of actions related to the Interactions (U_i)

- U_{I1} Harvesting / using resource units by divers users
- U_{I2} Information sharing among actors * **
- U_{I3} Deliberation process * **
- U_{I4} Conflicts among actors * **
- U_{I5} Investment activities * **
- U_{I6} Lobbying activities * ** †
- U_{I7} Self-organizing activities * **
- U_{I8} Networking activities * **
- U_{I9} Monitoring activities * **
- U_{I10} Evaluative activities * **

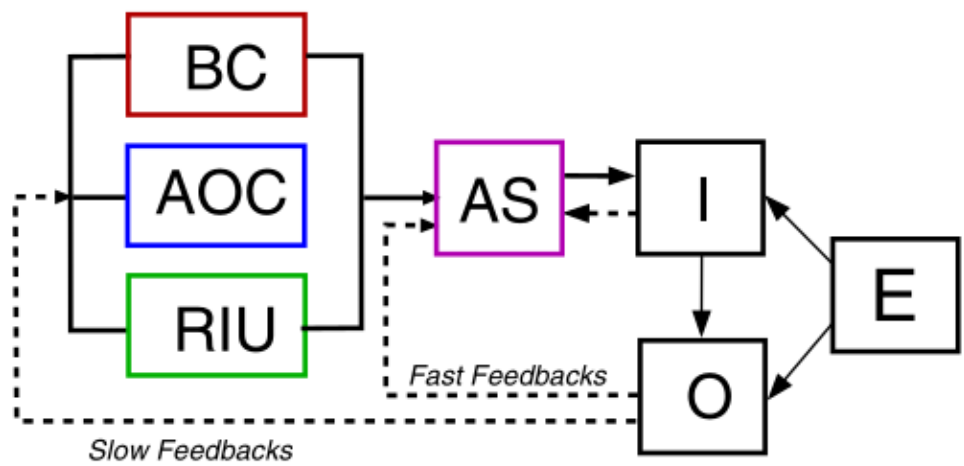
Set of actions related to the Outcomes (U_o)

- U_{O1} Social performance measures (e.g. efficiency, equity, accountability, sustainability) * **
- U_{O2} Ecological performance measures (e.g. overharvested, resilience, robustness, biodiversity) **
- U_{O3} Externalities to other SES †

CIS & Robustness framework (triggering of actions)

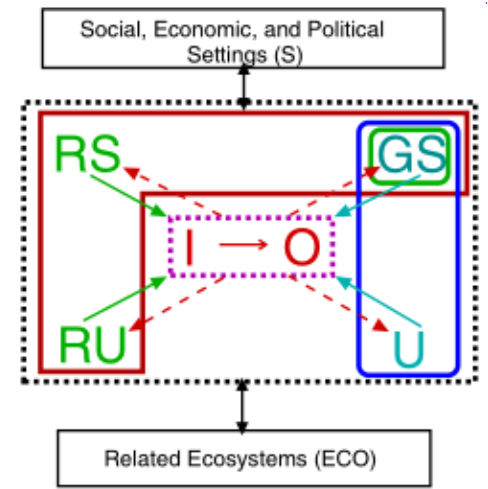


DAPP = "action situation"



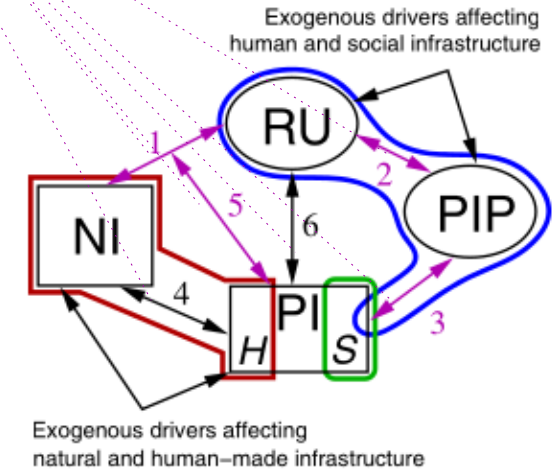
IAD Framework

a



Diagnostic/SES Framework

b



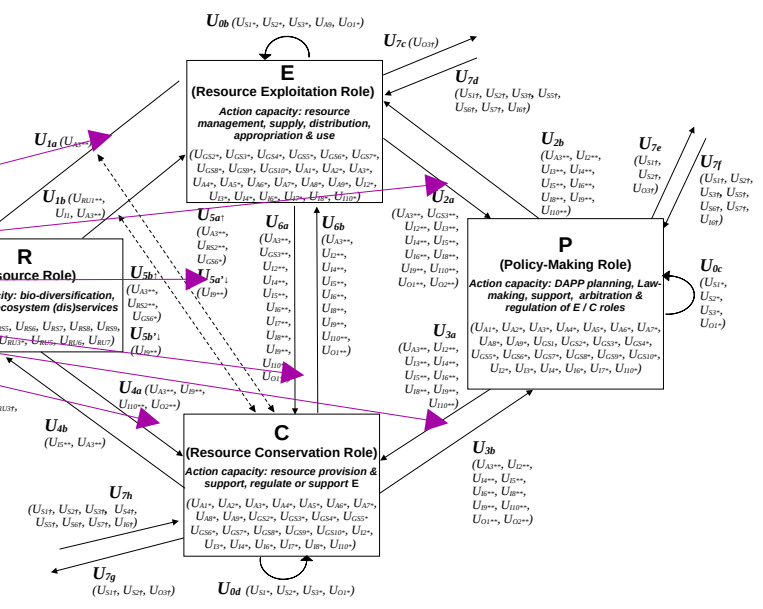
Robustness Framework

c

SES + CIS

targets of action → Roles that trigger & receive actions

Version of the SES Framework used to predict the possible targets of adaptation			
Social, Economic and Political settings (S)			
S1 Economic development * 1	S4 Other governance systems †	S7 Technology †	
S2 Demographic trends * 1	S5 Markets †		
S3 Political stability (risk of political change) * 1	S6 Media organizations †		
Resource Systems (R)			
R11 Sector	R12 Resource unit stability ** 1	R15 Interactions among resource units * 1	
R12 Clarity of system boundaries	R13 Growth of replacement rate of resource units	R16 Economic value	
R13 Size of resource system	R14 Interactions among resource units * 1	R17 Number of units	
R14 Infrastructure/constraints/facilities *	R15 Economic value	R18 Observed characteristics	
R15 Probability of the system	R16 Number of units	R19 Spatial & temporal distribution	
R16 Equilibrium response	R17 Observed characteristics		
R17 Predictability of system dynamics	R18 Observed characteristics		
R18 Storage characteristics	R19 Spatial & temporal distribution		
R19 Location			
R20 Ecosystem history			
Actors (A)			
A1 Policy area	A2 Number of relevant actors *	A3 Socioeconomic attributes *	
A2 Geographic scale of governance system *	A3 History of past experience **	A4 Location *	
A3 Propriety of participating population **	A4 Leadership / empowerment *	A5 Norms (social reciprocity) / social capital *	
A4 Response type (bureaucratic, monopoly-centric) *	A5 Knowledge of SES: mental models / heuristics *	A6 Proportion of resource dependent actors *	
A5 Team-working / organizations *	A6 Knowledge of SES: mental models / heuristics *	A7 Technologies available *	
A6 Property rights systems (relations among people in relation to resource units and infrastructure) *	A7 Proportion of resource dependent actors *		
A7 Dependence of cultural knowledge, beliefs, norms, practices (co-evolved) with rules and sanctions *	A8 Proportion of resource dependent actors *		
A8 Related resource distributions among the interacting organizations and the resource subject to these rules **	A9 Technologies available *		
A9 Historical continuity of the governance system (recent vs long-lasting open vs close to internal adaptation) *			
Outcomes (O)			
O1 Worsening among resource units by stressors	O2 Ecological performance measures (e.g. efficiency, equity, accountability, sustainability) **	O3 Exposed/less to other SES †	
O2 Information sharing among actors **			
O3 Collaboration among actors **			
O4 Conflicts among actors **			
O5 Investment activities **			
O6 Learning activities **			
O7 Self-organizing activities **			
O8 Networking activities **			
O9 Monitoring activities **			
O10 Evaluative activities **			



$$U = \{U_S, U_{RS}, U_{RU}, U_{GS}, U_A, U_I, U_O\}$$

Filtre 2 : CIS framework

Spread adaptation action by roles' actors & infrastructures

Principle 8-A: Polycentricity

Tier 1

$$U = \{U_S, U_{RS}, U_{RU}, U_{GS}, U_A, U_I, U_O\}$$

Tier 2

$$U_S = \{U_{S1}, U_{S2}, \dots, U_{S7}\}$$

$$U_{RS} = \{U_{RS1}, U_{RS2}, \dots, U_{RS10}\}$$

$$U_{RU} = \{U_{RU1}, U_{RU2}, \dots, U_{RS7}\}$$

$$U_{GS} = \{U_{GS1}, U_{GS2}, \dots, U_{GS10}\}$$

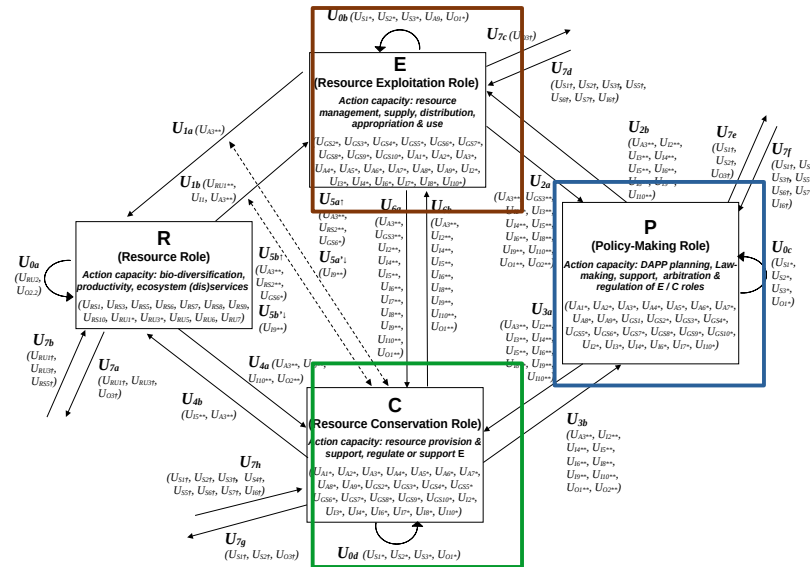
$$U_A = \{U_{A1}, U_{A2}, \dots, U_{A9}\}$$

$$U_I = \{U_{I1}, U_{I2}, \dots, U_{I10}\}$$

$$U_O = \{U_{O1}, U_{O2}, U_{O3}\}$$

Tier 3

...



Exploitation (E)

$$U_E = \{U_{E:S}, U_{E:RS}, U_{E:RU}, U_{E:GS}, U_{E:A}, U_{E:I}, U_{E:O}\}$$

$$U^E = \{U_{E:0b}, U_{E:1a}, U_{E:1b}, U_{E:2a}, U_{E:6a}, U_{E:7c}, U_{E:7d}\}$$

Arbitration (P)

$$U_P = \{U_{P:S}, U_{P:RS}, U_{P:RU}, U_{P:GS}, U_{P:A}, U_{P:I}, U_{P:O}\}$$

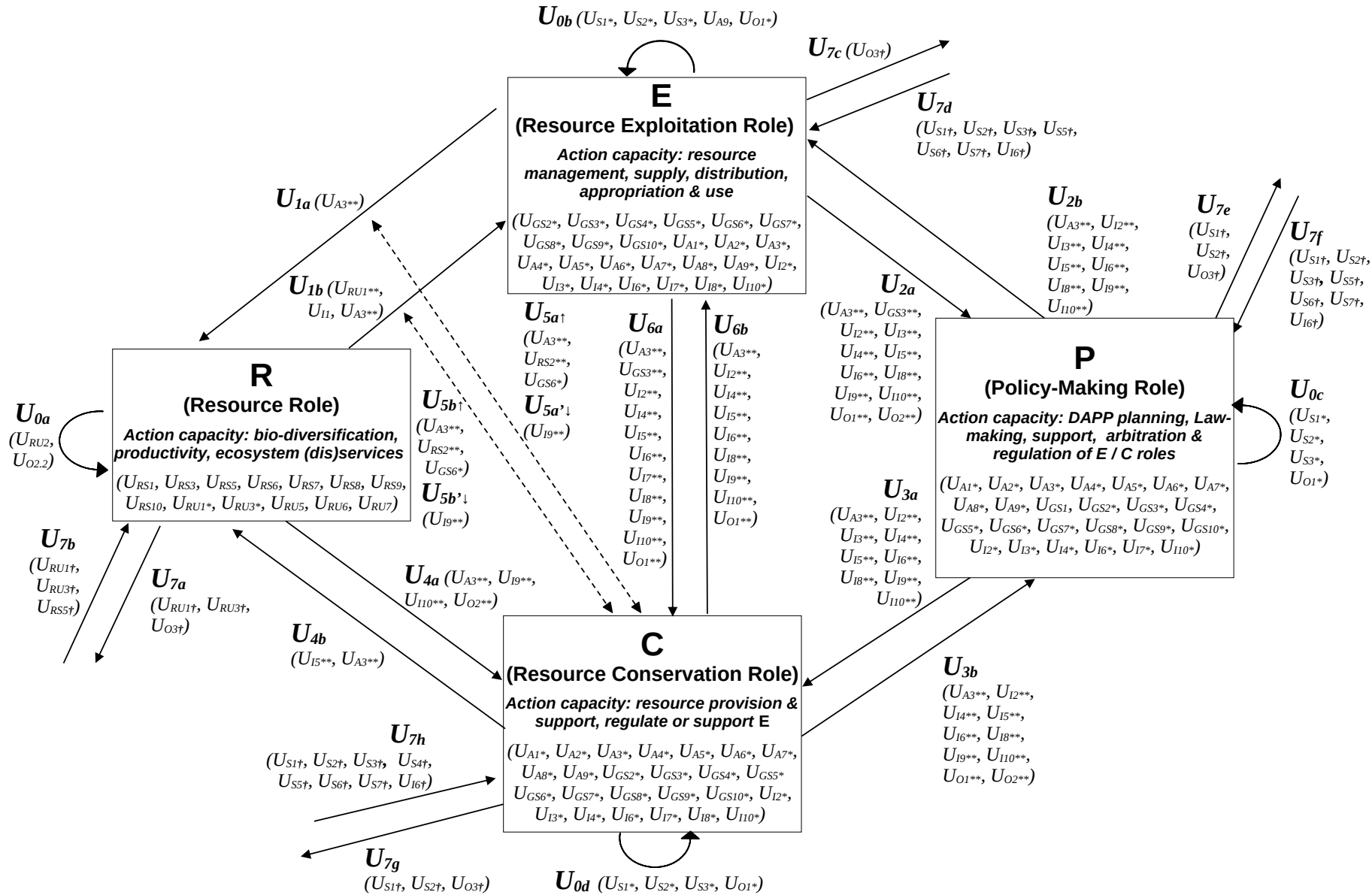
$$U_P = \{U_{P:0c}, U_{P:2b}, U_{P:3a}, U_{P:7e}, U_{P:7f}\}$$

Conservation (C)

$$U_C = \{U_{C:S}, U_{C:RS}, U_{C:RU}, U_{C:GS}, U_{C:A}, U_{C:I}, U_{C:O}\}$$

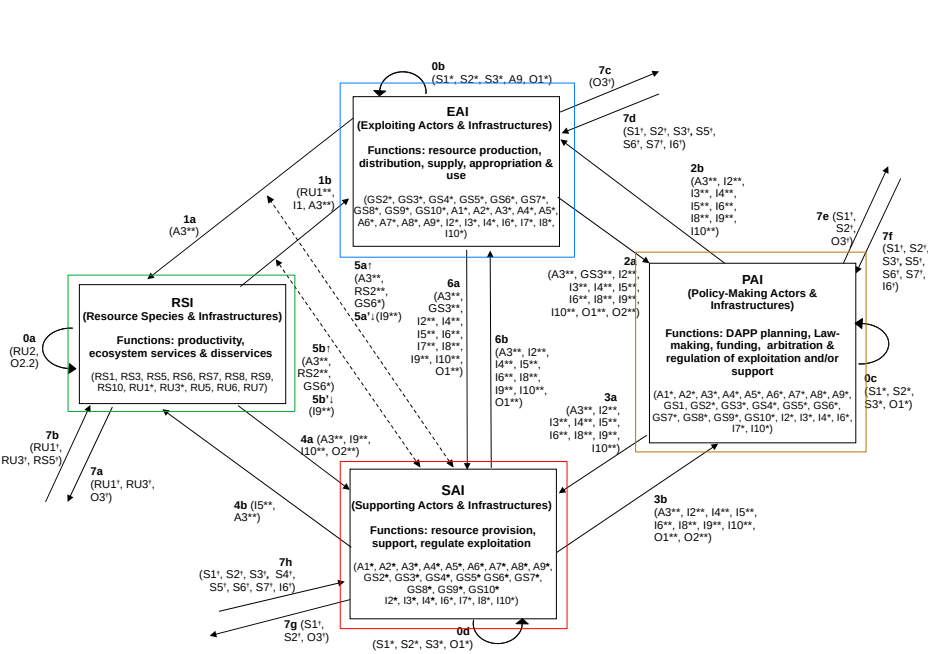
$$U_C = \{U_{C:0d}, U_{C:4a}, U_{C:4b}, U_{C:5a}, U_{C:5b}, U_{C:6b}, U_{C:7g}, U_{C:7h}\}$$

Anderies, J. M., Janssen, M. A., and Ostrom, E. (2004). A framework to analyze the robustness of social-ecological systems from an institutional perspective. *Ecology and society*, 9(1).



Transform the CIS into a system of equations

Consequences of adaptation actions on SES dynamics & viability



$$\begin{aligned}
 \frac{dR}{dt} &= \underbrace{U_{0a}.R}_{\text{Natural ES Growth}} \pm \underbrace{U_{7b}.R}_{\text{Impact of SES Settings}} - \underbrace{U_{7a}.R}_{\text{ES Externalities}} \\
 &+ \underbrace{U_{4a}.R.C}_{\text{R Support by C}} - \underbrace{U_{1b}.R.E}_{\text{ES Access \& Flow}} \cdot \underbrace{U_{5b}.C}_{\text{Regulation}} + \underbrace{U_{1a}.E.R}_{\text{Access \& Management}} \cdot \underbrace{U_{5a}.C}_{\text{Regulation}} \\
 \frac{dE}{dt} &= \pm \underbrace{U_{0b}.E}_{\text{Natural Growth/Decay}} \pm \underbrace{7d.E}_{\text{Impact of SES Settings}} - \underbrace{U_{7c}.E}_{\text{Externalities}} \\
 &+ \underbrace{U_{1b}.R.E}_{\text{Access R \& ES Flow}} \cdot \underbrace{U_{5b}.C}_{\text{Regulation}} \pm \underbrace{U_{6b'}.E.C}_{\text{C Support \& Regulation}} \pm \underbrace{U_{2b}.E.P}_{\text{P Support \& Sanctions}} \\
 \frac{dC}{dt} &= \pm \underbrace{U_{0d}.C}_{\text{Natural Growth/Decay}} \pm \underbrace{U_{7h}.C}_{\text{Impact of SES Settings}} - \underbrace{U_{7g}.C}_{\text{Externalities}} \\
 &+ \underbrace{U_{1b}.R.E}_{\text{Access \& ES Flow}} \cdot \underbrace{U_{5b'}.C}_{\text{Monitoring}} + \underbrace{U_{1a}.R.E}_{\text{Access \& Management}} \cdot \underbrace{U_{5a'}.C}_{\text{Monitoring}} \\
 &+ \underbrace{(U_{6a} - U_{6b}).E.C}_{\text{E Joining/leaving}} \pm \underbrace{U_{3a}.P.C}_{\text{P Support/Sanction}} \\
 \frac{dP}{dt} &= \pm \underbrace{U_{0c}.P}_{\text{Natural Growth/Decay}} \pm \underbrace{U_{7f}.C}_{\text{Impact of SES Settings}} - \underbrace{U_{7e}.C}_{\text{Externalities}} \\
 &\pm \underbrace{U_{2a}.E.P}_{\text{Join/Support/Sanction}} \pm \underbrace{U_{3b}.C.P}_{\text{Join/Support/Sanction}}
 \end{aligned}
 \tag{1a-1d}$$

Viability (robustness):

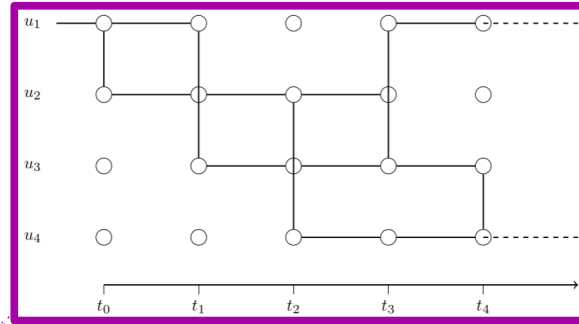
$$\text{Viab}_f(K) = \{\mathbf{x}(0) \in K \mid \exists u(.) \in U \text{ such that } \forall t \geq 0, \mathbf{x}(u(.)) \in K\}$$

Muneepeerakul, R., & Anderies, J. M. (2020). The emergence and resilience of self-organized governance in coupled infrastructure systems. *Proceedings of the National Academy of Sciences*, 117(9), 4617-4622.

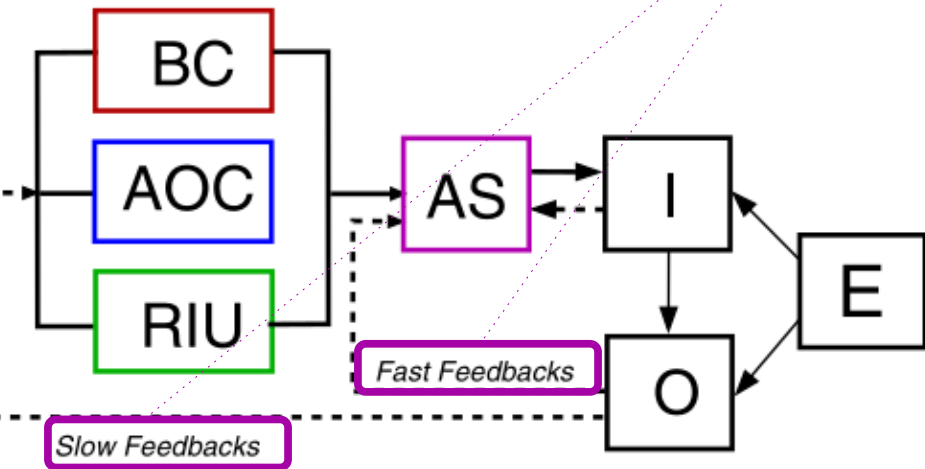
Houbbalah M., Mathias J.-D. and T. Cordonnier. (2021). An infrastructure perspective for enhancing multi-functionality of forests: A conceptual modeling approach. *Earth's Future*.

CIS & Robustness framework

Nested governance

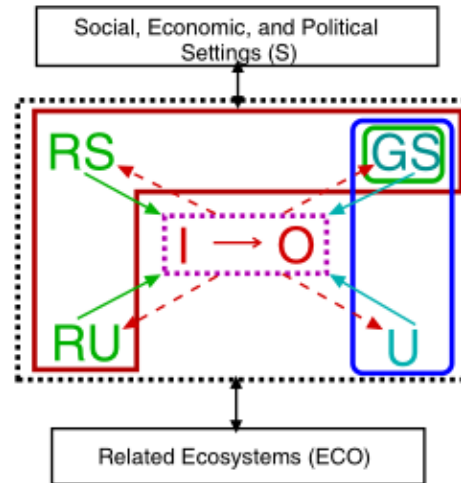


DAPP = "action situation"



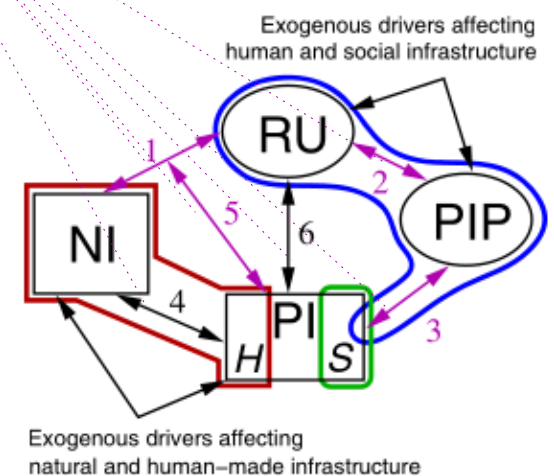
IAD Framework

a



Diagnostic/SES Framework

b



Exogenous drivers affecting natural and human-made infrastructure

Robustness Framework

c

Filtre 3 : Nested levels of gouvernance

Spread actors per nested levels of governance for adaptation actions

Principe 8-B : "Nested governance"

Exploitation (E)

$$U_E = \{U_{E:S}, U_{E:RS}, U_{E:RU}, U_{E:GS}, U_{E:A}, U_{E:I}, U_{E:O}\}$$

$$U^E = \{U_{E:0b}, U_{E:1a}, U_{E:1b}, U_{E:2a}, U_{E:6a}, U_{E:7c}, U_{E:7d}\}$$

Arbitration (P)

$$U_P = \{U_{P:S}, U_{P:RS}, U_{P:RU}, U_{P:GS}, U_{P:A}, U_{P:I}, U_{P:O}\}$$

$$U^P = \{U_{P:0c}, U_{P:2b}, U_{P:3a}, U_{P:7e}, U_{P:7f}\}$$

Conservation (C)

$$U_C = \{U_{C:S}, U_{C:RS}, U_{C:RS}, U_{C:GS}, U_{C:A}, U_{C:I}, U_{C:O}\}$$

Constitutional (CCA)

$$U^E = \{U_{E:0b}, U_{E:1a}, U_{E:1b}, U_{E:2a}, U_{E:6a}, U_{E:7c}, U_{E:7d}\}?$$

$$U_P = \{U_{P:0c}, U_{P:2b}, U_{P:3a}, U_{P:7e}, U_{P:7f}\}?$$

$$U_C = \{U_{C:0d}, U_{C:4a}, U_{C:4b}, U_{C:5a}, U_{C:5b}, U_{C:6b}, U_{C:7g}, U_{C:7h}\}?$$

Who ? What ?

Collective (KCA)

Composition de rôles & d'actions (chaînes)

$$U^{KCA-1} = U_{E:1a}(X) \circ (U_{C:6b} + U_{C:5a}) ?$$

$$U^{KCA-2} = U_{E:1a}(X) + U_{C:4b} ?$$

$$U^{KCA-3} = U_{E:1a}(X) \circ (U_{C:6b} + U_{C:5a}) + U_{C:4b} ? \dots$$

How ?

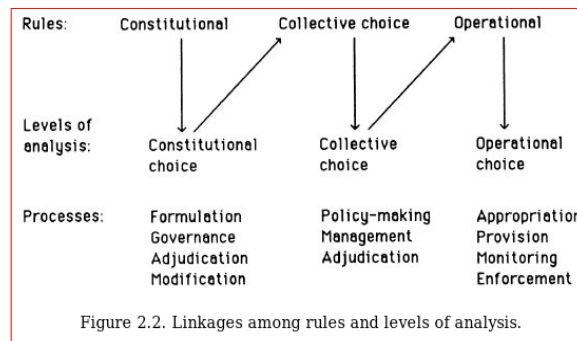
Operational (OCA)

$$U_{E:1a}(X) = [0.1 - 0.5] ? , = [0.5 - 0.9] ?$$

$$U_{C:4b}(X) = [0.2 - 0.3] ? , = [0.7 - 0.8] ?$$

...

How much ?

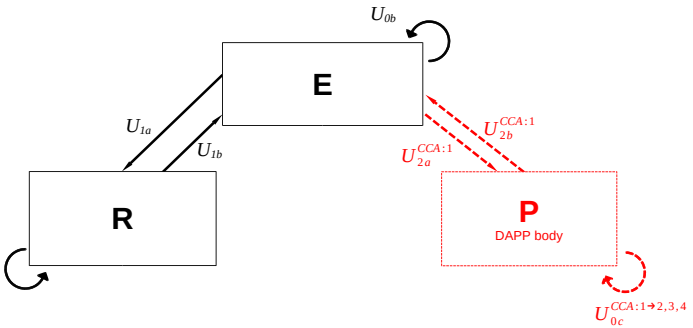


Ostrom, E. (1990). Governing the commons: The evolution of institutions for collective action. Cambridge University Press.

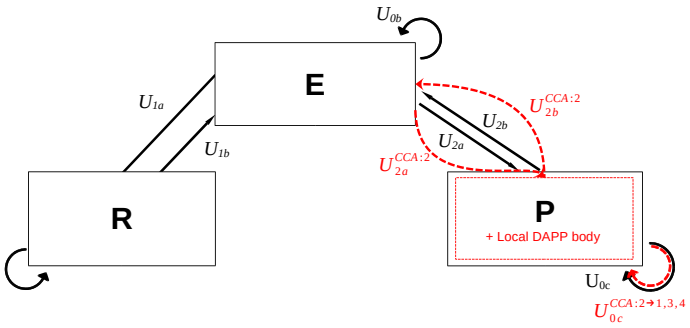
What constitutional choice or who can join ?

Adapt roles of actors & infra. that belong to $U = \{...\}$

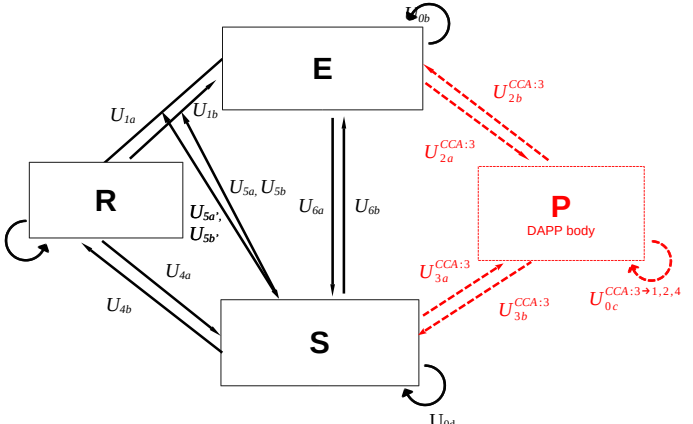
Constitutional-choice CCA-1
(private arrangement)



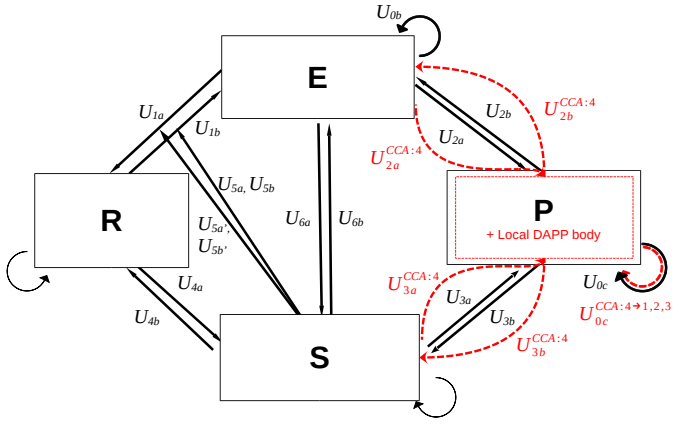
Constitutional-choice CCA-2
(e.g. joint private-public arrangement)



Constitutional-choice CCA-3
(e.g. joint private-community arrangement)



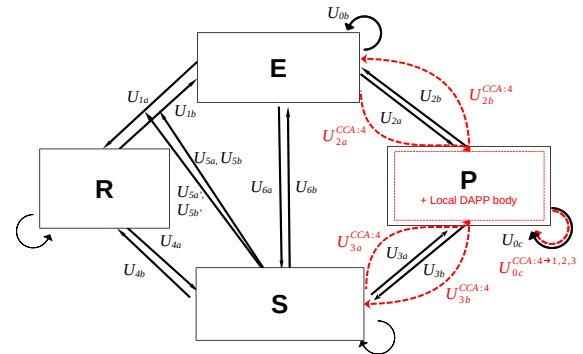
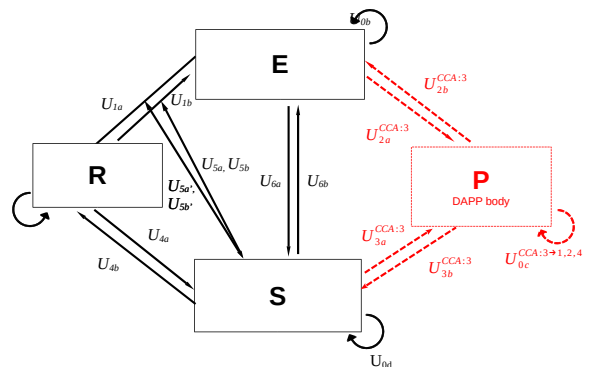
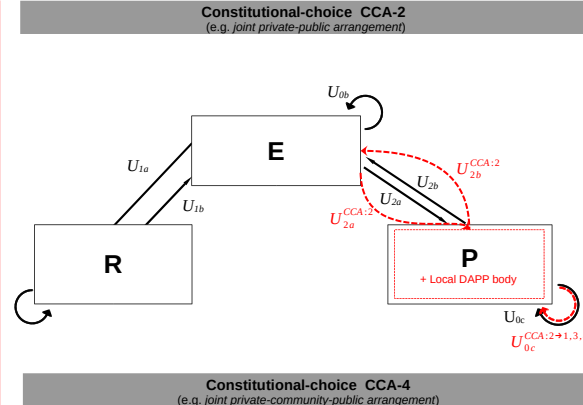
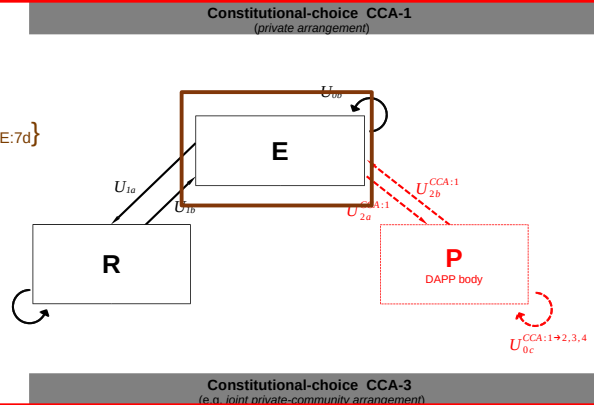
Constitutional-choice CCA-4
(e.g. joint private-community-public arrangement)



What constitutional choice or who can join ?

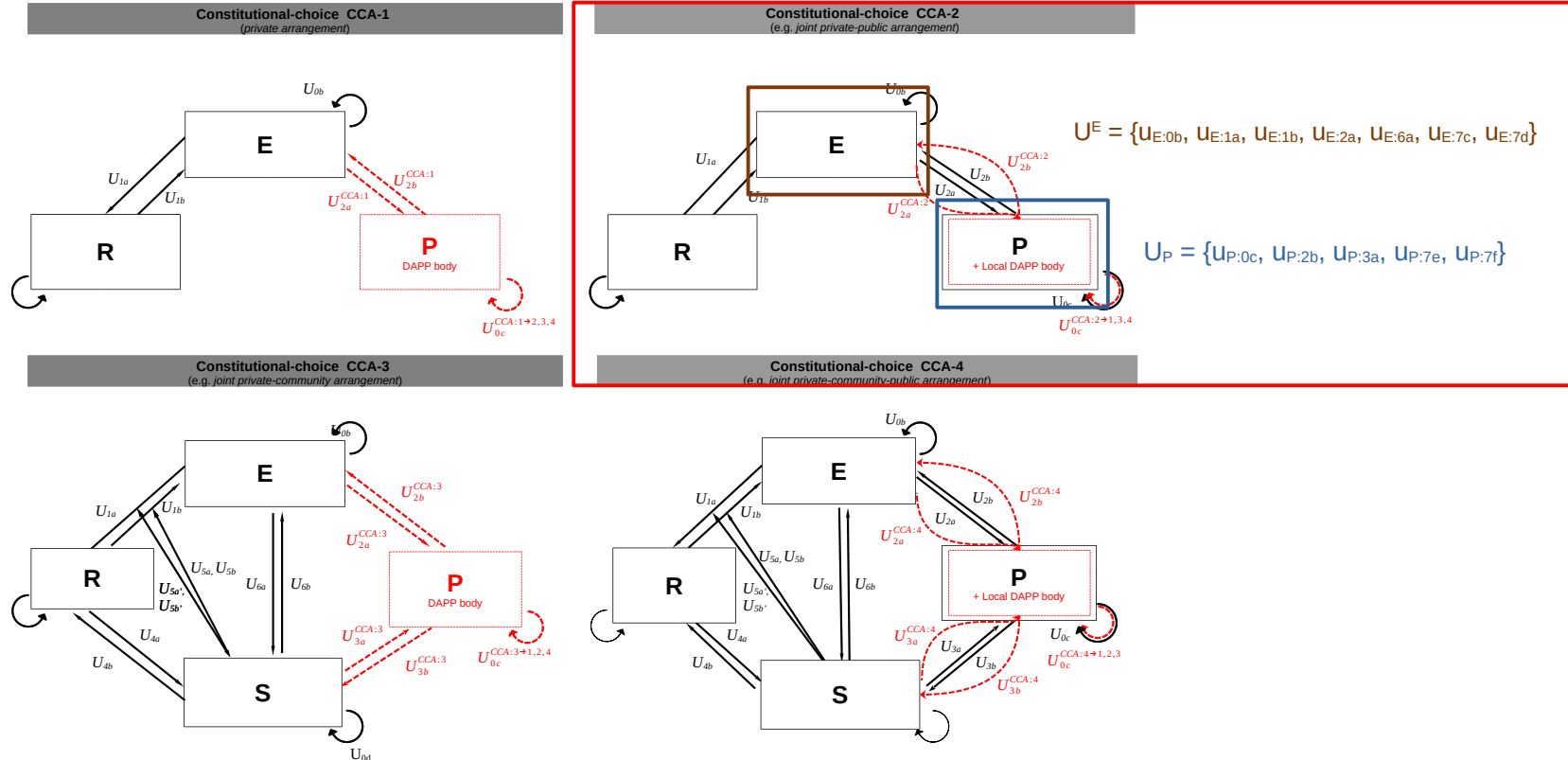
Private arrangement around the resource

$$U^E = \{U_{E:0b}, U_{E:1a}, U_{E:1b}, U_{E:2a}, U_{E:6a}, U_{E:7c}, U_{E:7d}\}$$



What constitutional choice or who can join ?

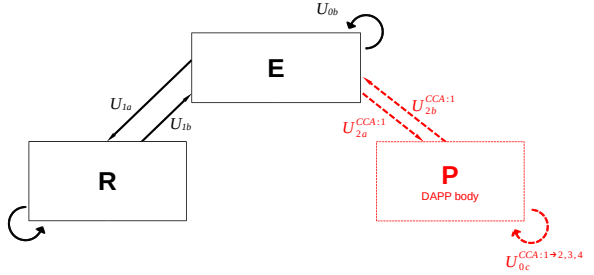
Private-Public arrangement



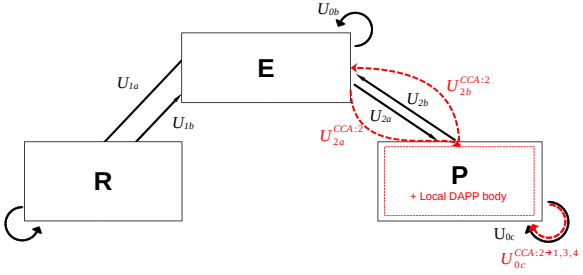
What constitutional choice or who can join ?

Private-Community Arrangement

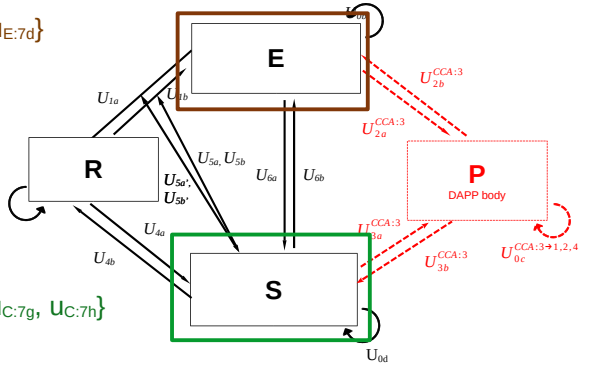
Constitutional-choice CCA-1
(private arrangement)



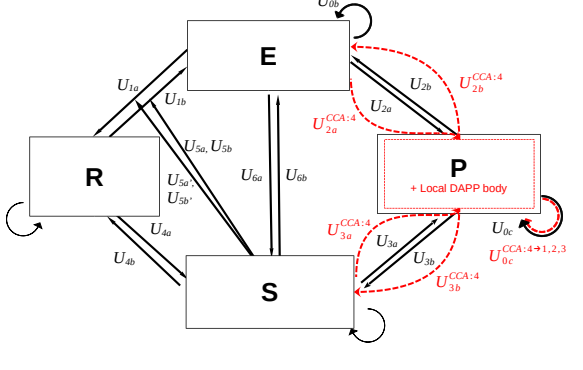
Constitutional-choice CCA-2
(e.g. joint private-public arrangement)



Constitutional-choice CCA-3
(e.g. joint private-community arrangement)



Constitutional-choice CCA-4
(e.g. joint private-community-public arrangement)



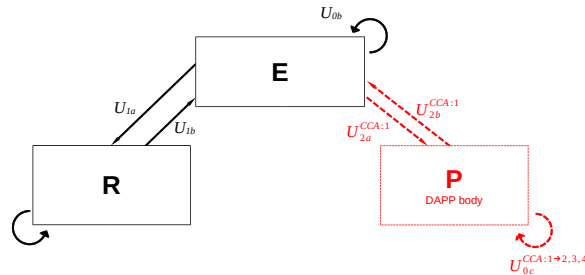
$U^E = \{U_{E:0b}, U_{E:1a}, U_{E:1b}, U_{E:2a}, U_{E:6a}, U_{E:7c}, U_{E:7d}\}$

$U^C = \{U_{C:0d}, U_{C:4a}, U_{C:4b}, U_{C:5a}, U_{C:5b}, U_{C:6b}, U_{C:7g}, U_{C:7h}\}$

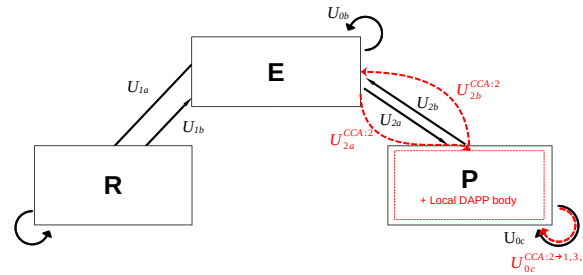
What constitutional choice or who can join ?

Private-Public-Community arrangement

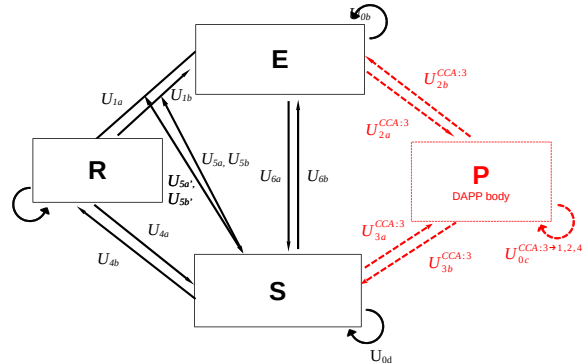
Constitutional-choice CCA-1
(private arrangement)



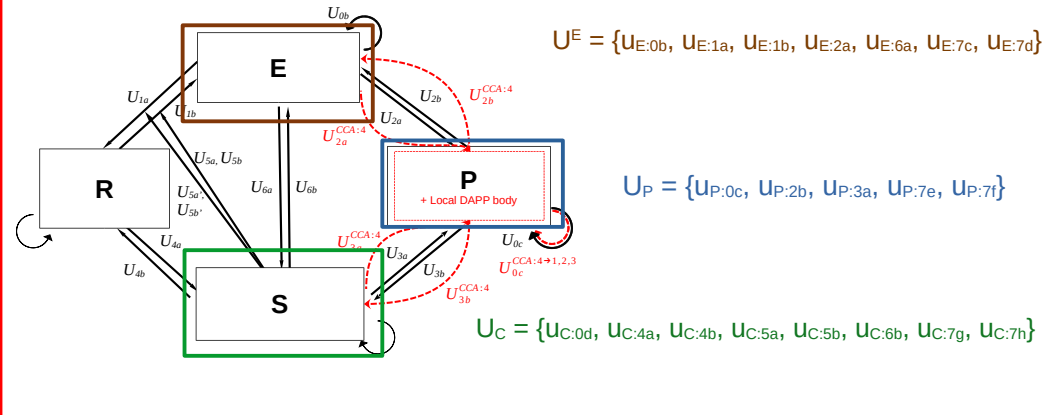
Constitutional-choice CCA-2
(e.g. joint private-public arrangement)



Constitutional-choice CCA-3
(e.g. joint private-community arrangement)



Constitutional-choice CCA-4
(e.g. joint private-community-public arrangement)

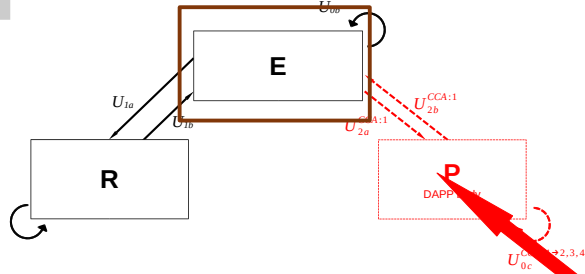


What constitutional choice or who can join ?

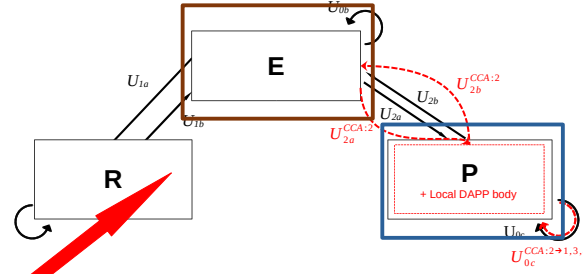
$$U = \{U^{CCA-1}, U^{CCA-2}, U^{CCA-3}, U^{CCA-4}\}$$

$$U^{CCA-1} = \{U^{CCA-1 \rightarrow 1}, U^{CCA-1 \rightarrow 2}, U^{CCA-1 \rightarrow 3}, U^{CCA-1 \rightarrow 4}\}$$

Constitutional-choice CCA-1
(private arrangement)



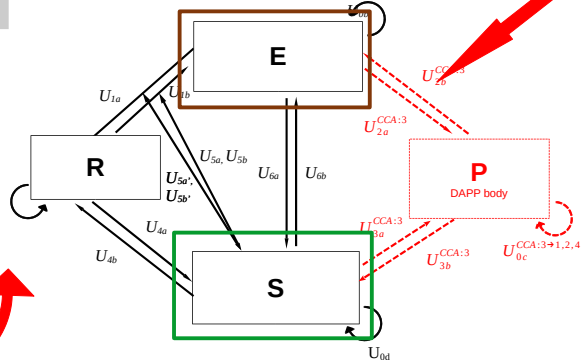
Constitutional-choice CCA-2
(e.g. joint private-public arrangement)



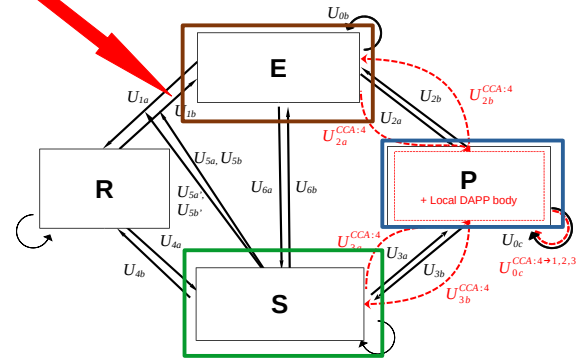
$$U^{CCA-2} = \{U^{CCA-2 \rightarrow 1}, U^{CCA-2 \rightarrow 2}, U^{CCA-2 \rightarrow 3}, U^{CCA-2 \rightarrow 4}\}$$

$$U^{CCA-3} = \{U^{CCA-3 \rightarrow 1}, U^{CCA-3 \rightarrow 2}, U^{CCA-3 \rightarrow 3}, U^{CCA-3 \rightarrow 4}\}$$

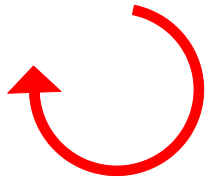
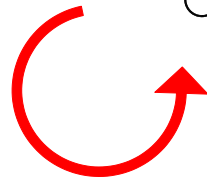
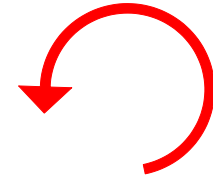
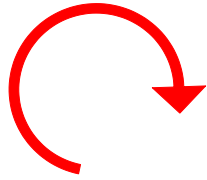
Constitutional-choice CCA-3
(e.g. joint private-community arrangement)



Constitutional-choice CCA-4
(e.g. joint private-community-public arrangement)



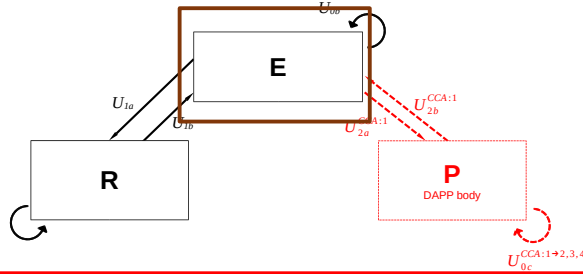
$$U^{CCA-4} = \{U^{CCA-4 \rightarrow 1}, U^{CCA-4 \rightarrow 2}, U^{CCA-4 \rightarrow 3}, U^{CCA-4 \rightarrow 4}\}$$



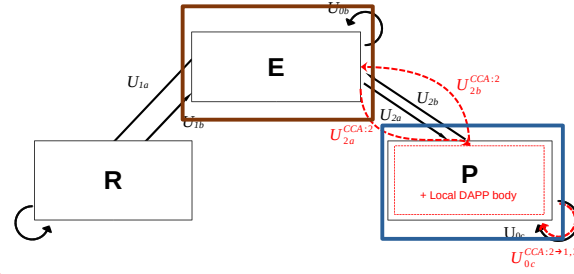
What constitutional choice or who can join ?

Private-Community Arrangement

Constitutional-choice CCA-1
(private arrangement)

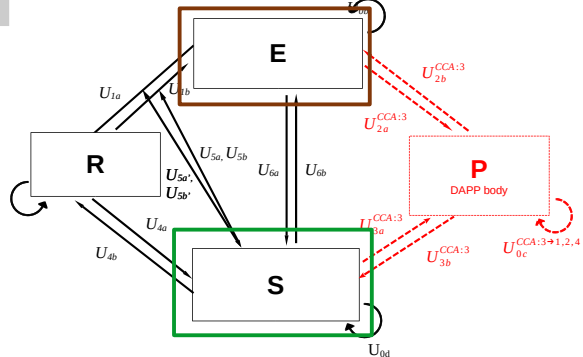


Constitutional-choice CCA-2
(e.g. joint private-public arrangement)

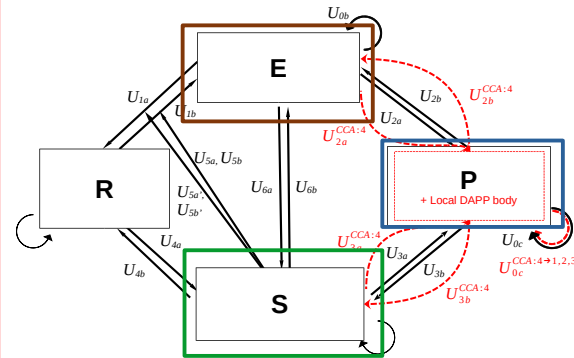


$$U^{CCA-3} = \{U^{CCA-3 \rightarrow 1}, U^{CCA-3 \rightarrow 2}, U^{CCA-3 \rightarrow 3}, U^{CCA-3 \rightarrow 4}\}$$

Constitutional-choice CCA-3
(e.g. joint private-community arrangement)



Constitutional-choice CCA-4
(e.g. joint private-community-public arrangement)

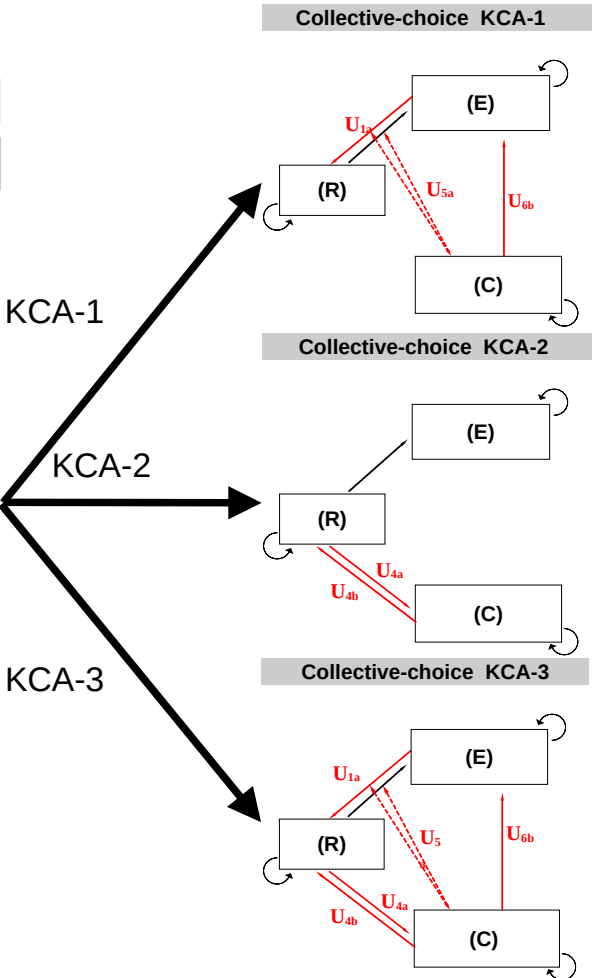
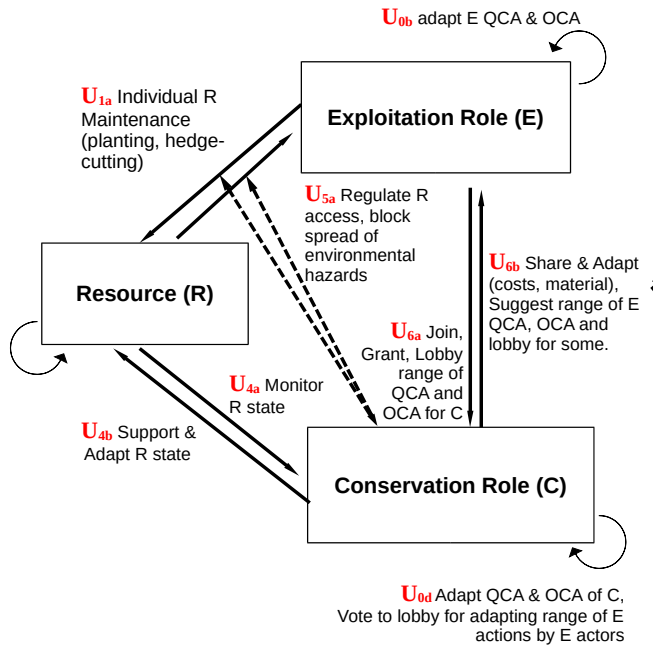


What collective choice or how to join?

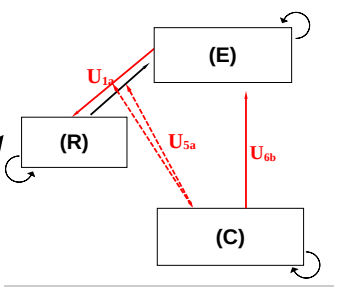
Adapt composition (chains / network) of roles & actions ($u_1(x) \circ u_2$)

$$\mathcal{U}^{KCA} = \{\mathcal{U}^{KCA:1}, \mathcal{U}^{KCA:2}, \mathcal{U}^{KCA:3}\} \in \mathcal{U}^{CCA:3}$$

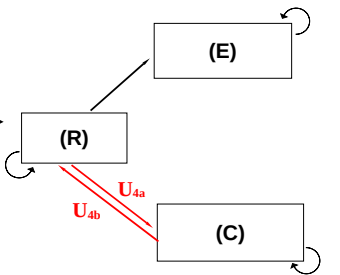
Constitutional-choice CCA-3
(e.g. joint private-community arrangement)



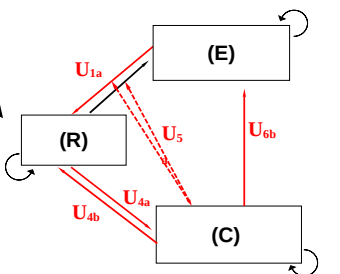
Collective-choice KCA-1



Collective-choice KCA-2



Collective-choice KCA-3



$$\mathcal{U}^{KCA:1} : u_{1a}(R) \circ (u_{6b} + u_{5a})$$

$$\mathcal{U}^{KCA:1} = \{\mathcal{U}^{KCA:1 \rightarrow 1}, \mathcal{U}^{KCA:1 \rightarrow 2}, \mathcal{U}^{KCA:1 \rightarrow 3}\}$$

$$\mathcal{U}^{KCA:2} : u_{1a}(R) + u_{4b} \circ u_{4a}$$

$$\mathcal{U}^{KCA:2} = \{\mathcal{U}^{KCA:2 \rightarrow 1}, \mathcal{U}^{KCA:2 \rightarrow 2}, \mathcal{U}^{KCA:2 \rightarrow 3}\}$$

$$\mathcal{U}^{KCA:3} : u_{1a}(R) \circ (u_{6b} + u_{5a}) + u_{4b} \circ u_{4a}$$

$$\mathcal{U}^{KCA:3} = \{\mathcal{U}^{KCA:3 \rightarrow 1}, \mathcal{U}^{KCA:3 \rightarrow 2}, \mathcal{U}^{KCA:3 \rightarrow 3}\}$$

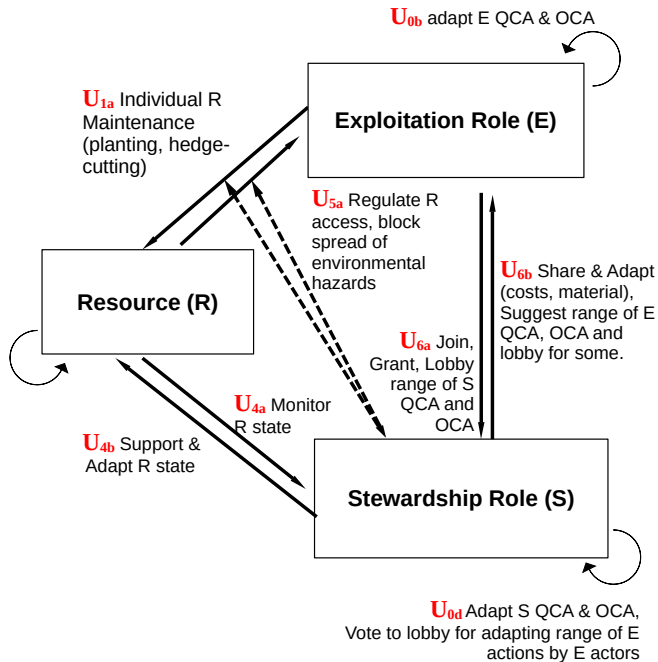
What collective choice or how to join?

Adapt composition (chains / network) of roles & actions ($u_1(x) \circ u_2$)

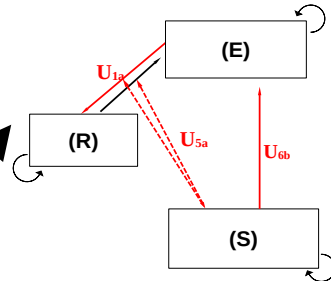
$$U^{KCA} = \{U^{KCA:1}, U^{KCA:2}, U^{KCA:3}\} \in U^{CCA:3}$$

Constitutional-choice CCA-3

(e.g. joint private-community arrangement)



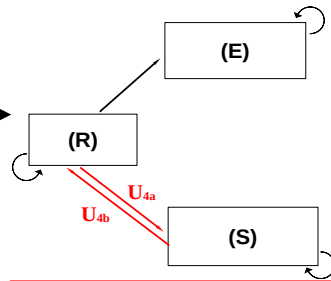
Collective-choice KCA-1



$$U^{KCA:1} : u_{1a}(R) \circ (u_{6b} + u_{5a})$$

$$U^{KCA:1} = \{U^{KCA:1 \rightarrow 1}, U^{KCA:1 \rightarrow 2}, U^{KCA:1 \rightarrow 3}\}$$

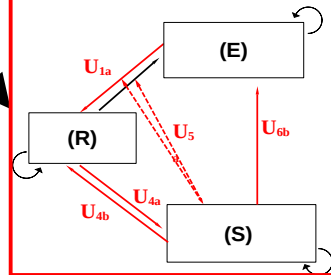
Collective-choice KCA-2



$$U^{KCA:2} : u_{1a}(R) + u_{4b} \circ u_{4a}$$

$$U^{KCA:2} = \{U^{KCA:2 \rightarrow 1}, U^{KCA:2 \rightarrow 2}, U^{KCA:2 \rightarrow 3}\}$$

Collective-choice KCA-3



$$U^{KCA:3} : u_{1a}(R) \circ (u_{6b} + u_{5a}) + u_{4b} \circ u_{4a}$$

$$U^{KCA:3} = \{U^{KCA:3 \rightarrow 1}, U^{KCA:3 \rightarrow 2}, U^{KCA:3 \rightarrow 3}\}$$

What operational choice or which level of action ?

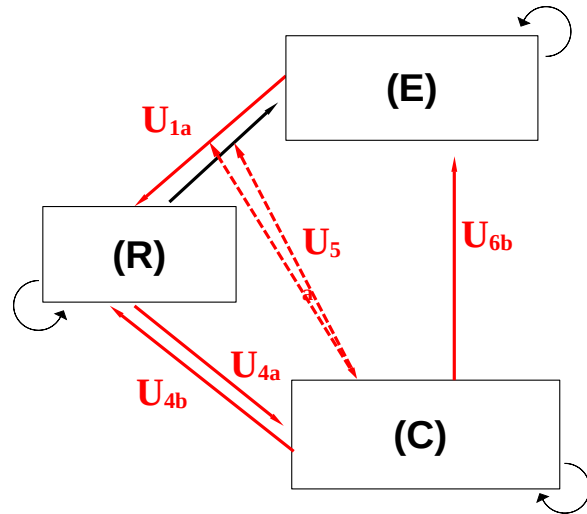
Adapt intensity, frequency of actions

$$U^{OCA} = \{U^{OCA:1}, U^{OCA:2}\} \in U^{KCA:3}$$

$$U^{OCA:1} = \{U^{OCA:1 \rightarrow 1}, U^{OCA:1 \rightarrow 2}\}$$

$$U^{OCA:2} = \{U^{OCA:2 \rightarrow 1}, U^{OCA:2 \rightarrow 2}\}$$

Collective-choice KCA-3



U_{1a} : Exploit



$\rightarrow U_{1a} =$

U_{5a} : Regulate access



$\rightarrow U_{5a} =$

U_{4b} : Replant for conservation



$\rightarrow U_{4b} =$

U_{4a} : Monitor for conservation



$\rightarrow U_{4a} =$

OCA-1

OCA-2

$\{= [0.1 - 0.5], = [0.5 - 0.9]\}$

$\{\leq - 0.05, \leq - 0.4\}$

$\{= 0.2, = [0.3 - 0.4]\}$

$\{= 0.1, \geq 0.5\}$

$$U = \{u_1, u_2, \dots, u_n\}$$

SES framework

Construction the set T of 2nd tier actions based on a version of Ostrom's social-ecological system framework (SESF)

Set of actions related to the social, economic & political Settings (S1)	
U11 Economic development **	U14 Other governance systems †
U12 Demographic trends ** †	U15 Markets †
U13 Political stability (type of political change) ** †	U16 Media organizations †
	U17 Technology †
Set of actions related to the Resource Systems (R1a)	
U21a Scarce	U21a Resource availability ** †
U21b Clarity of system boundaries	U21b Growth or replacement rate of resource units
U21c Size of resource system	U21c Interactions among resource units ** †
U21d Human controlled facilities *	U21d Economic value
U21e Productivity of the system	U21e Number of units
U21f Equilibrium properties	U21f Distinctive characteristics
U21g Resiliability of system dynamics	U21g Spatial & temporal distribution
U21h Change characteristics	
U21i Location	
U21ja Ecosystem history	
Set of actions related to the Governance Systems (G1a)	
U31a Policy area	U31a Number of resource users *
U31b Organizational mode of governance systems *	U31b Socio-economic institutions *
U31c Propensity of participating organizations**	U31c History of past experience **
U31d Rights type (individualistic, community-centric) *	U31d Location*
U31e Rule-making organizations **	U31e Leadership / entrepreneurship *
U31f Institutions	U31f Assets (non-ecological), social capital
U31g Property rights systems (relations among people in relation to resource units and infrastructure) *	U31g Knowledge of SES / mental models / beliefs *
U31h Preparation of cultural knowledge, beliefs, norms, practices (strategic) with-to rules and sanctions *	U31h Preparation of resource dependent actions *
U31i Network structure (interactions among the rule-making organizations and the population subject to those rules) **	U31i Technologies available *
U31j Resilience/continuity of the governance system (rules or long lasting, open or close to internal adaptation) *	
Set of actions related to the Interactions (I1)	
U41 Harvesting (using resource units by direct users)	U41 Social performance measures (e.g. efficiency, equity, accountability, sustainability) **
U42 Information sharing among actors **	U42 Ecological performance measures (e.g. environmental, resilience, robustness, sustainability) **
U43 Collaboration process **	U43 Extraneous to other SES †
U44 Conflict among actors **	
U45 Investment activities **	
U46 Learning activities **	
U47 Self-organizing activities **	
U48 Monitoring activities **	
U49 Maintaining activities **	
U4a Evaluation activities **	

$$U = \{u_1, u_2, \dots, u_n\}$$



CIS framework

Construction the set U of 2nd tier actions based on a version of Ostrom's social-ecological system framework (SESF)

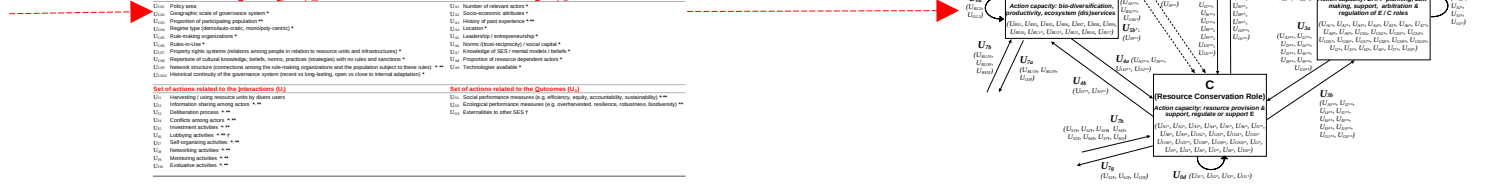
Set of actions related to the social, economic & political Settings (S)	
U_{S1} Economic development **	U_{S2} Other governance system ?
U_{S3} Demographic trends **	U_{S4} Markets ?
U_{S5} Political stability (over of political change) **	U_{S6} Media organization ?
	U_{S7} Technology ?

Set of actions related to the Resource Systems (R)		Set of actions related to the Resource Limits (L)	
U_{R1} Scarce	U_{L1} Resource endowments **	U_{L2} Growth or replacement rate of resource units	U_{L3} Interactions among resource units **
U_{R2} Clarity of system boundaries	U_{L4} Economic value	U_{L5} Number of units	U_{L6} Disturbance characteristics
U_{R3} Ease of resource system	U_{L7} Spatial & temporal distribution		
U_{R4} Human controlled facilities *			
U_{R5} Probability of the system			
U_{R6} Equilibrium properties			
U_{R7} Predictability of system dynamics			
U_{R8} Storage characteristics			
U_{R9} Land-use			
U_{R10} Ecosystem history			

Set of actions related to the Governance Systems (G)		Set of actions related to the Actors (A)	
U_{G1} Policy rules	U_{A1} Nature of resource access *	U_{A2} Socio-economic attributes	U_{A3} History of past experience **
U_{G2} Geographic scale of governance systems **	U_{A4} Location *	U_{A5} Land-use / entrepreneurship *	U_{A6} Knowledge of SES / mental models / beliefs *
U_{G3} Geographic scale of governance systems **	U_{A7} Proprietor of resource dependent access *	U_{A8} Technological assets *	
U_{G4} Propriety of participating organizations **			
U_{G5} Multiple scale (territorial-ethnic-identity-context) *			
U_{G6} Institutional rules			
U_{G7} Property rights systems (relations among people in relation to resource units and infrastructure) *			
U_{G8} Preparation of cultural knowledge, beliefs, norms, practices (strategic) with no rules and sanctions *			
U_{G9} Network structure (interactions among the rule-making organizations and the population subject to those rules) **			
U_{G10} Historical continuity of the governance system (rules or long lasting, open or close to internal adaptation) *			

Set of actions related to the Interactions (I)		Set of actions related to the Outcomes (O)	
U_{I1} Harvesting (using resource units by users) users	U_{O1} Social performance measures (e.g. efficiency, equity, accountability, sustainability) **	U_{O2} Ecological performance measures (e.g. environmental, resilience, robustness, biodiversity) **	U_{O3} Extraneous to other SES ?
U_{I2} Information sharing among actors **			
U_{I3} Collaboration process **			
U_{I4} Conflict among actors **			
U_{I5} Investment activities **			
U_{I6} Learning activities **			
U_{I7} Self-organizing activities **			
U_{I8} Monitoring activities **			
U_{I9} Maintaining activities **			
U_{I10} Enforcing activities **			

$$U = \{u_1, u_2, \dots, u_n\}$$



$$U = \{u_1, u_2, \dots, u_n\}$$

Construction the set U of 2nd tier actions based on a version of Ostrom's social-ecological system framework (SESF)

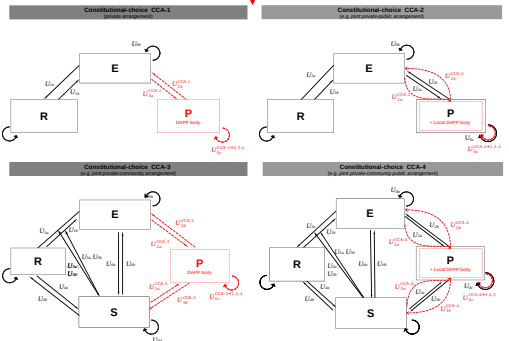
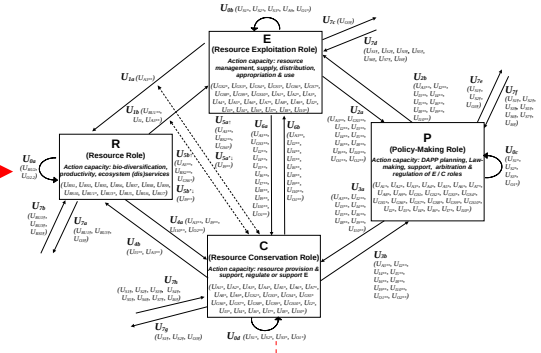
Set of actions related to the social, economic & political settings (S)	
U _{S1} : Economic development **	U _{S2} : Other governance system ?
U _{S3} : Demographic trends **	U _{S4} : Markets ?
U _{S5} : Political stability (over of political change) **	U _{S6} : Media organisations ?
U _{S7} : Technology ?	

Set of actions related to the Resource Systems (R)	
U _{R1} : State	U _{R2} : Resource availability **
U _{R3} : Clarity of system boundaries	U _{R4} : Growth or replacement rate of resource units
U _{R5} : State of resource system	U _{R6} : Interactions among resource units **
U _{R7} : Human controlled facilities	U _{R8} : Economic value
U _{R9} : Number of users	U _{R10} : Disturbance characteristics
U _{R11} : Equilibrium properties	U _{R12} : Spatial & temporal distribution
U _{R13} : Predictability of system dynamics	
U _{R14} : Storage characteristics	
U _{R15} : Variability	
U _{R16} : Ecosystem theory	

Set of actions related to the Governance Systems (G)	
U _{G1} : Policy rules	U _{G2} : Number of resource users *
U _{G3} : Ontogenetic choice of governance systems **	U _{G4} : Social-economic stability **
U _{G5} : Propensity of participating organisations **	U _{G6} : History of past experience **
U _{G7} : Legitimacy (non-coercive, non-punitive control) *	U _{G8} : Leadership *
U _{G9} : Role-making organisations *	U _{G10} : Norms (non-reciprocity), social capital *
U _{G11} : Property rights systems (relations among people in relation to resource units and infrastructure) *	U _{G12} : Knowledge of SES / mental models / beliefs *
U _{G13} : Preparation of cultural knowledge, beliefs, norms, practices (strategies) with/for rules and sanctions *	U _{G14} : Propagation of resource management actions *
U _{G15} : Network structure (interactions among the rule-making organisations and the population subject to these rules) **	U _{G16} : Technological assistance *
U _{G17} : Historical continuity of the governance system (rules or long lasting, open or close to internal adaptation) *	

Set of actions related to the Interactions (I)	
U _{I1} : Harvesting (using resource units by direct users)	U _{I2} : Social performance measures (e.g. efficiency, equity, accountability, sustainability) **
U _{I3} : Information sharing among actors **	U _{I4} : Ecological performance measures (e.g. environmental, resilience, robustness, sustainability) **
U _{I5} : Collaboration process **	U _{I6} : Expenditure to other SES ?
U _{I7} : Conflict among actors **	
U _{I9} : Investment activities **	
U _{I11} : Learning activities **	
U _{I13} : Self-organising activities **	
U _{I15} : Monitoring activities **	
U _{I17} : Maintaining activities **	
U _{I19} : Collaborative activities **	

Set of actions related to the Actors (A)	
U _{A1} : Resource unit quality **	U _{A2} : Action capacity: bio-diversification, productivity, ecosystem (bio)resilience (U _{A2a} , U _{A2b} , U _{A2c} , U _{A2d} , U _{A2e} , U _{A2f} , U _{A2g} , U _{A2h} , U _{A2i} , U _{A2j} , U _{A2k} , U _{A2l} , U _{A2m} , U _{A2n} , U _{A2o} , U _{A2p} , U _{A2q} , U _{A2r} , U _{A2s} , U _{A2t} , U _{A2u} , U _{A2v} , U _{A2w} , U _{A2x} , U _{A2y} , U _{A2z})
U _{A3} : Legitimacy *	U _{A4} : Action capacity: DAPP planning, law making, resource, application & propagation of E/C rules (U _{A4a} , U _{A4b} , U _{A4c} , U _{A4d} , U _{A4e} , U _{A4f} , U _{A4g} , U _{A4h} , U _{A4i} , U _{A4j} , U _{A4k} , U _{A4l} , U _{A4m} , U _{A4n} , U _{A4o} , U _{A4p} , U _{A4q} , U _{A4r} , U _{A4s} , U _{A4t} , U _{A4u} , U _{A4v} , U _{A4w} , U _{A4x} , U _{A4y} , U _{A4z})
U _{A5} : Norms (non-reciprocity), social capital *	U _{A6} : Action capacity: resource provision at support, regulation or support & (U _{A6a} , U _{A6b} , U _{A6c} , U _{A6d} , U _{A6e} , U _{A6f} , U _{A6g} , U _{A6h} , U _{A6i} , U _{A6j} , U _{A6k} , U _{A6l} , U _{A6m} , U _{A6n} , U _{A6o} , U _{A6p} , U _{A6q} , U _{A6r} , U _{A6s} , U _{A6t} , U _{A6u} , U _{A6v} , U _{A6w} , U _{A6x} , U _{A6y} , U _{A6z})
U _{A7} : Knowledge of SES / mental models / beliefs *	
U _{A8} : Propagation of resource management actions *	
U _{A9} : Technological assistance *	

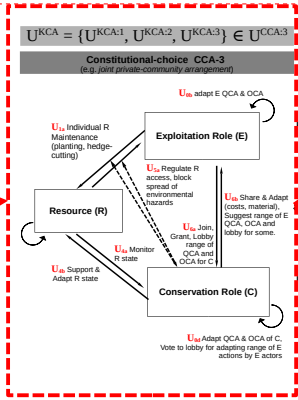
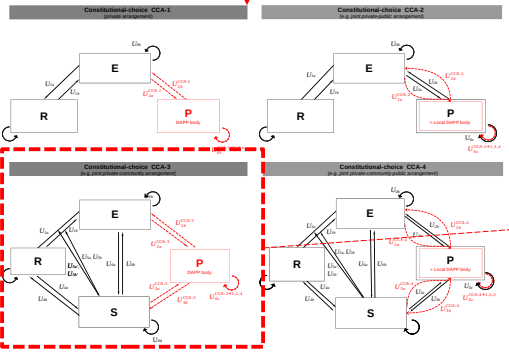
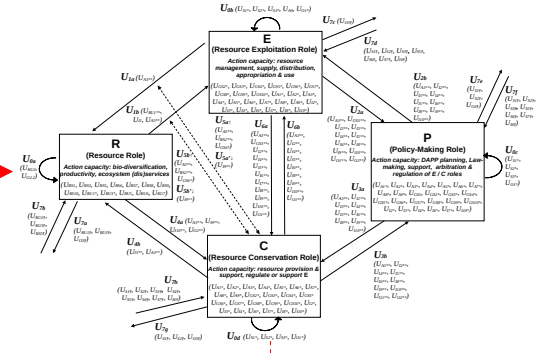


Constitutional-level adaptation actions

$$U = \{u_1, u_2, \dots, u_n\}$$

Construction of the set U of 2nd tier actions based on a version of Ostrom's social-ecological system framework (SESF)

Set of actions related to the social, economic & political Settings (S₁) U ₁ : Economic development * U ₂ : Demographic trends * U ₃ : Political stability (over of political change) **	U ₄ : Other governance system * U ₅ : Markets * U ₆ : Media organization * U ₇ : Technology *
Set of actions related to the Resource Systems (R₁) U ₈ : Scarce U ₉ : Clarity of system boundaries U ₁₀ : Size of resource system U ₁₁ : Harms associated facilities * U ₁₂ : Probability of the system U ₁₃ : Equilibrium properties U ₁₄ : Predictability of system dynamics U ₁₅ : Storage characteristics U ₁₆ : Location U ₁₇ : Ecosystem history	Set of actions related to the Resource Units (R₂) U ₁₈ : Resource unit history * U ₁₉ : Growth or replacement rate of resource units U ₂₀ : Interactions among resource units * U ₂₁ : Economic value U ₂₂ : Number of units U ₂₃ : Disturbance characteristics U ₂₄ : Spatial & temporal distribution
Set of actions related to the Governance Systems (U₁) U ₂₅ : Policy mix U ₂₆ : Geographic scale of governance system * U ₂₇ : Propriety of participating population ** U ₂₈ : Legitimacy (social-ecological-ecology-culture) * U ₂₉ : Incentive mix (formal-informal-implicit-contract) * U ₃₀ : Role-making organizations U ₃₁ : Social norms U ₃₂ : Property rights systems (relations among people in relation to resource units and infrastructure) * U ₃₃ : Preparation of cultural knowledge, beliefs, norms, practices (integrated with role and institutions) * U ₃₄ : Network structure (connections among the role-making organizations and the population subject to these rules) ** U ₃₅ : Historical continuity of the governance system (does it keep being, open or close to external adaptation) *	Set of actions related to the Actors (U₂) U ₃₆ : Number of resource actors * U ₃₇ : Socio-economic attributes * U ₃₈ : History of past experience ** U ₃₉ : Location * U ₄₀ : Role-making organizations U ₄₁ : Norms (formal-informal) social capital * U ₄₂ : Knowledge of SES / mental models / beliefs * U ₄₃ : Propriety of resource dependent actors * U ₄₄ : Technological assets *
Set of actions related to the Interactions (U₃) U ₄₅ : Harvesting (using resource units by users) U ₄₆ : Information sharing among actors ** U ₄₇ : Collaboration process ** U ₄₈ : Conflict among actors ** U ₄₉ : Investment activities ** U ₅₀ : Lobbying activities ** U ₅₁ : Self-organizing activities ** U ₅₂ : Monitoring activities ** U ₅₃ : Maintaining activities ** U ₅₄ : Enforcing activities **	Set of actions related to the Outcomes (U₄) U ₅₅ : Social performance measures (e.g. efficiency, equity, accountability, sustainability) ** U ₅₆ : Ecological performance measures (e.g. environmental, resilience, robustness, sustainability) ** U ₅₇ : Extraneous to other SES *



Collective-choice KCA-1

Collective-choice KCA-2

Collective-choice KCA-3

$$U^{KCA:1} : u_{1a}(R) \circ (u_{6b} + u_{5a})$$

$$U^{KCA:1} = \{U^{KCA:1-1}, U^{KCA:1-2}, U^{KCA:1-3}\}$$

$$U^{KCA:2} : u_{1a}(R) + u_{4b} \circ u_{4a}$$

$$U^{KCA:2} = \{U^{KCA:2-1}, U^{KCA:2-2}, U^{KCA:2-3}\}$$

$$U^{KCA:3} : u_{1a}(R) \circ (u_{6b} + u_{5a}) + u_{4b} \circ u_{4a}$$

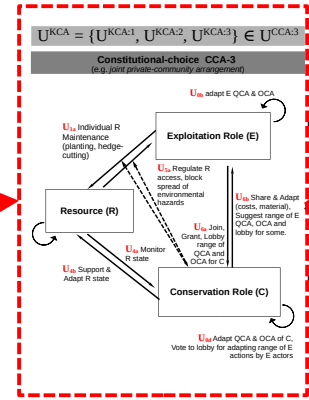
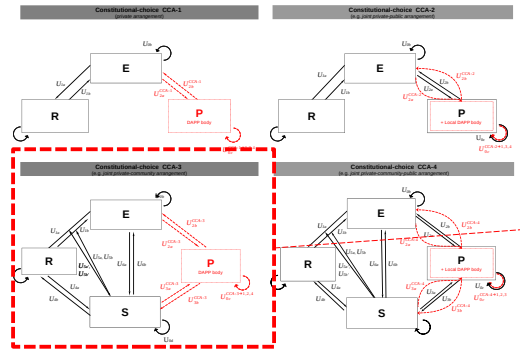
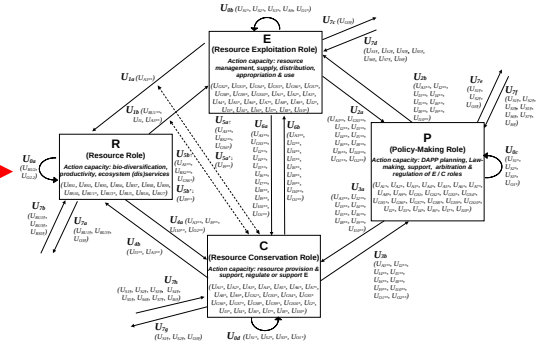
$$U^{KCA:3} = \{U^{KCA:3-1}, U^{KCA:3-2}, U^{KCA:3-3}\}$$

Collective-level adaptation actions

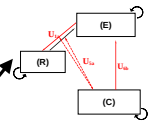
Construction of the set 1st tier actions based on a version of Odum's social-ecological system framework (SESF)

Set of actions related to the social, economic & political Settings (S) U ₁ : Economic development + U ₂ : Demographic trends + U ₃ : Political stability (or political change) +	U ₄ : Other governance systems + U ₅ : Markets + U ₆ : Media organization + U ₇ : Technology +
Set of actions related to the Resource Systems (R) U ₈ : Energy U ₉ : Clarity of system boundaries U ₁₀ : Size of resource system U ₁₁ : Human controlled facilities + U ₁₂ : Probability of the system U ₁₃ : Equilibrium properties U ₁₄ : Predictability of system dynamics U ₁₅ : Storage characteristics U ₁₆ : Land-use U ₁₇ : Ecosystem theory	Set of actions related to the Resource Units (U) U ₁₈ : Resource unit stability + U ₁₉ : Growth or replacement rate of resource units U ₂₀ : Interactions among resource units + U ₂₁ : Economic value U ₂₂ : Number of units U ₂₃ : Disturbance characteristics U ₂₄ : Spatial & temporal distribution
Set of actions related to the Governance Systems (G) U ₂₅ : Policy area U ₂₆ : Geographic scope of governance system + U ₂₇ : Social-economic institutions + U ₂₈ : Propriety of participation practices + U ₂₉ : Incentive (or disincentive) structure + U ₃₀ : Stake-making organizations U ₃₁ : Stakeholder U ₃₂ : Property rights systems (relations among people in relation to resource units and infrastructure) + U ₃₃ : Preparation of cultural ecological audits, norms, practices (integrated with risk and scenarios) + U ₃₄ : Network structure (connections among the role-making organizations and the population subject to those roles) + U ₃₅ : Historical continuity of the governance system (does it keep being open or close to external adaptation) +	Set of actions related to the Actors (A) U ₃₆ : Number of relevant actors + U ₃₇ : Social-economic institutions + U ₃₈ : History of past experience + U ₃₉ : Location + U ₄₀ : Leadership / entrepreneurship + U ₄₁ : Norms (ethno-ecology), social capital + U ₄₂ : Knowledge of SES / mental models / beliefs + U ₄₃ : Propriety of resource dependent actors + U ₄₄ : Technological assets +
Set of actions related to the Interactions (I) U ₄₅ : Harvesting / using resource units by direct users U ₄₆ : Information sharing among actors + U ₄₇ : Collaboration process + U ₄₈ : Conflict among actors + U ₄₉ : Investment activities + U ₅₀ : Lobbying activities + U ₅₁ : Self-organizing activities + U ₅₂ : Monitoring activities + U ₅₃ : Maintaining activities + U ₅₄ : Enforcing activities +	Set of actions related to the Outcomes (O) U ₅₅ : Social performance measures (e.g. efficiency, equity, accountability, sustainability) + U ₅₆ : Ecological performance measures (e.g. environmental, resilience, robustness, sustainability) + U ₅₇ : Expenditure to other SES +

$$U = \{u_1, u_2, \dots, u_n\}$$



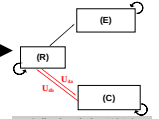
Collective-choice KCA-1



$$U^{KCA:1} : u_{1a}(R) \circ (u_{6b} + u_{5a})$$

$$U^{KCA:1} = \{U^{KCA:1-1}, U^{KCA:1-2}, U^{KCA:1-3}\}$$

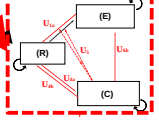
Collective-choice KCA-2



$$U^{KCA:2} : u_{1a}(R) + u_{4b} \circ u_{4a}$$

$$U^{KCA:2} = \{U^{KCA:2-1}, U^{KCA:2-2}, U^{KCA:2-3}\}$$

Collective-choice KCA-3



$$U^{KCA:3} : u_{1a}(R) \circ (u_{6b} + u_{5a}) + u_{4b} \circ u_{4a}$$

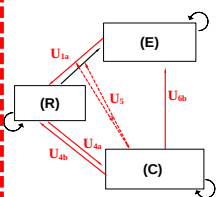
$$U^{KCA:3} = \{U^{KCA:3-1}, U^{KCA:3-2}, U^{KCA:3-3}\}$$

$$U^{OCA} = \{U^{OCA:1}, U^{OCA:2}\} \in U^{KCA:3}$$

$$U^{OCA:1} = \{U^{OCA:1-1}, U^{OCA:1-2}\}$$

$$U^{OCA:2} = \{U^{OCA:2-1}, U^{OCA:2-2}\}$$

Collective-choice KCA-3



U_{1a}: Exploit



$$\rightarrow U_{1a} = \{= [0.1 - 0.5], = [0.5 - 0.9]\}$$

U_{5a}: Regulate access



$$\rightarrow U_{5a} = \{\leq -0.05, \leq -0.4\}$$

U_{4b}: Replant for conservation



$$\rightarrow U_{4b} = \{= -0.2, = [0.3 - 0.4]\}$$

U_{1a}: Monitor for conservation



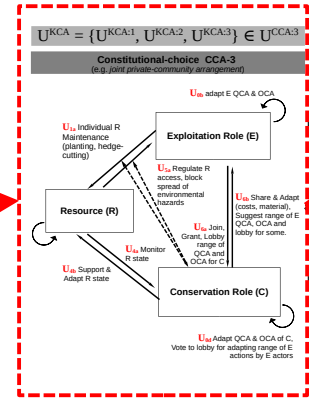
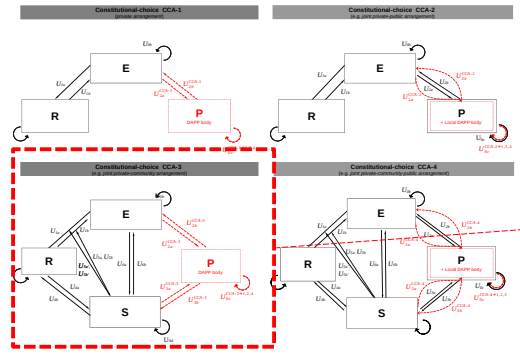
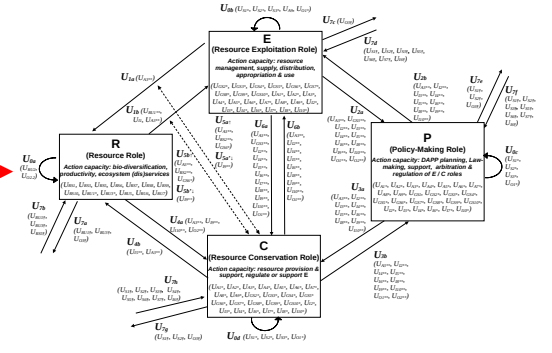
$$\rightarrow U_{1a} = \{= 0.1, \geq 0.5\}$$

Operational-level adaptation actions

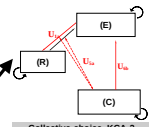
$$U = \{u_1, u_2, \dots, u_n\}$$

Construction the set 1' of 2nd tier actions based on a version of Odum's social-ecological system framework (SESF)

Set of actions related to the social, economic & political Settings (S) U ₁ : Economic development * U ₂ : Demographic trends * U ₃ : Political stability (over of political change) **	U ₄ : Other governance system * U ₅ : Markets * U ₆ : Media organization * U ₇ : Technology *
Set of actions related to the Resource Systems (R) U ₈ : Energy U ₉ : Clarity of system boundaries U ₁₀ : Clarity of resource system U ₁₁ : Human controlled facilities * U ₁₂ : Probability of the system U ₁₃ : Equilibrium properties U ₁₄ : Predictability of system dynamics U ₁₅ : Storage characteristics U ₁₆ : Variability U ₁₇ : Ecosystem theory	Set of actions related to the Resource Units (U) U ₁₈ : Resource unit stability * U ₁₉ : Growth or replacement rate of resource units U ₂₀ : Interactions among resource units ** U ₂₁ : Economic value U ₂₂ : Number of units U ₂₃ : Disturbance characteristics U ₂₄ : Spatial & temporal distribution
Set of actions related to the Governance Systems (G) U ₂₅ : Policy type U ₂₆ : Geographic scale of governance system * U ₂₇ : Socio-economic attributes * U ₂₈ : Propriety of participation modalities ** U ₂₉ : Incentive type (individualistic, community-oriented) * U ₃₀ : Localism * U ₃₁ : Rule-making organizations U ₃₂ : Institutional culture U ₃₃ : Property rights systems (relations among people in relation to resource units and infrastructure) * U ₃₄ : Preparation of cultural knowledge, beliefs, norms, practices (integrated with law and customs) * U ₃₅ : Network structure (connections among the rule-making organizations and the population subject to these rules) ** U ₃₆ : Historical continuity of the governance system (does it keep being open to close to internal adaptation) *	Set of actions related to the Actors (A) U ₃₇ : Number of relevant actors * U ₃₈ : Socio-economic attributes * U ₃₉ : History of experience ** U ₄₀ : Location * U ₄₁ : Leadership/entrepreneurship * U ₄₂ : Norms (team-ethically), social capital * U ₄₃ : Knowledge of SES / mental models / beliefs * U ₄₄ : Propriety of resource dependent access * U ₄₅ : Technological assistance *
Set of actions related to the Interactions (I) U ₄₆ : Harvesting (using resource units by direct users) U ₄₇ : Information sharing among actors ** U ₄₈ : Collaboration process ** U ₄₉ : Conflict among actors ** U ₅₀ : Investment activities ** U ₅₁ : Lobbying activities ** U ₅₂ : Self-organizing activities ** U ₅₃ : Monitoring activities ** U ₅₄ : Maintaining activities ** U ₅₅ : Evaluation activities **	Set of actions related to the Governance (G) U ₅₆ : Social performance measures (e.g. efficiency, equity, accountability, sustainability) ** U ₅₇ : Geopolitical performance measures (e.g. environmental, resilience, robustness, sustainability) ** U ₅₈ : Expenditures to other SES *



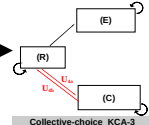
Collective-choice KCA-1



$$U^{KCA:1} : u_{1a}(R) \circ (u_{6b} + u_{5a})$$

$$U^{KCA:1} = \{U^{KCA:1-1}, U^{KCA:1-2}, U^{KCA:1-3}\}$$

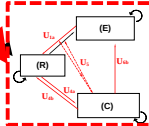
Collective-choice KCA-2



$$U^{KCA:2} : u_{1a}(R) + u_{4b} \circ u_{4a}$$

$$U^{KCA:2} = \{U^{KCA:2-1}, U^{KCA:2-2}, U^{KCA:2-3}\}$$

Collective-choice KCA-3

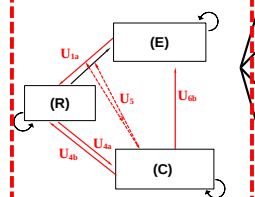


$$U^{KCA:3} : u_{1a}(R) \circ (u_{6b} + u_{5a}) + u_{4b} \circ u_{4a}$$

$$U^{KCA:3} = \{U^{KCA:3-1}, U^{KCA:3-2}, U^{KCA:3-3}\}$$

$U^{OCA} = \{U^{OCA:1}, U^{OCA:2}\} \in U^{KCA:3}$
 $U^{OCA:1} = \{U^{OCA:1-1}, U^{OCA:1-2}\}$
 $U^{OCA:2} = \{U^{OCA:2-1}, U^{OCA:2-2}\}$

Collective-choice KCA-3



U_{1a}: Exploit



$$\rightarrow U_{1a} = \{=[0.1 - 0.5], \quad = [0.5 - 0.9]\}$$

U_{5a}: Regulate access



$$\rightarrow U_{5a} = \{\leq -0.05, \quad \leq -0.4\}$$

U_{4b}: Replant for conservation



$$\rightarrow U_{4b} = \{=-0.2, \quad = [0.3 - 0.4]\}$$

U_{4a}: Monitor for conservation



$$\rightarrow U_{4a} = \{= 0.1, \quad \geq 0.5\}$$

OCA-1 OCA-2

$\frac{dR}{dt}$	Natural EX Growth	Impact of SES Settings	ES Externality	
$\frac{dR}{dt}$	$\pm \overline{U_{1a}} \cdot R$	$\pm \overline{U_{1b}} \cdot R$	$\pm \overline{U_{1c}} \cdot R$	(1a)
$\frac{dE}{dt}$	$\pm \overline{U_{2a}} \cdot R \cdot E$	$\pm \overline{U_{2b}} \cdot R \cdot E$	$\pm \overline{U_{2c}} \cdot R \cdot E$	(1b)
$\frac{dC}{dt}$	$\pm \overline{U_{3a}} \cdot R \cdot E$	$\pm \overline{U_{3b}} \cdot R \cdot E$	$\pm \overline{U_{3c}} \cdot R \cdot E$	(1c)
$\frac{dP}{dt}$	$\pm \overline{U_{4a}} \cdot P$	$\pm \overline{U_{4b}} \cdot P$	$\pm \overline{U_{4c}} \cdot P$	(1d)

Formal definition of DAPP maps deriving from Ostrom & viability theories

Nested conditions (actions, time, states):

- Set of actions: $\mathbf{U} = \{\mathbf{U}^{CCA}, \mathbf{U}^{KCA}, \mathbf{U}^{OCA}\}_1$
- Set of constitutional actions: $\mathbf{U}^{CCA} = \{U^{CCA_1}, U^{CCA_2}, \dots, U^{CCA_{i1}}, \dots, U^{CCA_{m1}}\}_1$
- Set of collective actions: $\mathbf{U}^{KCA} = \{U^{KCA_1}, U^{KCA_2}, \dots, U^{KCA_{i2}}, \dots, U^{KCA_{m2}}\}_1$
- Set of operational actions: $\mathbf{U}^{OCA} = \{U^{OCA_1}, U^{OCA_2}, \dots, U^{OCA_{i3}}, \dots, U^{OCA_{m3}}\}_1$
- Time sequence: $T = \{t_0, t_1, \dots, t_j, \dots, t_n\}$
- Set of states: $X = \{R, E, C, P\}$
- Set of Resource states: $R = \{R_1, R_2, \dots, R_{l1}\}$
- Set of exploitation role states: $E = \{E_1, E_2, \dots, E_{l2}\}$
- Set of conservation role states: $C = \{C_1, C_2, \dots, C_{l2}\}$
- Set of policy-making role states: $P = \{P_1, P_2, \dots, P_{l3}\}$

A nested viable DAPP (nested viable control pathway):

$$\begin{aligned}
 u_K(\cdot) = & u_{OCA}(u_{KCA}(u_{CCA}(t_0))), u_{OCA}(u_{KCA}(u_{CCA}(t_1))), \dots, \\
 & u_{OCA}(u_{KCA}(u_{CCA}(t_j))), \dots, u_{OCA}(u_{KCA}(u_{CCA}(t_n))) \\
 & \text{such that } u(t_j) \in (\mathbf{U}_K(t_j) \forall j) \in \mathbf{U}
 \end{aligned} \tag{38}$$

- (1) Nested governance (IAD framework)
- (2) Polycentric (CIS framework)
- (3) Multi-tier (SES framework)
- (4) Viable

Nested regulatory Map [\(Aubin et al. 2011\)](#) [Definition 2.9.4 p.73]:

$$\mathcal{R}(x) = \left\{ u \in U^{OCA} \in U^{KCA} \in U^{CCA} \in U(x) \mid x \in K, f(x, u(x)) \in Viab_K \right\} \tag{39}$$

Nested viable DAPP map (nested graph):

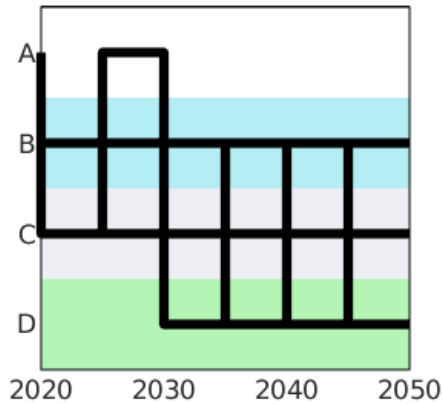
- General DAPP Graph: $\mathcal{G} = V \times E$ with $dim(\mathcal{G}) = U^T$
- CCA level: $\mathcal{G}^{CCA} = V^{CCA} \times E^{CCA}$ with $dim(\mathcal{G}^{CCA}) = (U^{CCA})^T$
- KCA level: $\mathcal{G}^{KCA} = V^{KCA} \times E^{KCA}$ with $dim(\mathcal{G}^{KCA}) = (U^{CCA} \times U^{KCA})^T$
- OCA level: $\mathcal{G}^{OCA} = V^{OCA} \times E^{OCA}$ with $dim(\mathcal{G}^{OCA}) = (U^{CCA} \times U^{KCA} \times U^{OCA})^T$

- Vertex $V \rightarrow U \times T$ representing decision nodes at time t_0, t_1, \dots, t_T for every possible action u , such that $V = \bigcup_{t=0}^T U(x(t))$
- Edges $E = e_{ij} \subseteq V \times V$ representing possible viable transition pathways between decision nodes, which correspond to viable state transitions under control $u(t)$, such that: $E = \{u(t), u(t+1) \mid u(t) \in \mathcal{R}(x(t), u(t)), u(t+1) \in \mathcal{R}(x(t+1), u(t+1))\}$

Nested DAPP maps

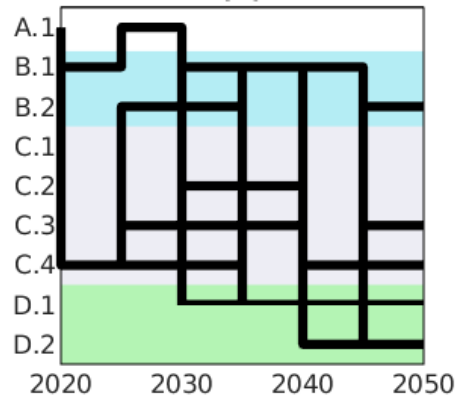
Adaptation of Constitutional → Operational arrangements

Viable DAPP map
Constitutional level



$$U_{CCA} = \{U_{CCA-A}, U_{CCA-B}, U_{CCA-C}, U_{CCA-D}\}$$

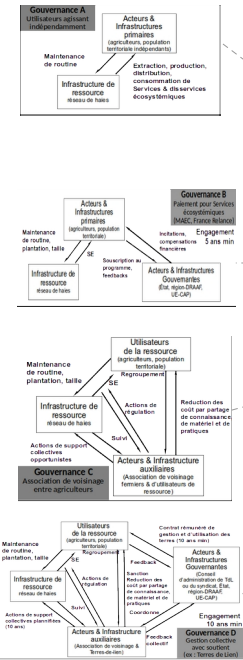
Viable DAPP map
Collective level



$$U_{KCA} = \{U_{KCA-1}, U_{KCA-2}, U_{KCA-3}\} \in U_{CCA-3}$$

Viable DAPP map
Operational level

$$U_{OCA} = \{U_{OCA-1}, U_{OCA-2}\} \in U_{KCA-3}$$

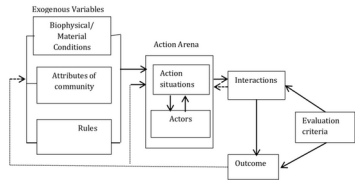


Daily constraints, costs, benefits

Nested institutional level of adaptation

SES targets of adaptation

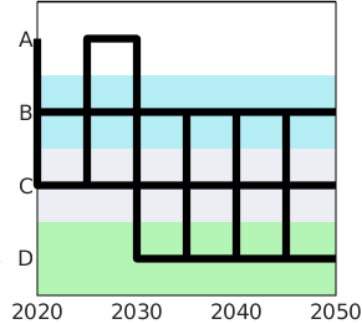
Roles: who? How? how much?



Gouvernance A (Infrastructure nationale)	
1. Maintien de la routine	2. Adaptation des infrastructures existantes
3. Développement de nouvelles infrastructures	4. Renforcement des capacités institutionnelles
5. Amélioration de la gouvernance	6. Renforcement des capacités individuelles
7. Développement de nouvelles infrastructures	8. Renforcement des capacités institutionnelles
9. Amélioration de la gouvernance	10. Renforcement des capacités individuelles



DAPP Control Map (Γ_K)



Practice



Theory

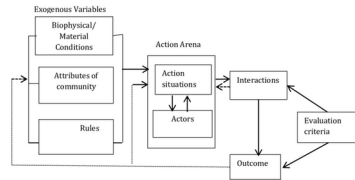
Bridge

Daily constraints, costs, benefits

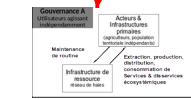
Nested institutional level of adaptation

SES targets of adaptation

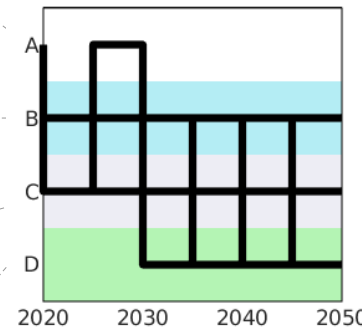
Roles: who? How? how much?



Description des variables de l'ETP (voir annexes basées sur les travaux de l'Institut de Recherche pour le Développement (IRD))	
Etat des ressources	Etat des ressources (niveau de stock, état de santé, etc.)
Etat des institutions	Etat des institutions (niveau de confiance, état de santé, etc.)
Etat des acteurs	Etat des acteurs (niveau de connaissance, état de santé, etc.)
Etat des interactions	Etat des interactions (niveau de coopération, état de santé, etc.)
Etat des résultats	Etat des résultats (niveau de production, état de santé, etc.)

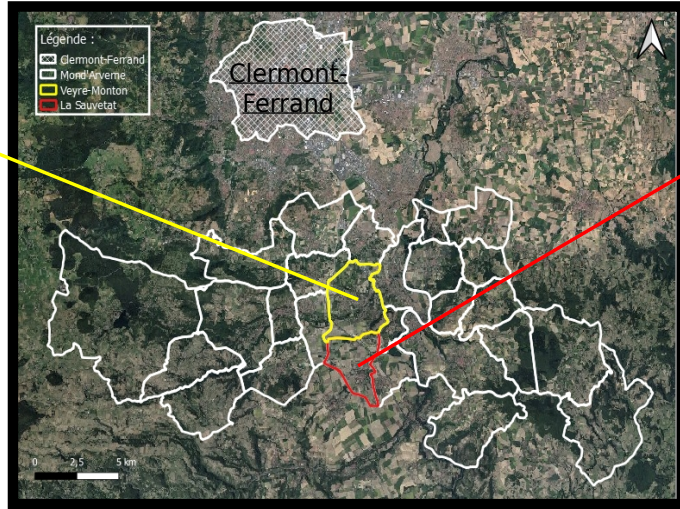
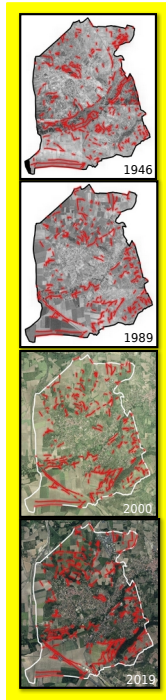


DAPP Control Map (Γκ)

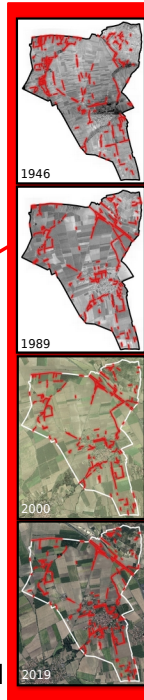


Application example

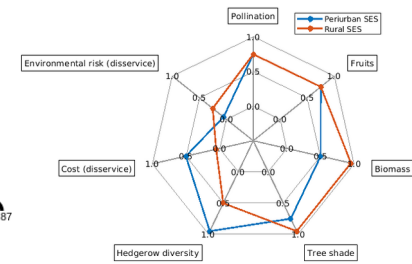
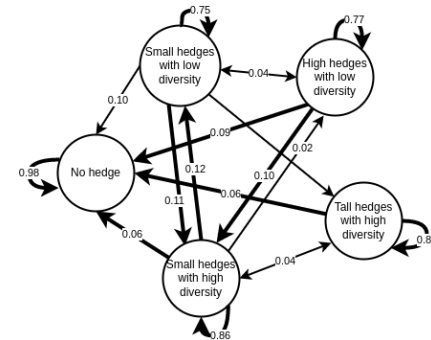
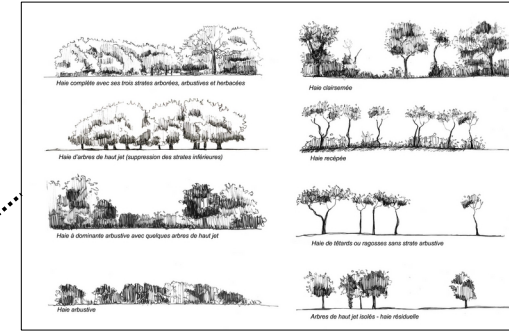
Rural & Peri-urban SES in France



Péri-urbain



Rural



Constitutional-Choice arrangements (CCA)			Associated Collective-Choice Arrangements (KCA)			Consequences on the operational choice arrangement (OCA) for the EAI: proportion of every type of action for link 1a			Effect of the OCA on the resource infrastructure (0a)	Relative cost reduction provided by the KCA to compensate the disservice cost of management (hedgerows).
Name	Description	Minimal duration	#	objectives	Method (chain of collective actions) to achieve the objective	No maintenance	Hedge-cutting (tractor mounted)	Integrative soft management		
(A) Private arrangement	Individualistic social organization (current dominant practice): no incentives or collective actions to support the hedgerow network or regulate actions. Most common practice is trimming. We assume that this action is included in the SES that was observed during the 1989-2019 period.	no	A1	Collective-choice arrangement for baseline monitoring and range of operational actions	#NA	0.2	0.6	0.2	Business-as-usual dynamics (#NA)	0%
(B) Joint Private-Public arrangement	Social organization and infrastructures around state-controlled scheme for the payments for ecosystem services (PES): The state pay farmers who enter a PES scheme, under the condition that they maintain hedgerows and associated ES	5 years	B1	Compulsory planting of species-rich hedgerows to increase public & common-good ES	2b → 1a → 0a → 1b	0.2	0.6	0.2	More planting of species-rich hedgerows: Tall +5%, Short +5%	-10%
			B2	Compulsory planting of species-rich hedgerows under integrated soft management (constrain the on tractor hedge-cutting use) to protect public & common-good ES	2b->1a->0a-->1b	0.2	0.4	0.4	#NA	0%
(C) Joint Private-Community arrangement	Social organization and infrastructures around the support and regulation of the hedgerow network, ecosystem services and exploiting actors: Neighboring farmers enter joint private-community arrangement by forming an auxiliary association (AIA) to set auxiliary practices regarding monitoring, the sharing of material/costs/knowledge, and set operational constrains on PIA appropriation practices (e.g. on planting new hedgerows, tractor hedge-cutting, integrated soft management).	no	C1	Incentives to share material and reduce costs in order to reduce constrains on tractor hedge-cutting	6a-->1a+1b	0.1	0.8	0.1	#NA	-10%
			C2	Regulate the planting to increase poor-species hedgerows in order to increase biomass production	5a->1a->0a->1b	0.2	0.6	0.2	More planting of productive species in species-poor hedgerows: Tall: +5%, Short+5%	0%
			C3	Regulate the use of tractor hedge-cutting + Incentives on the planting of species-rich hedgerows + integrated soft management practices on these hedgerows	5a → 1a → 0a → 1b	0.2	0.4	0.4	More planting of species-rich hedgerows: Tall +5%, Short +5%	0%
			C4	Strongly regulate maintenance activities for reducing costs and increase nature conservation	5a->1a->0a->1b	0.4	0.4	0.2	#NA	0%
(D) Joint-Private-Community-Public arrangement	Social organisation and infrastructure for governing, arbitrating between exploiting and supporting actors and infrastructures: Farmers join organic farming NGO Terre-de-liens (TdL) and the EU-CAP sponsored PES scheme. Farmers lease land to TdL with extra individual regulations and benefits for the management of their own hedgerows. Farmers can join the TdL SAI group that receive funds from TdL to collectively protect the hedgerow network	10 years	D1	Regulate the use of tractor hedge-cutting, set incentives to plant more species-rich hedgerows that require integrated soft management practices	5a → 1a → 0a → 1b	0.2	0.4	0.4	More planting of species-rich hedgerows: Tall +5%, Short +5%	-20%
			D2	Strongly regulate maintenance activities & set cost sharing incentives to increase nature conservation	5a+6b → 1a → 0a → 1b	0.4	0.4	0.2	#NA	-20%

Ecosystem (dis)services (ES)
(i.e. link 1b in the CIS model
from figure 1)

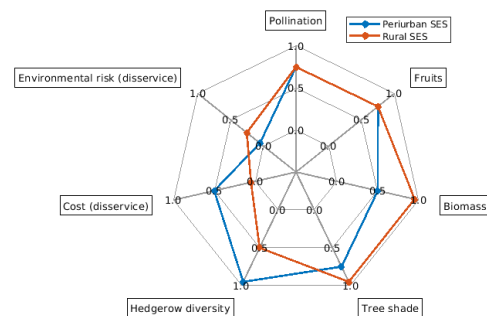
Weighted limits of satisfaction for
every ES deduced from the actors
surveyed in the two SES [0-1]

Relative production of ES by type of hedgerow, on a [0-1] scale,
with 1 corresponding to the observed maximal production or effect
of the ES

Impact of maintenance operational action on ES, on a [0-1]
scale, with 0 corresponding to a total degradation of the ES,
whereas 1 meaning a perfect conservation of the ES.

Quantitative indicator of ecosystem services
(and origin of indicator and measurement)

	Rural SES	(La Peri-urban SES	No	Short hedgerow (SH)		Tall hedgerow (TH)		No maintenance	Hedge-cutting	Integrative soft	
	Sauvetat)	(Veyre-Monton)		hedgerow	Species-poor	Species-rich	Species-poor				
				(PH)	(RH)	(PH)	(RH)		mounted)		
Fruit production	0.9	0.95	0	0.553	1	0.3169	0.9859	0.5	0.25	0.75	Mean number of edible fruits species (based on ecological survey)
Pollination	0.9	0.95	0	0.5204	0.9959	0.2353	1	0.5	0.25	0.75	Mean number of species attracting pollinators (based on ecological survey)
Biomass Production	0.95	0.5	0	0.25	0.25	1	0.75	1	0.5	0.75	Aerial carbon (Open data from Carboceage)
Sunlight Protection	0.95	0.5	0	0.3231	0.3508	0.938	1	0.75	0.25	0.5	Mean height (based on ecological survey)
Landscape aesthetics	0.5	0.95	Aesthetic opinion of actors changes with the diversity of hedgerow present in the landscape.					0.5	0.25	0.75	Shannon index (calculated from the relative proportion of the four hedgerow types present in the landscape, and confronted to opinions of actors based on social survey)
Maintenance cost (social-economic cost)	0.1	0.1	0	0.25	0.25	0.75	1	0	0.5	0.75	Mean annual maintenance cost
Environmental hazards: fire, lateral encumbrance, snag fall, etc ...	0.15	0.2	0	0.25	0.25	0.75	1	1	0.5	0.5	Based on expert knowledge

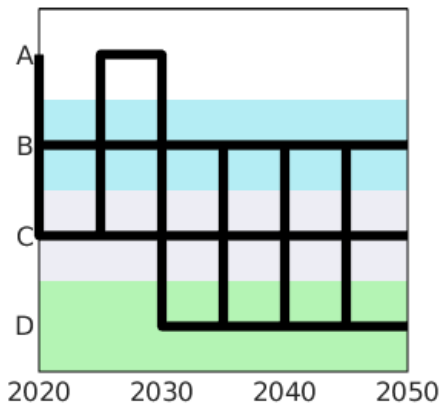




Nested DAPP maps

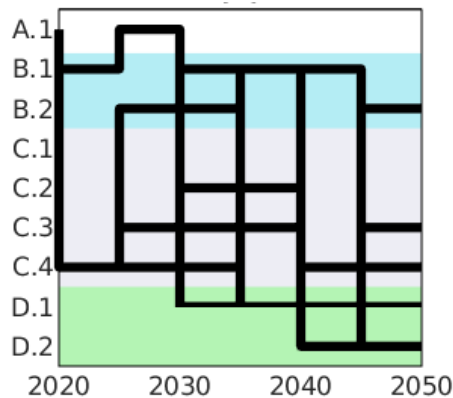
Adaptation of constitutional & Collective choices
(Operational level = fixed)

Viable DAPP map
Constitutional level

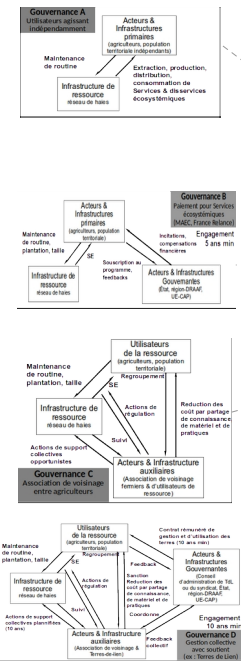


$$U_{CCA} = \{U^{CCA-A}, U^{CCA-B}, U^{CCA-C}, U^{CCA-D}\}$$

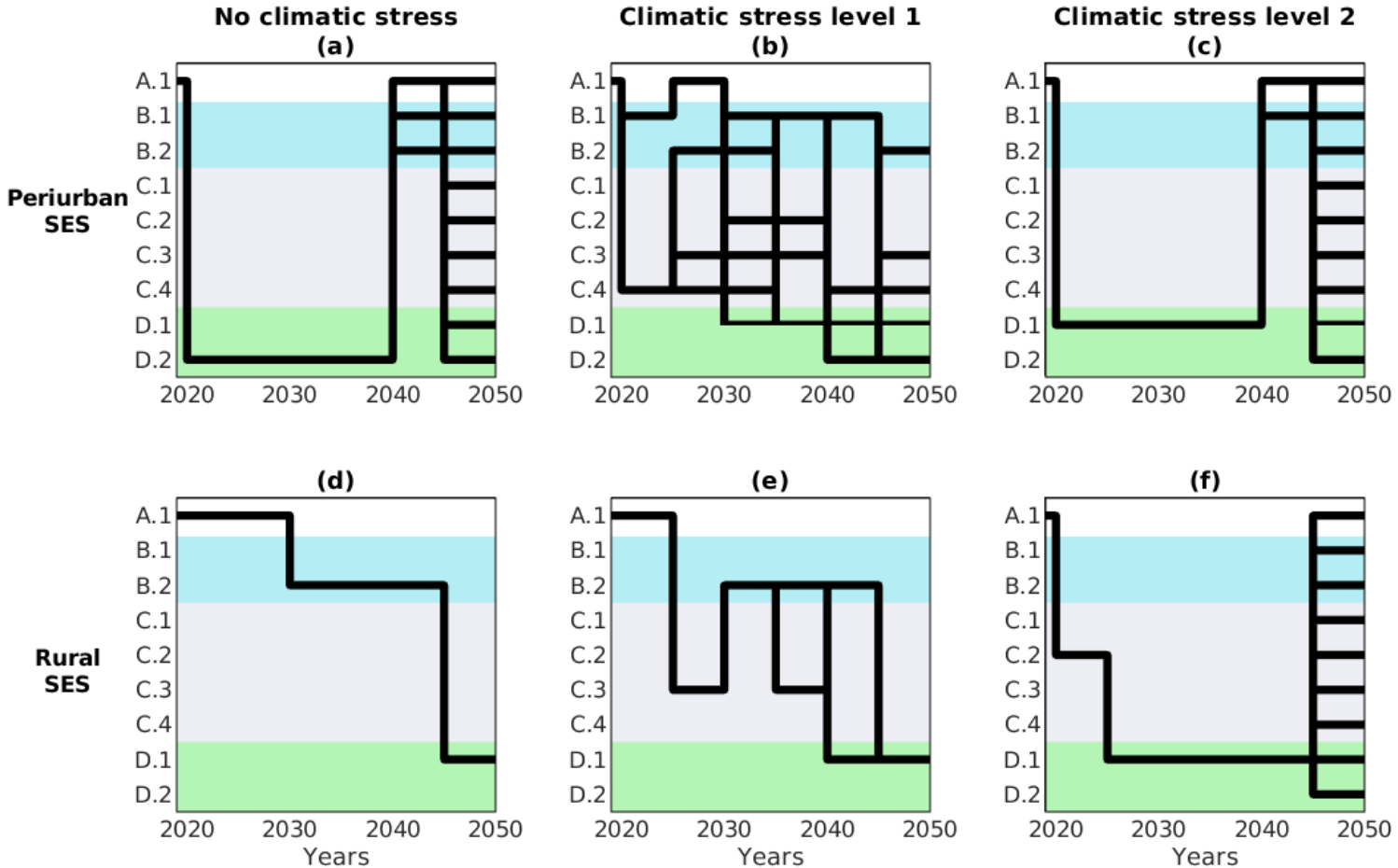
Viable DAPP map
Collective level



$$U_{KCA} = \{U^{KCA-1}, U^{KCA-2}, U^{KCA-3}\} \in U^{CCA-3}$$

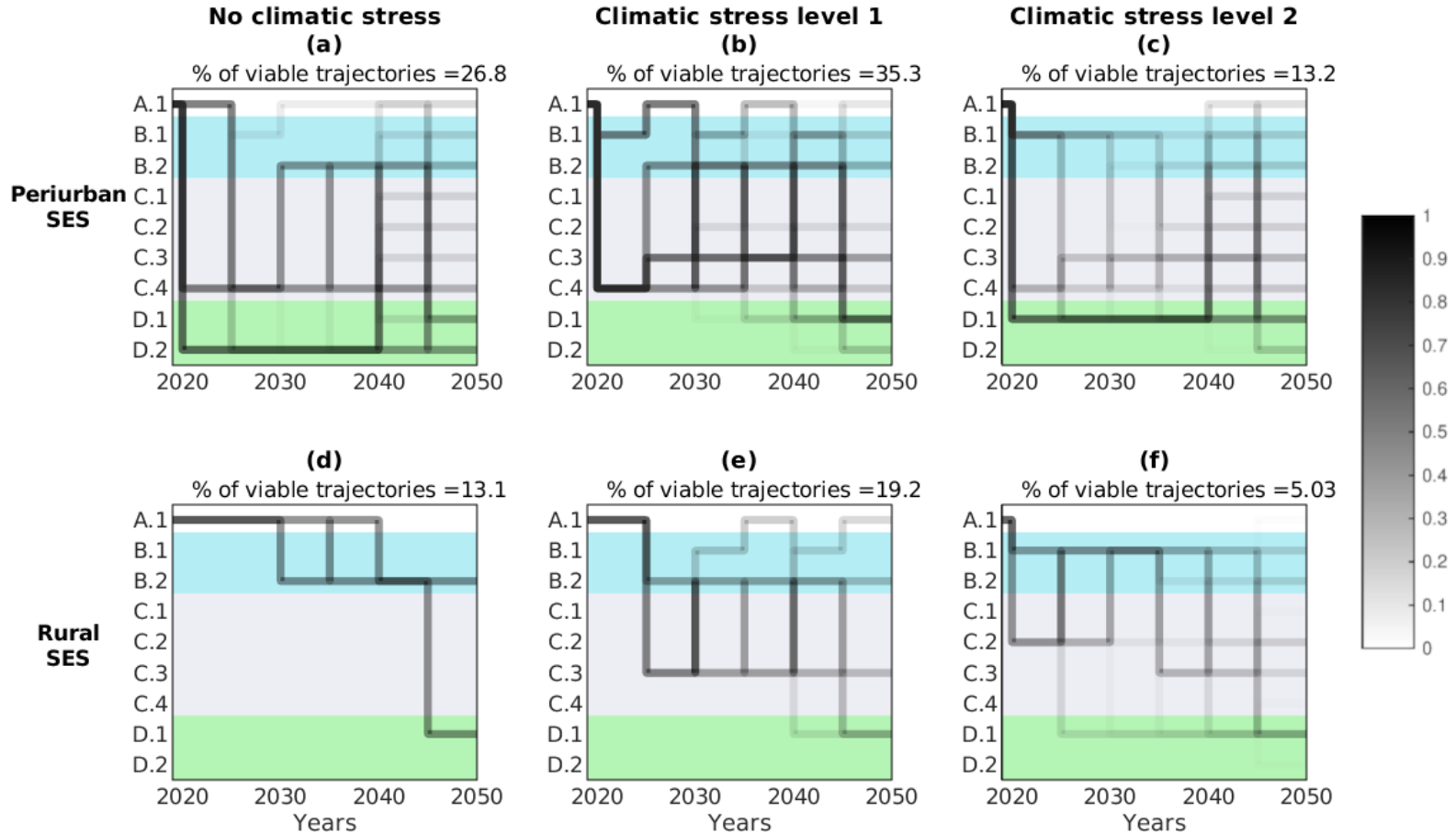


Secured DAPP maps



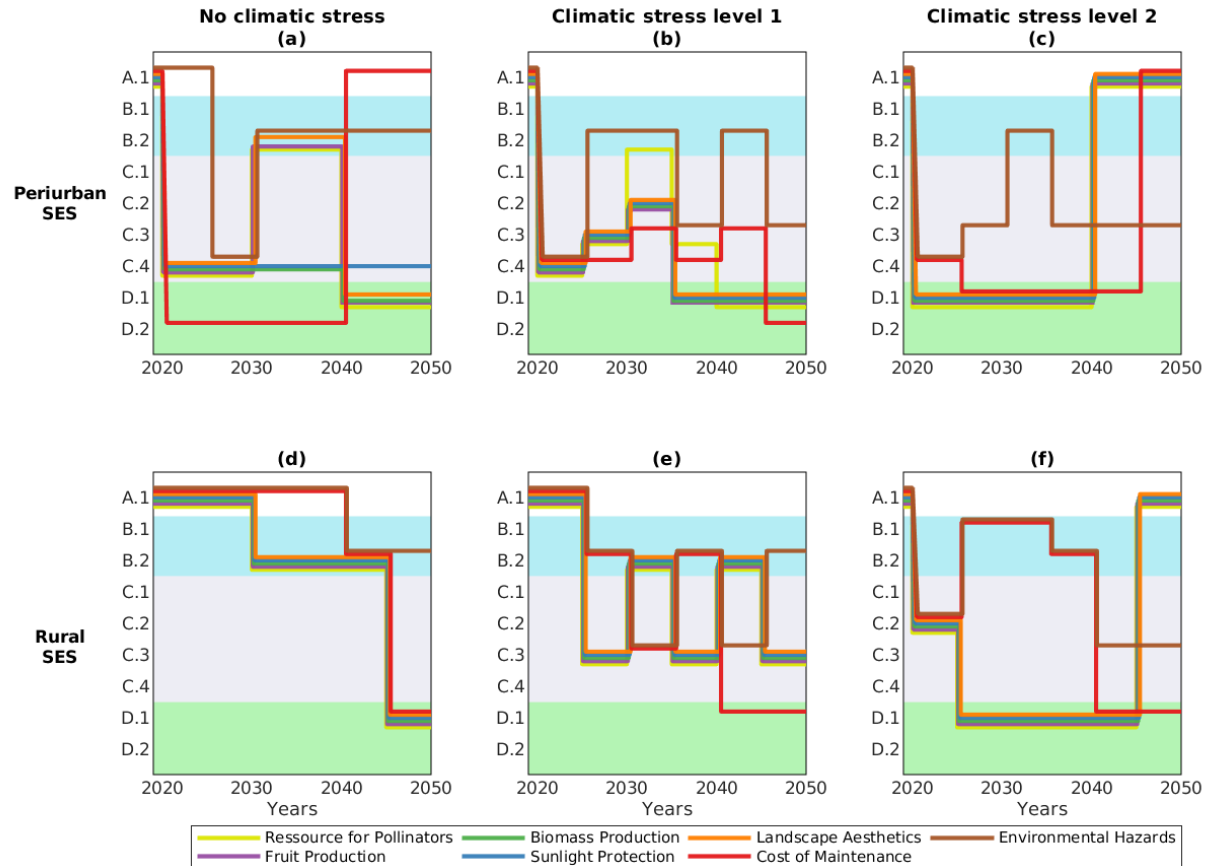
Risk DAPP maps

Pathways that minimize risks of becoming non-viable

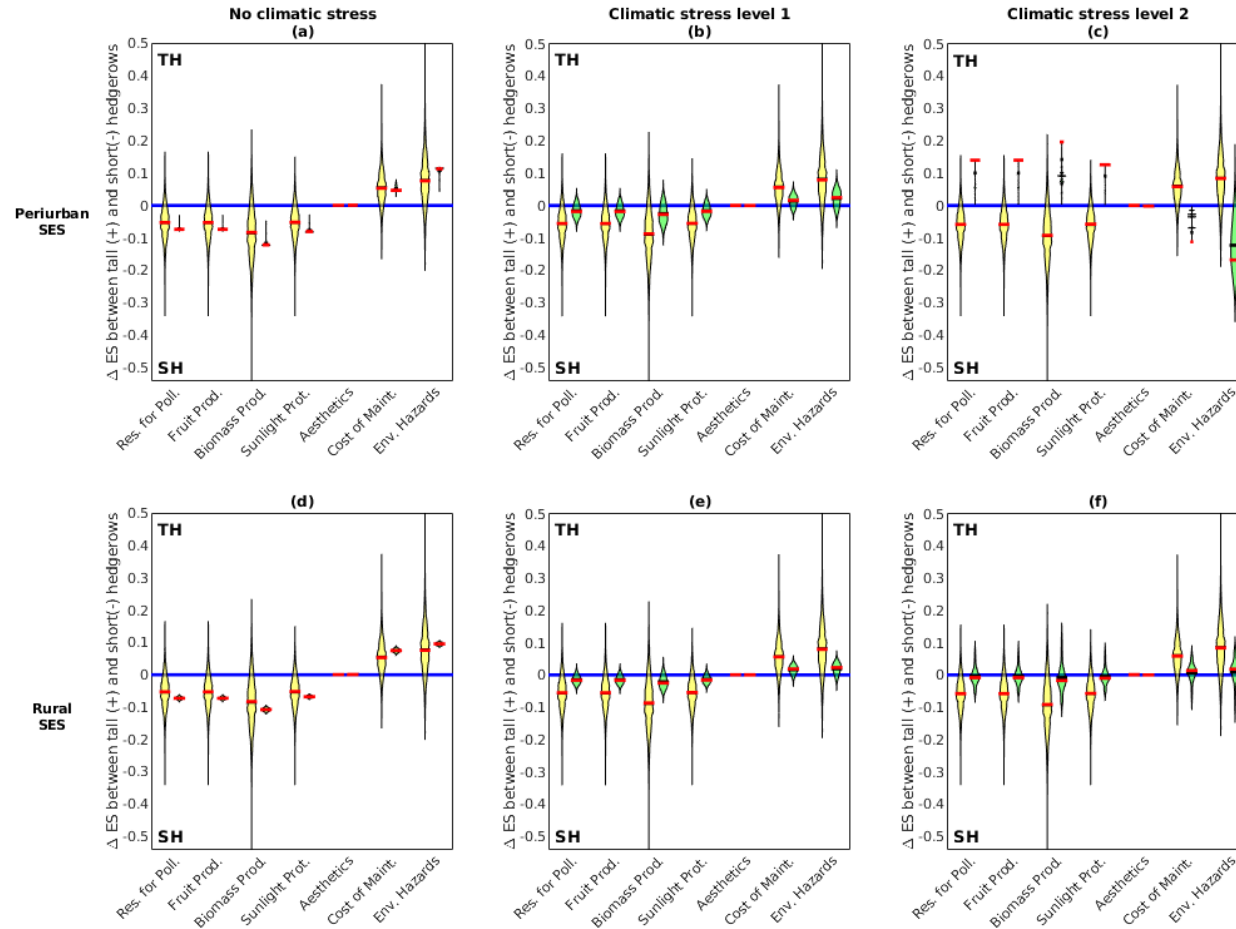


Optimal DAPP maps

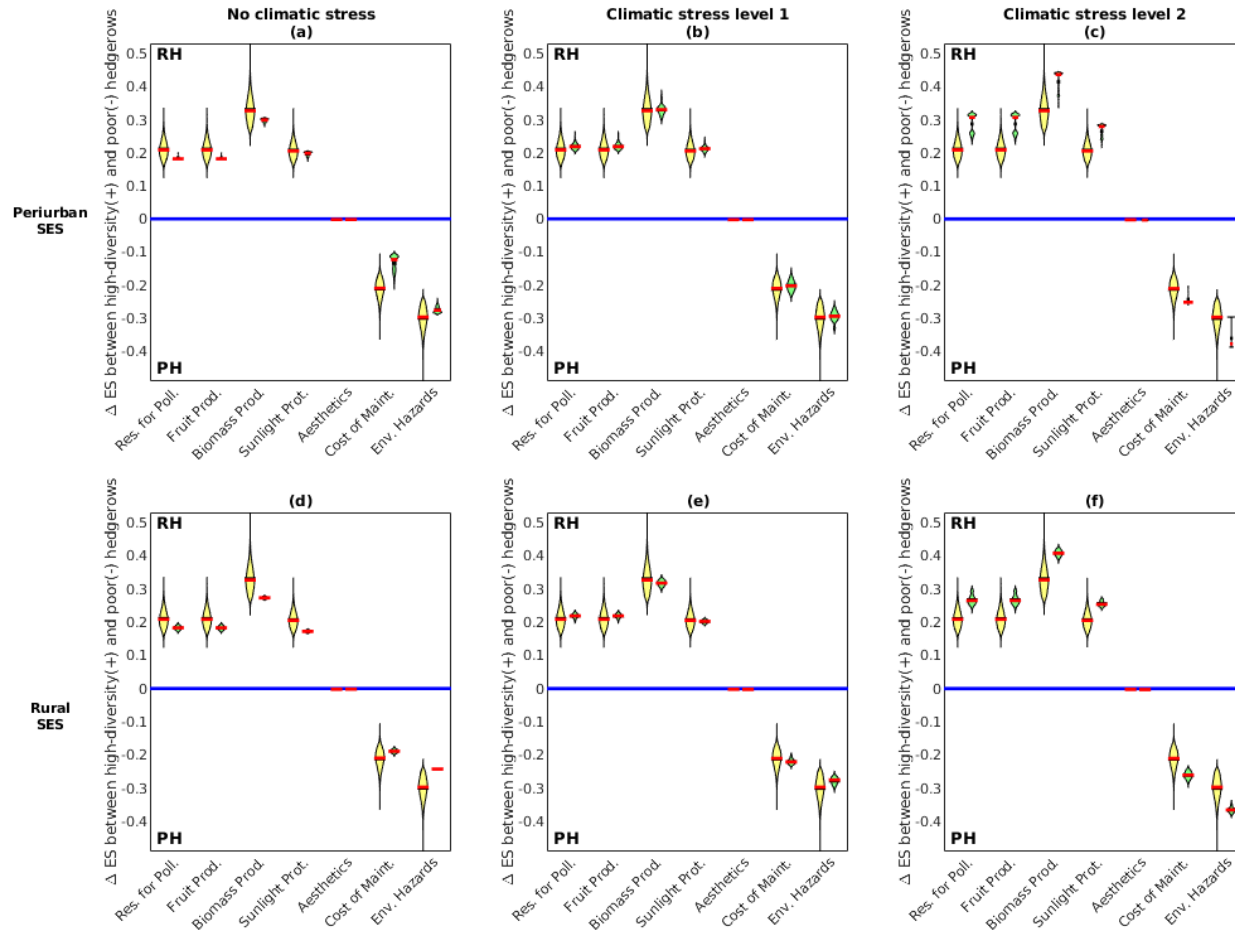
Switching optimization between distinct ecosystem services



Security gains in ES by targeting different hedgerows height



Security gains in ES by targeting different biodiversity levels



Trajectories selection

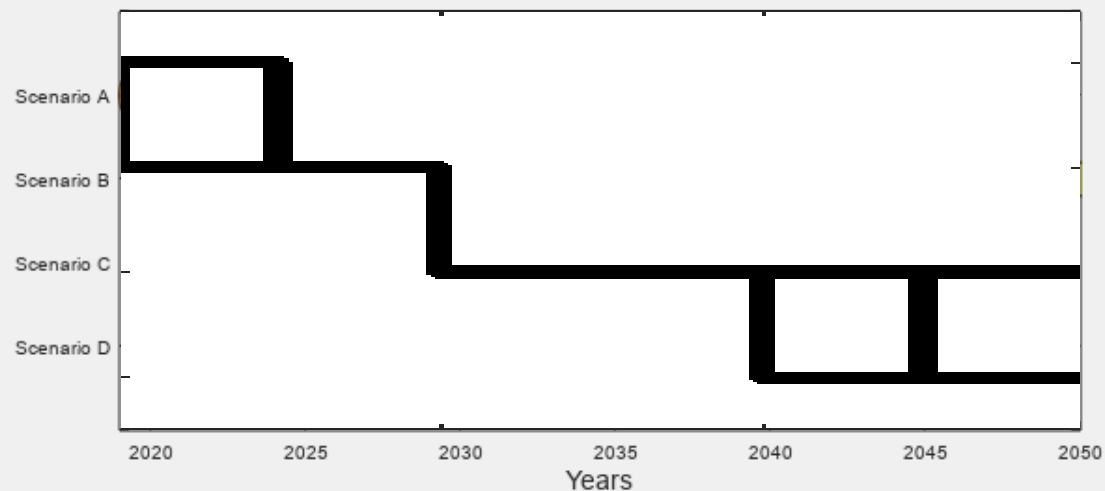
Metric

Initial year = 2019

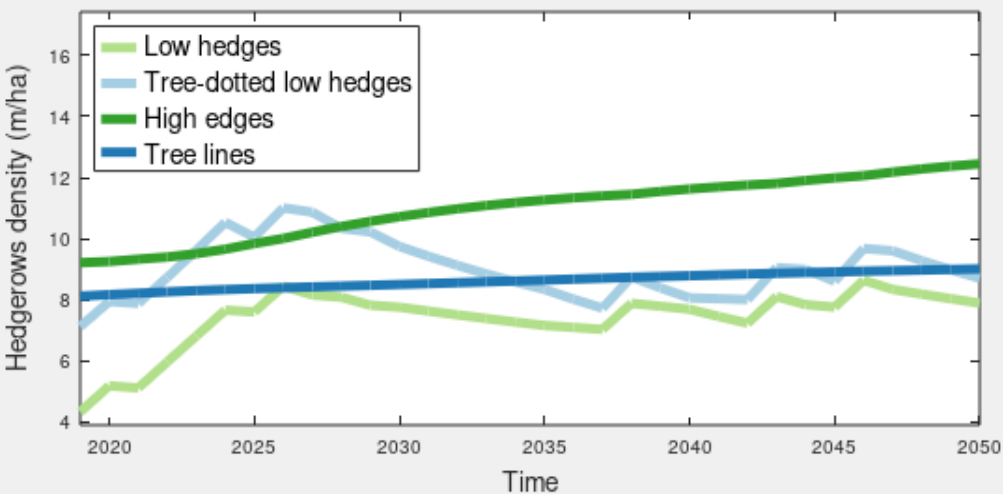
Time horizon = 32

Number of runs = 10000

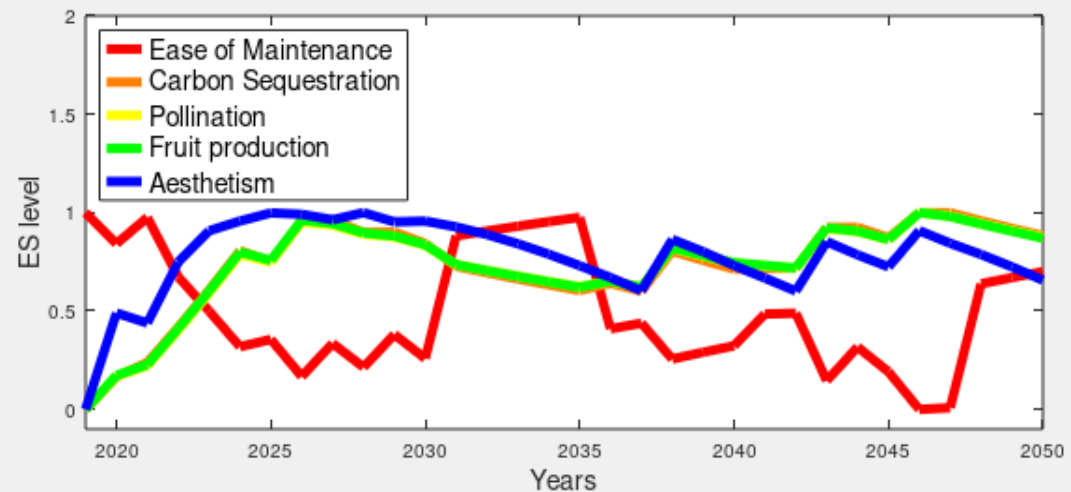
Adaptation pathways



Hedgerow dynamics



Ecosystem services



Load

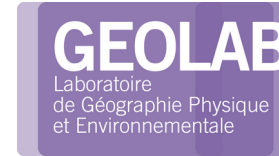
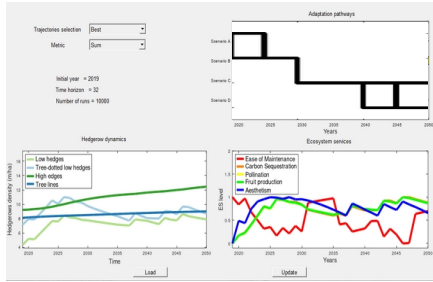
Update

Problem 3

Transform this method
Into a decision support tool ?

Consortium

I-Site : CIR1 :Axe 4 (2024-2025)



Deltares

Areas of expertise Software Academy Facilities About us Contact

Contact

Marjolijn Haasnoot
Climate adaptation



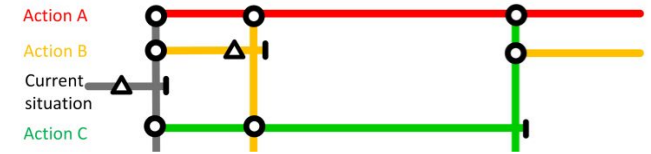
+31(0)88335 77 33 (Deltares
press number)
Marjolijn.Haasnoot@deltares.nl

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Climate Adaptation and Risk
Management



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Dynamic Adaptive Policy Pathways: supporting decision making under uncertainty using Adaptation Tipping Points and Adaptation Pathways in policy analysis



Dynamic Adaptive Policy Pathways

Problem 4

Extend to other case studies

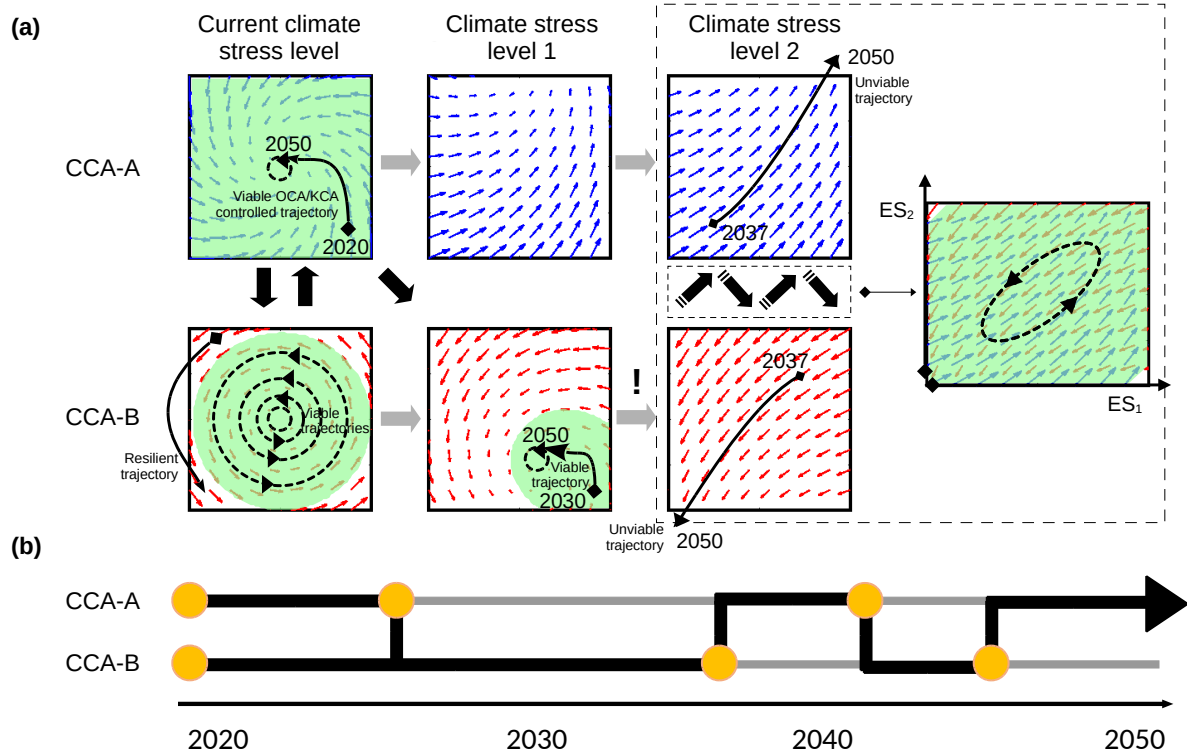
Test universality of this method









UMR
Silva

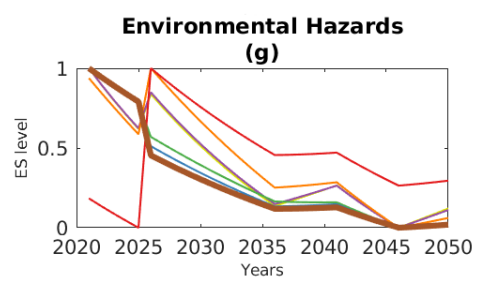
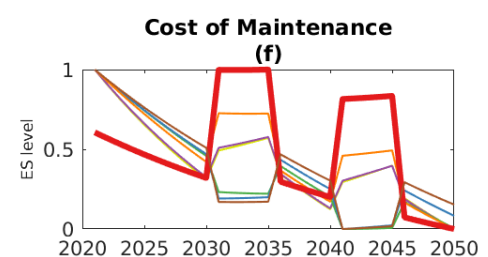
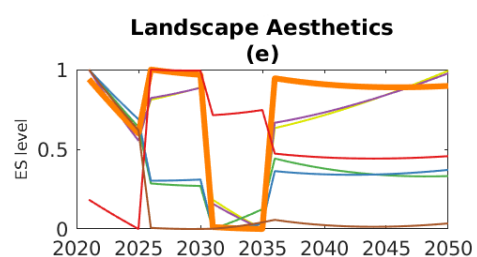
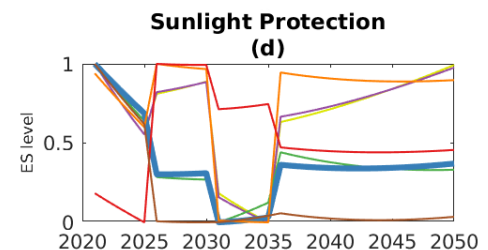
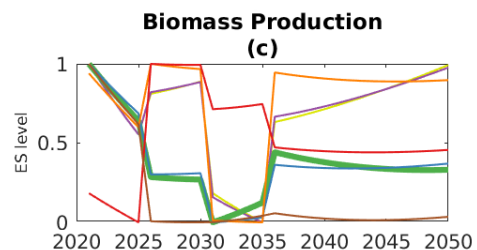
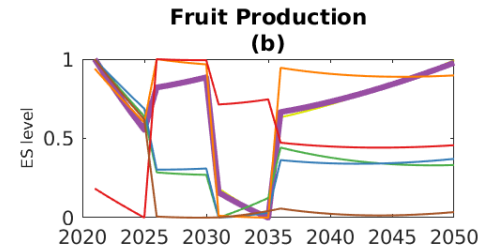
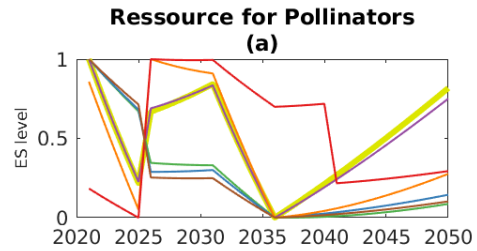
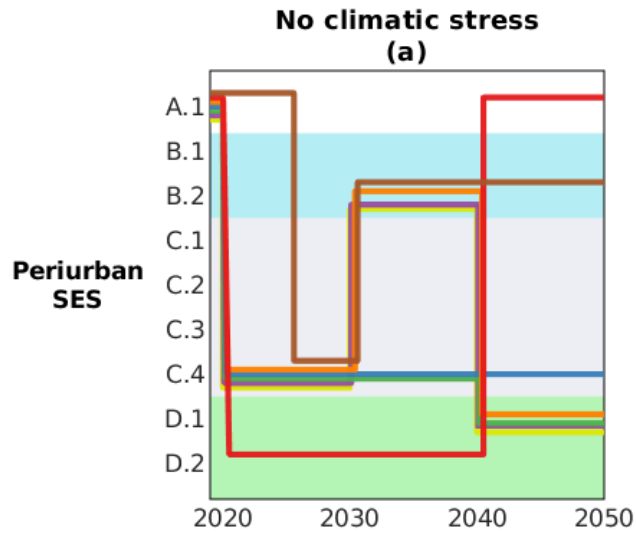


Thank you
Questions ?



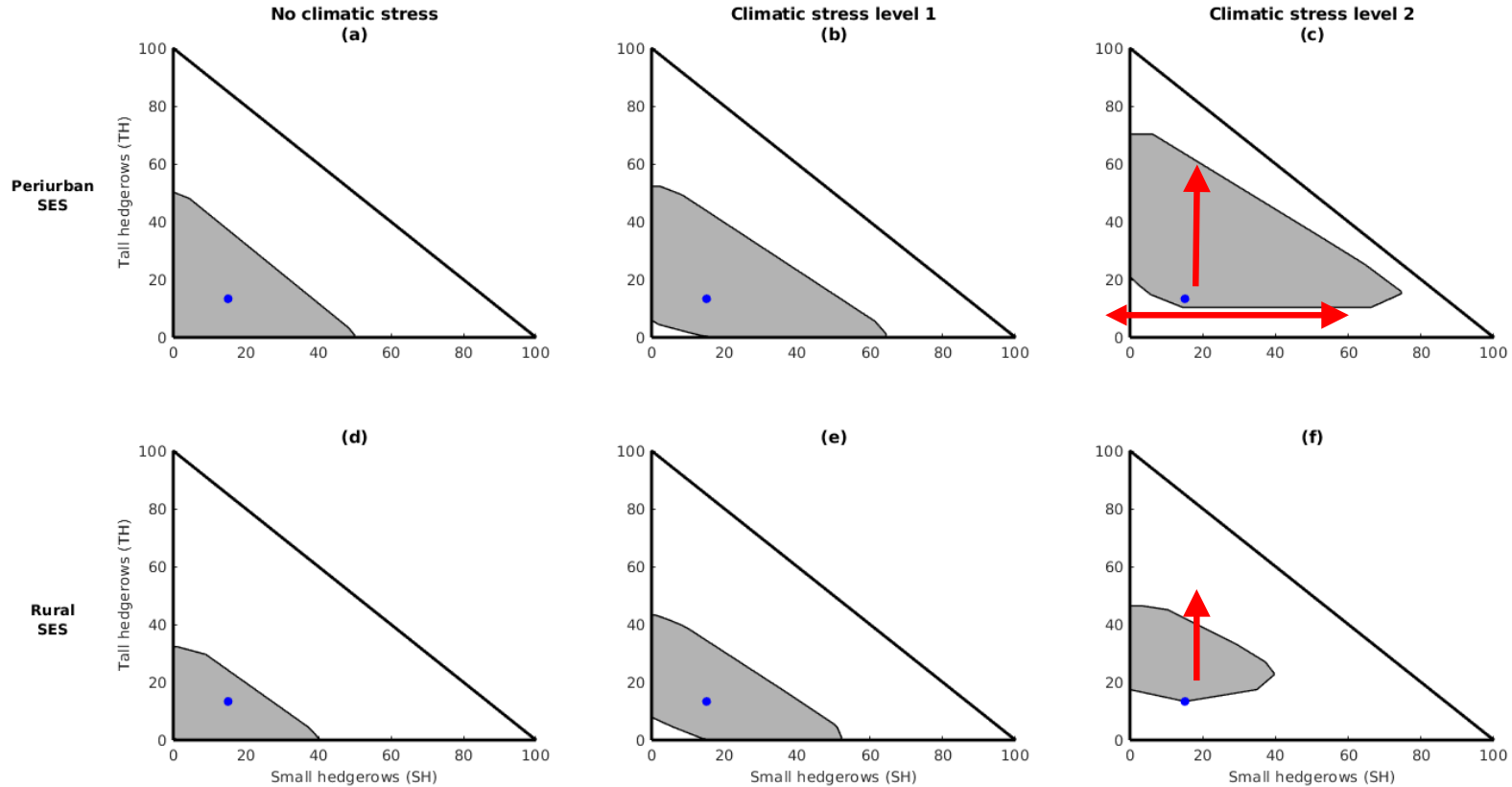
-  Constraining domain of satisfaction K , for two ecosystem services (ES_1 and ES_2). Outside K , the state of the SES is un-viable.
-  Vector field showing the direction of controlled trajectories of the state at time t of the two ES for the SES. The sequence of controls involve a nested set OCA and/or KCA actions for every CCA.
-  Viability kernel $Viab(K)$ where at least one trajectory (controlled by nested OCA/KCA actions) will never leave K . Outside this sub-domain, controlled trajectories can either leave to permanently become non-viable or go back and be considered resilient.
-  Uncontrolled transition and regime shift leading to a change in the size of $Viab(K)$ for the same constitutional change arrangement (CCA)
-  Controlled transitions through adaptation of CCA-A into CCA-B (and vice versa), each possessing unique regime and (null) $Viab(K)$, but leading sequentially to a globally non-null or larger $Viab(K)$
-  Decision node as represented in the DAPP framework, representing the event when actors need to collectively decide whether they want to keep or adapt their CCA in order to stay viable

Résultats supplémentaires



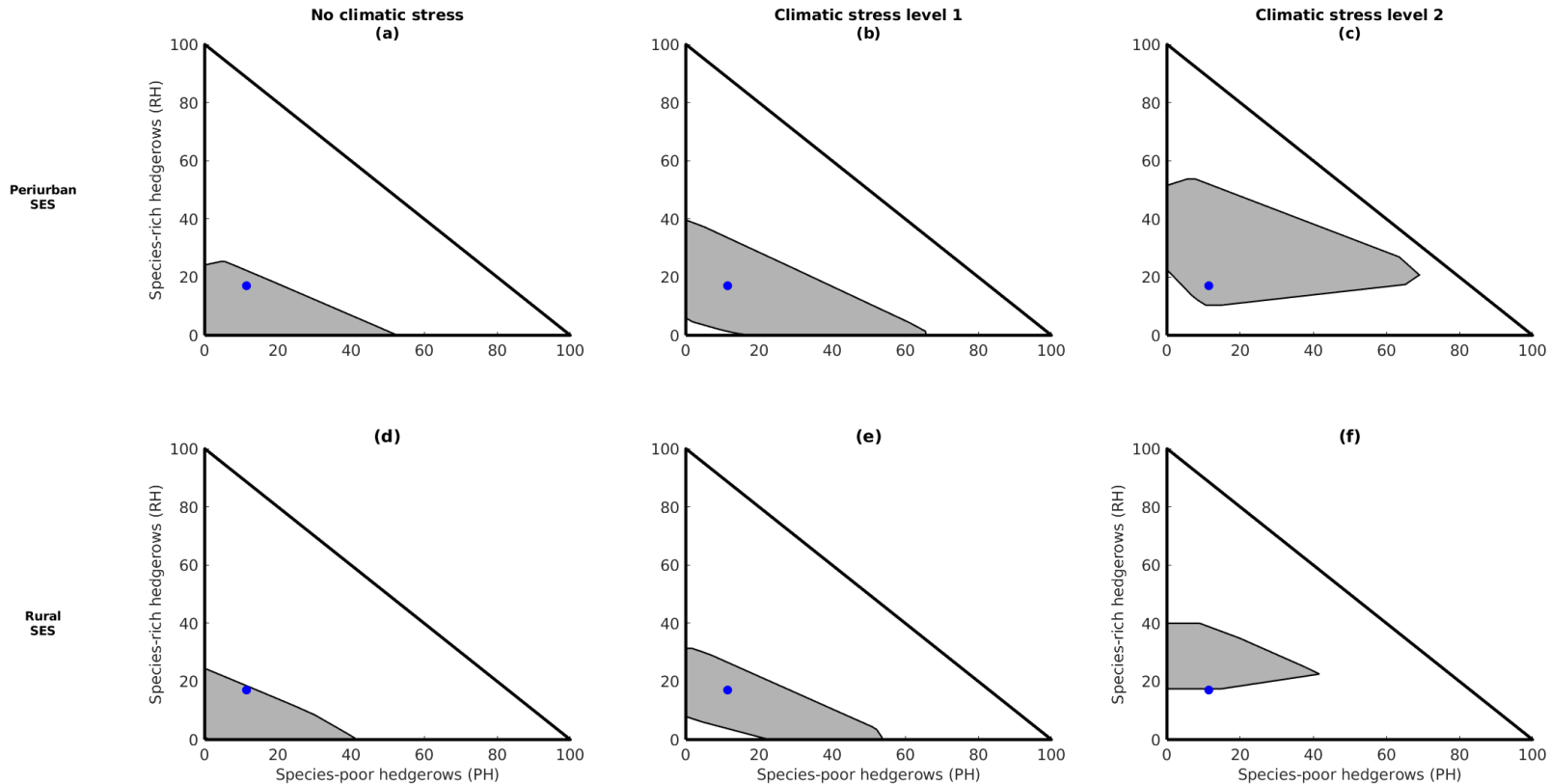
Analyse de viabilité

Coupe en fonction de la taille de haies



Analyse de viabilité

Coupe en fonction de la biodiversité des haies



Evaluer les gains en sécurisation des SE quand on adapte l'action opérationnelle

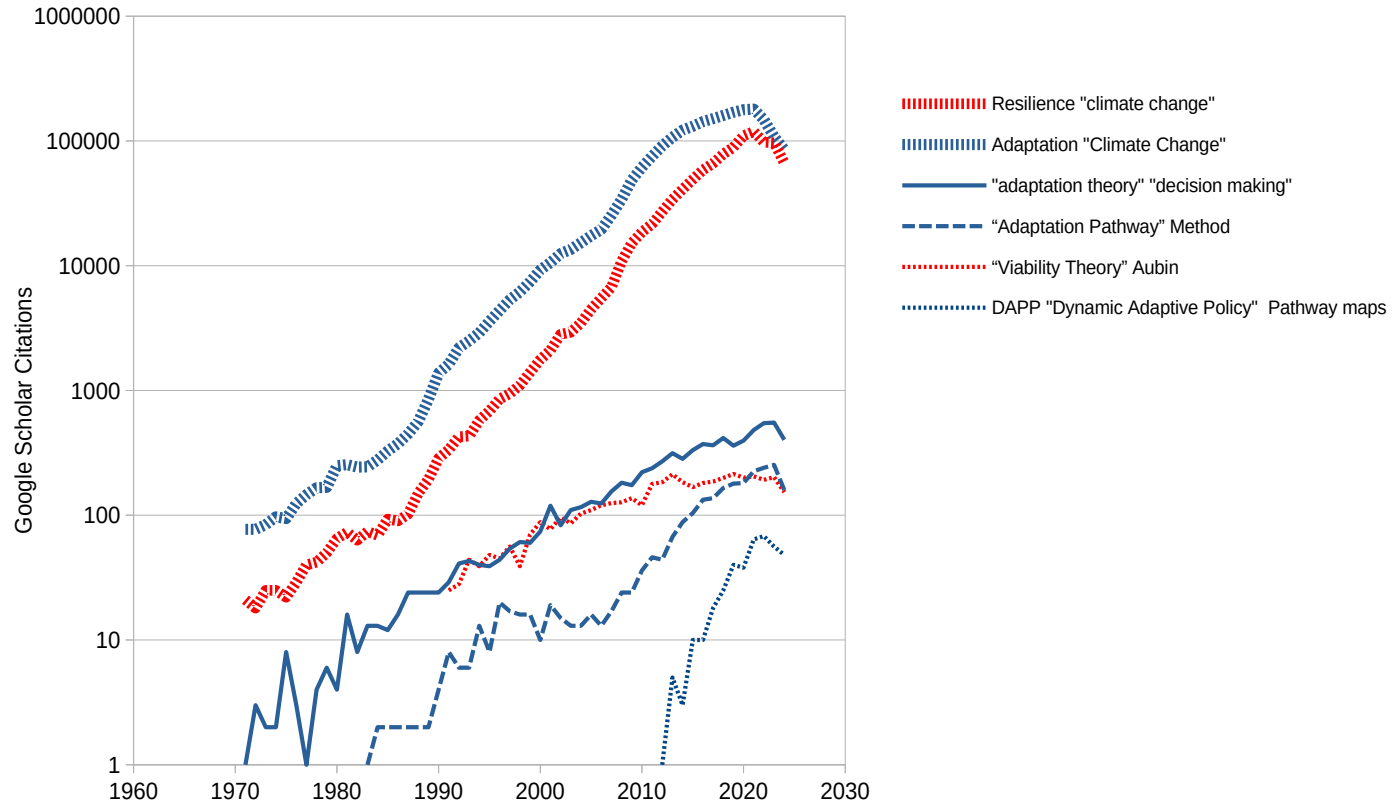
Analyse de sensibilité : changer type de haie

$$\left(\frac{\Delta ES_{TH-SH}}{\Delta a_{OCA}^{TH-SH}(\cdot)} = \Delta ES_{TH-SH} \right)$$

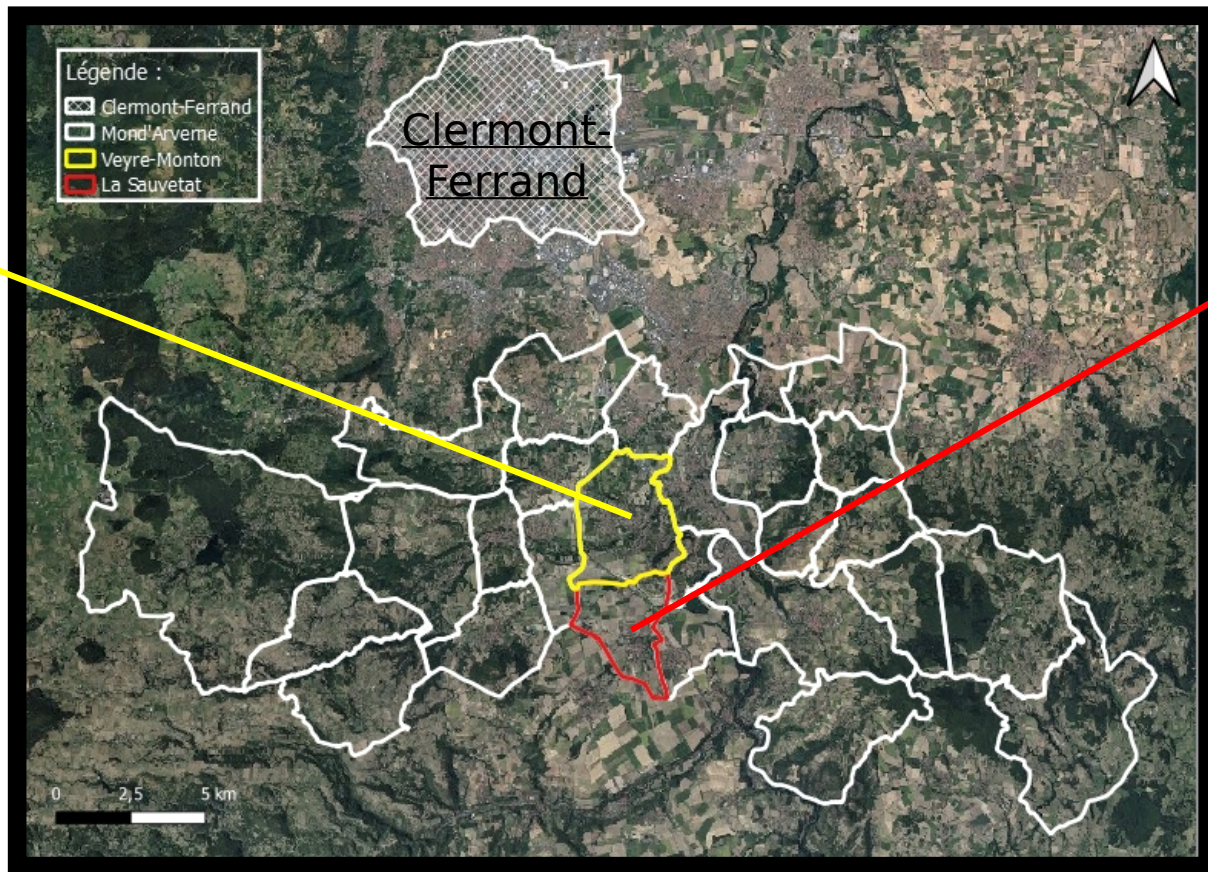
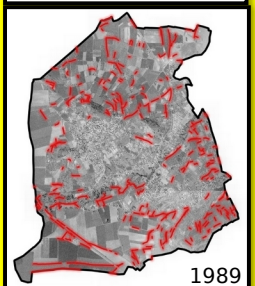
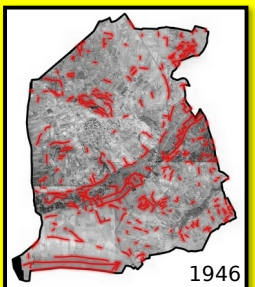
$$\Delta ES_i^{TH} = ES_i(a_{OCA}^{TH}(\cdot)) - ES_{i,min}$$

$$\Delta ES_{TH-SH} = \Delta ES_{TH} - \Delta ES_{SH} = [ES(a_{OCA}^{TH}(\cdot)) - ES_{i,min}] - [ES(a_{OCA}^{SH}(\cdot)) - ES_{i,min}]$$

Resilience (viability) & Adaptation

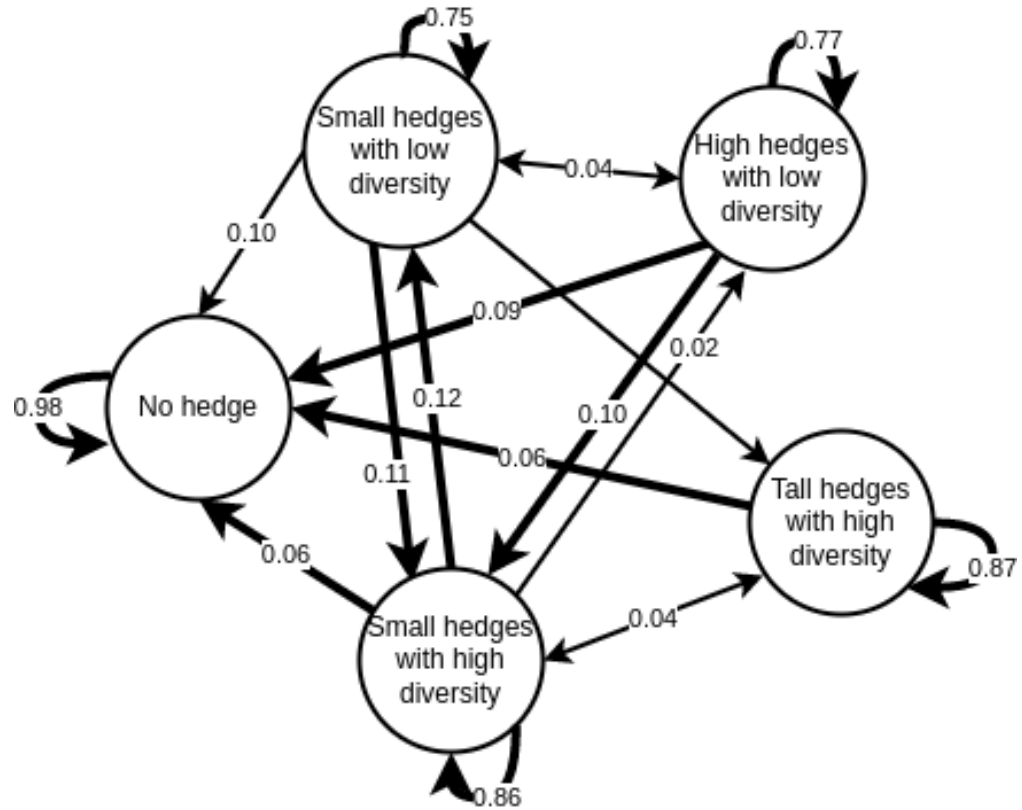


Paramètres du modèle (terrain + entretiens)



Péri-urbain

Rural

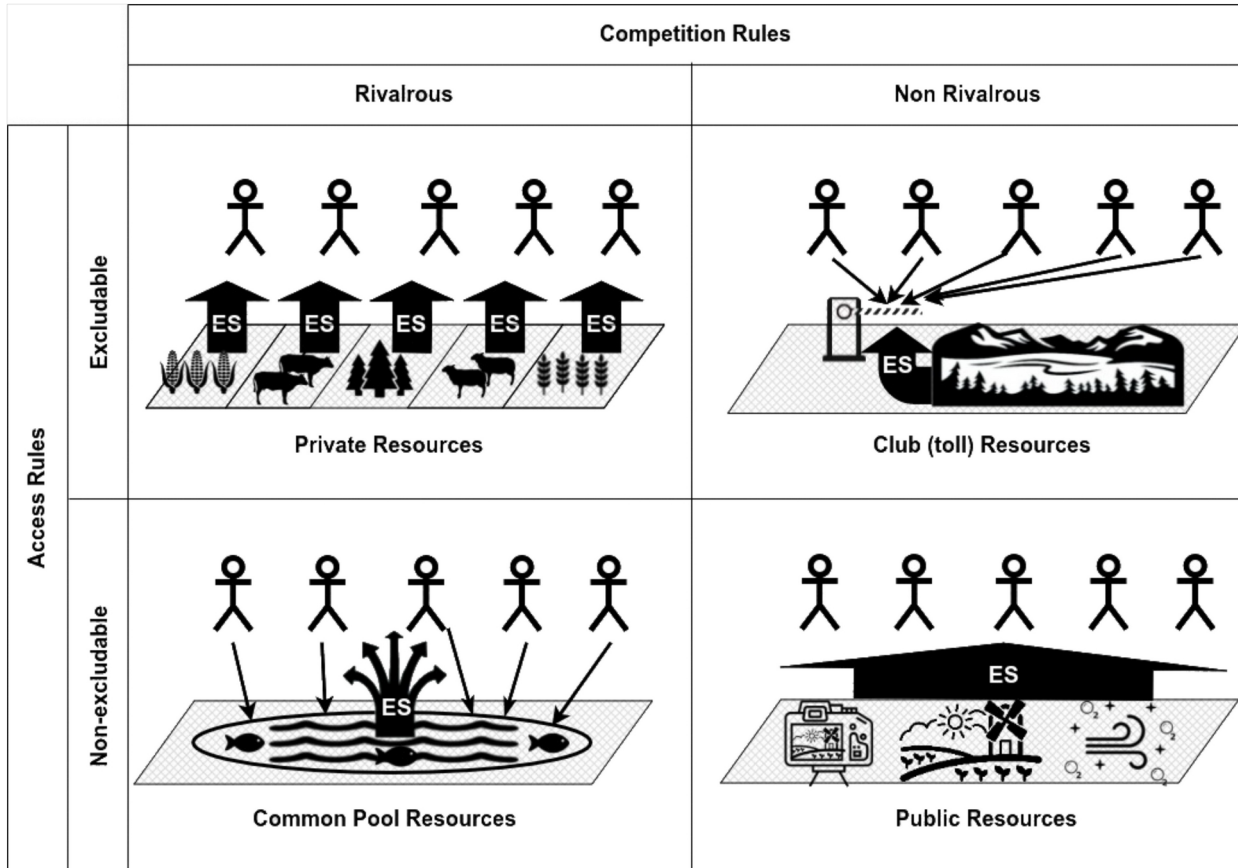


Veyre-Monton

La Sauvetat

Typologie biens & services écosystémiques (théorie économique)

Adaptation depends on type of actors organization around goods and services





Strawberry fields forever !

National Parks



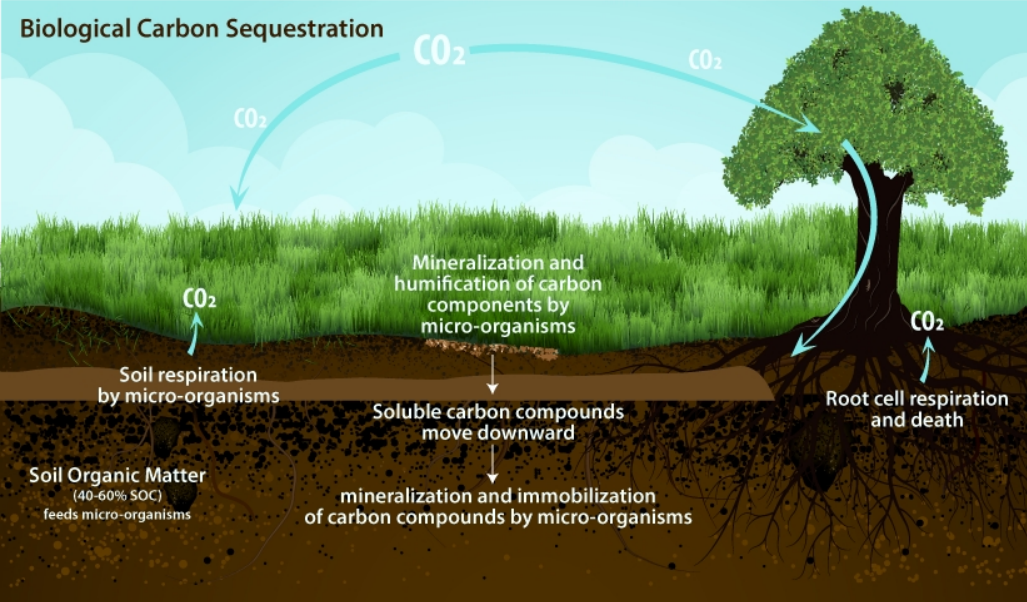
Japanese Iriai-satoyama forests



Hunting in Alsace







Climate

Scenary

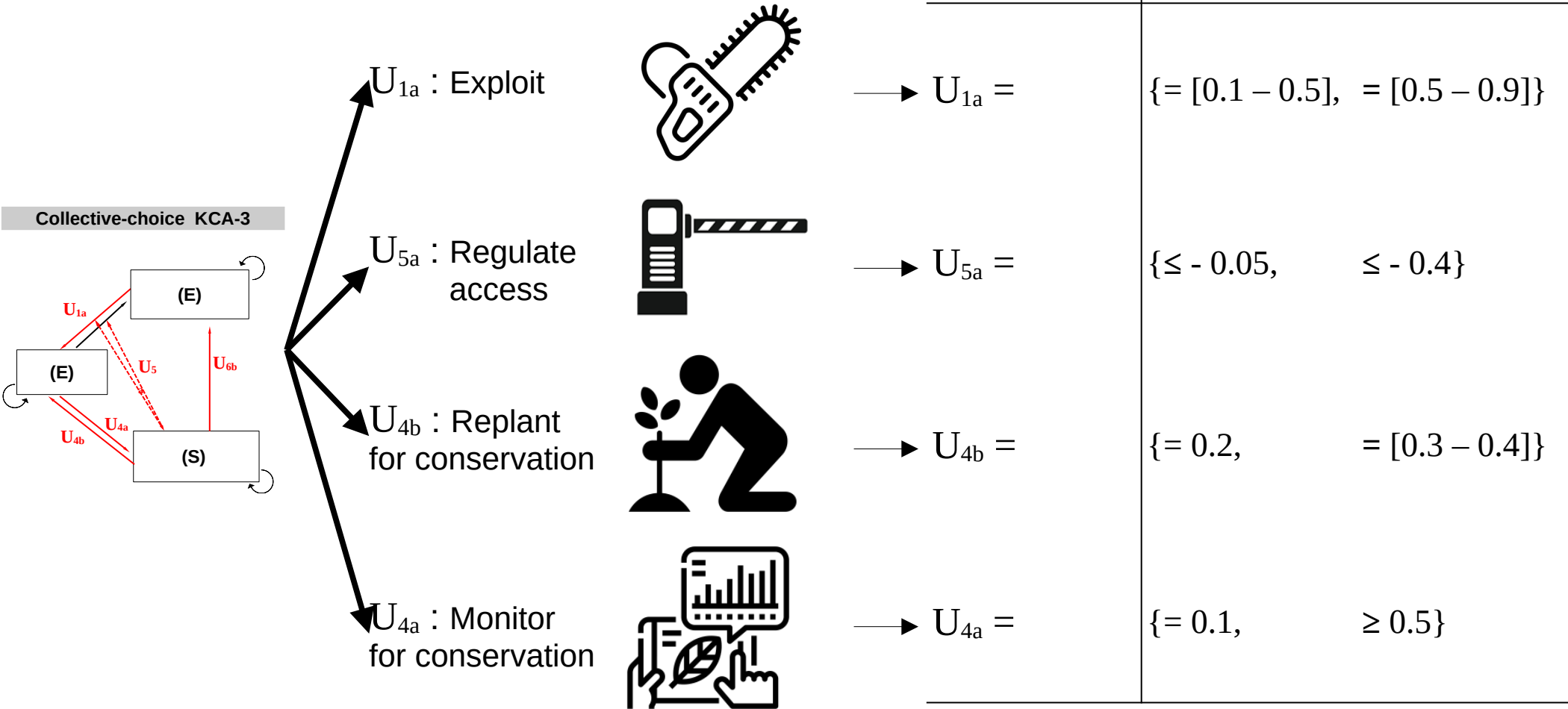




Originaux

Choix opérationnels ou quel niveau d'action ?

Adapter l'intensité, la fréquence des actions



Re-situer DAPP dans le cadre IAD

DAPP = représentation de la “situation d’action”

